

Interpreting Belle II excess with light dark matter

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Based on arXiv: 2401.10112

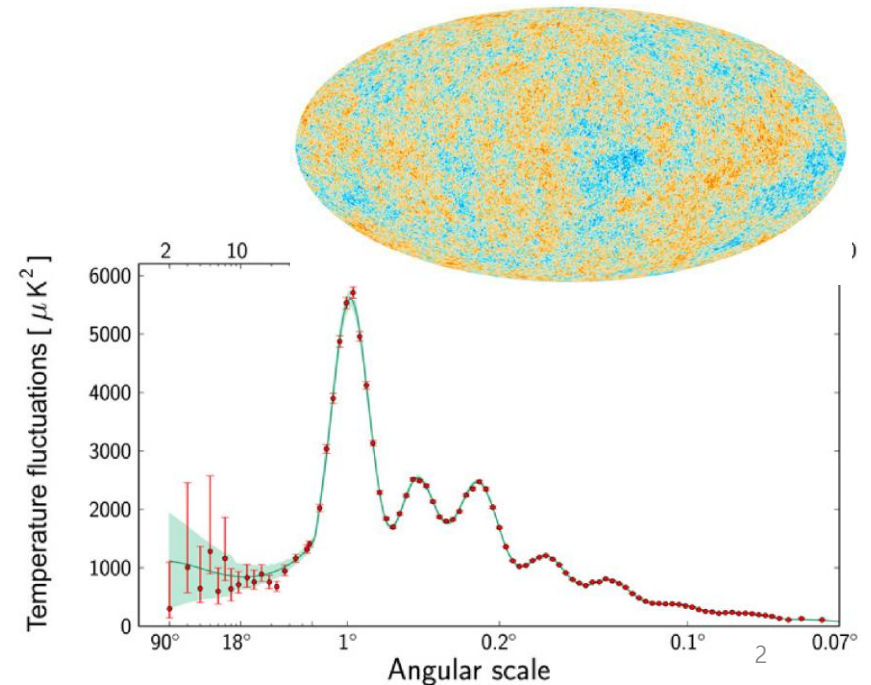
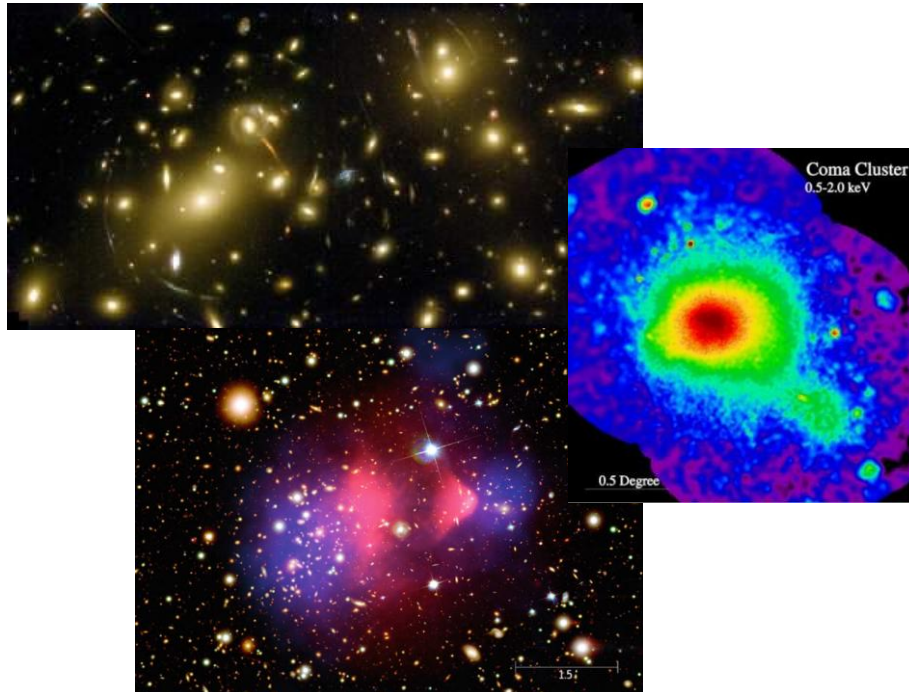
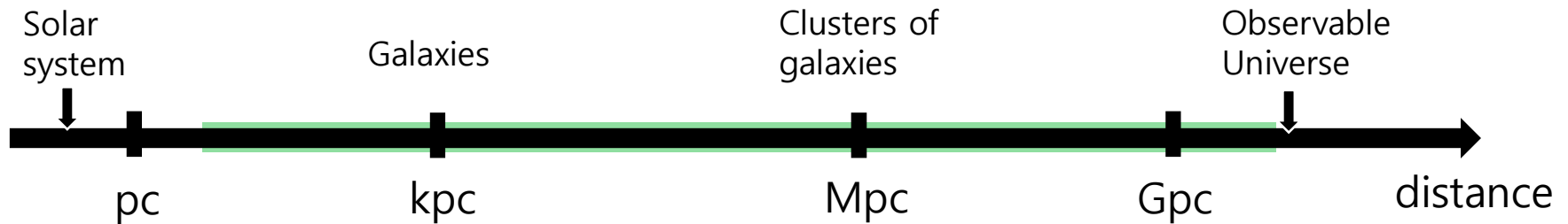
In collaboration with Shu-Yu Ho (Academia Sinica), Pyungwon Ko (KIAS)

2025. 2. 22 (Sat)



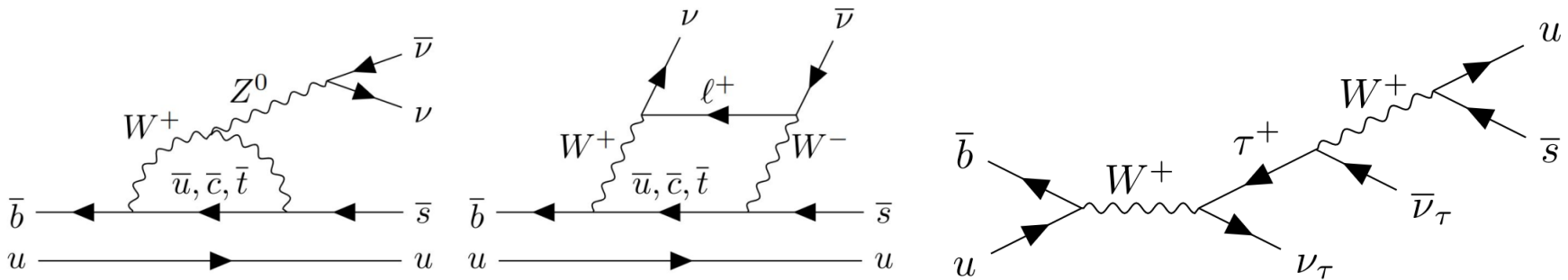
Evidences – Dark Matter

- There are undeniable evidences for dark matter in a wide range of distance scales



Measurement of $B^+ \rightarrow K^+ \nu \bar{\nu}$

- The $B^+ \rightarrow K^+ \nu \bar{\nu}$ process is known with high accuracy in the SM:
 - $Br(B^+ \rightarrow K^+ \nu \bar{\nu}) = (5.58 \pm 0.37) \times 10^{-6}$ HPQCD, PRD 2023



$$\mathcal{L}_{b \rightarrow s \nu \bar{\nu}} = -C_\nu \bar{s}_L \gamma^\mu b_L \bar{\nu} \gamma^\mu \nu$$

$$C_\nu = \frac{g_W^2}{M_W^2} \frac{g_W^2 V_{ts}^* V_{tb}}{16\pi^2} \left[\frac{x_t^2 + 2x_t}{8(x_t - 1)} + \frac{3x_t^2 - 6x_t}{8(x_t - 1)^2} \ln x_t \right],$$

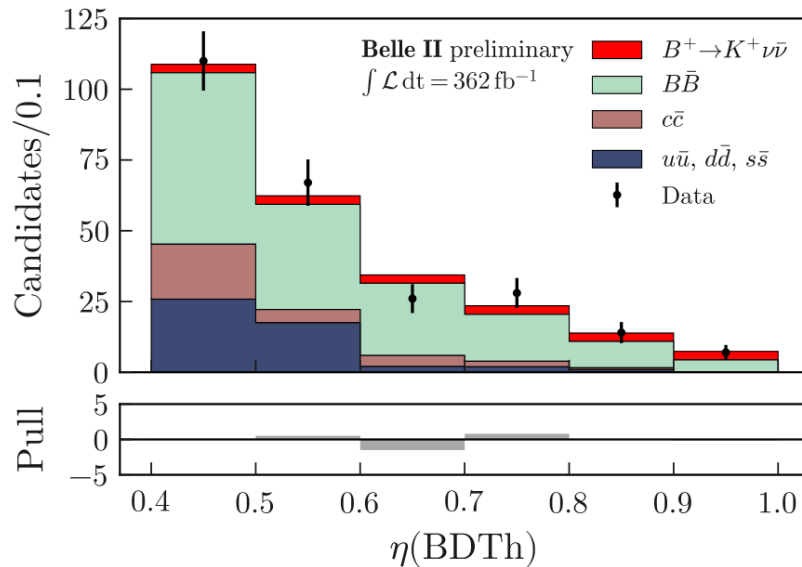
where $x_t = m_t^2 / M_W^2$.

Measurement of $B^+ \rightarrow K^+ \nu \bar{\nu}$

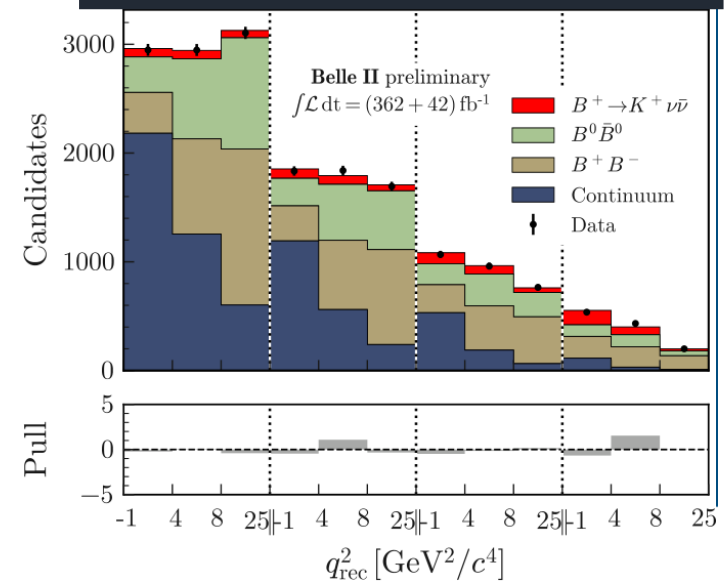
Belle II, 2311.14647

- **Two ways** of tagging
 - HTA: Better resolution, purity
 - ITA: Better efficiency

Hadronic tagging (HTA)



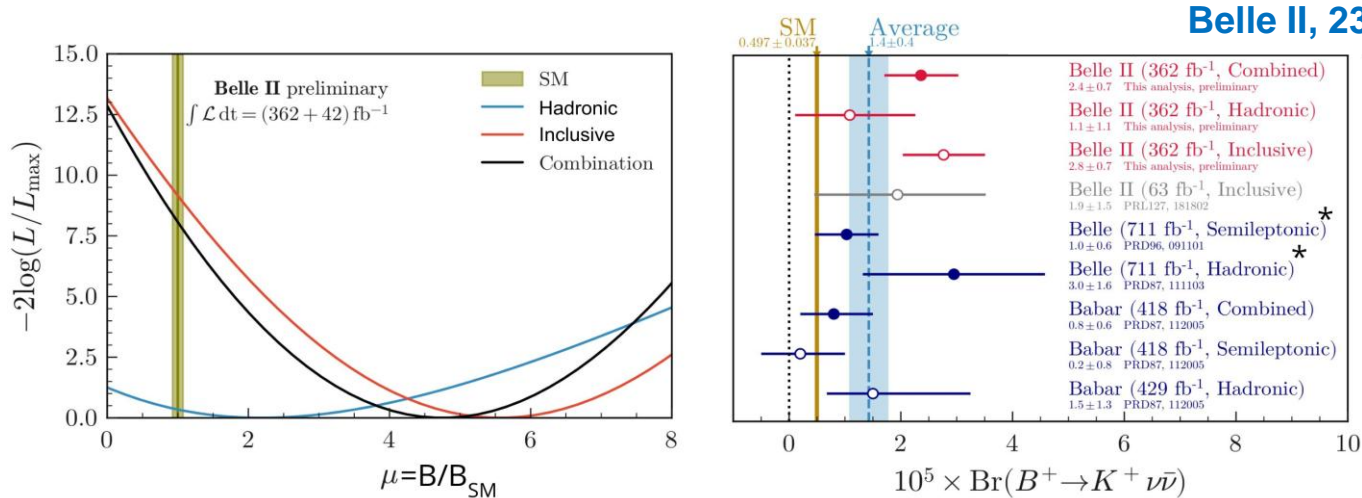
Inclusive tagging (ITA)



$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{HTA}} = (1.1^{+0.9+0.8}_{-0.8-0.5}) \times 10^{-5}$$

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{ITA}} = (2.7 \pm 0.5 \pm 0.5) \times 10^{-5}$$

Measurement of $B^+ \rightarrow K^+ \nu \bar{\nu}$



- $Br(B^+ \rightarrow K^+ \nu \bar{\nu})_{Exp} = (2.3 \pm 0.7) \times 10^{-5}$
 - Prob(null signal from $B^+ \rightarrow K^+ \nu \bar{\nu}$) = 0.012%
 - ➔ Significance of observation: 3.5σ
 - Prob($B^+ \rightarrow K^+ \nu \bar{\nu}$)_{SM} = 0.17% (2.8σ tension with the SM prediction)
- $Br(B^+ \rightarrow K^+ E_{mis})_{NP} = (1.8 \pm 0.7) \times 10^{-5}$
 - **Indirect NP effects:** The presence of heavy NP particles
 - **Direct NP effects:** the presence of new invisible particles

Solutions: EFT-approach

X. He et al, 2309.12741

- Real/Complex scalar DM

$$\mathcal{O}_{q\phi}^{S, sb} = (\bar{s}b)(\phi^\dagger\phi),$$

$$\mathcal{O}_{q\phi}^{V, sb} = (\bar{s}\gamma^\mu b)(\phi^\dagger i\overleftrightarrow{\partial}_\mu\phi), (\times)$$

- Majorana/Dirac fermion DM

$$\mathcal{O}_{q\chi 1}^{S, sb} = (\bar{s}b)(\bar{\chi}\chi),$$

$$\mathcal{O}_{q\chi 2}^{S, sb} = (\bar{s}b)(\bar{\chi}i\gamma_5\chi),$$

$$\mathcal{O}_{q\chi 1}^{V, sb} = (\bar{s}\gamma^\mu b)(\bar{\chi}\gamma_\mu\chi), (\times)$$

$$\mathcal{O}_{q\chi 2}^{V, sb} = (\bar{s}\gamma^\mu b)(\bar{\chi}\gamma_\mu\gamma_5\chi),$$

$$\mathcal{O}_{q\chi 1}^{T, sb} = (\bar{s}\sigma^{\mu\nu} b)(\bar{\chi}\sigma_{\mu\nu}\chi), (\times)$$

$$\mathcal{O}_{q\chi 2}^{T, sb} = (\bar{s}\sigma^{\mu\nu} b)(\bar{\chi}\sigma_{\mu\nu}\gamma_5\chi), (\times)$$

- Real/Complex vector DM

$$\mathcal{O}_{qX}^{S, sb} = (\bar{s}b)(X_\mu^\dagger X^\mu),$$

$$\mathcal{O}_{qX 1}^{T, sb} = \frac{i}{2}(\bar{s}\sigma^{\mu\nu} b)(X_\mu^\dagger X_\nu - X_\nu^\dagger X_\mu), (\times)$$

$$\mathcal{O}_{qX 2}^{T, sb} = \frac{1}{2}(\bar{s}\sigma^{\mu\nu}\gamma_5 b)(X_\mu^\dagger X_\nu - X_\nu^\dagger X_\mu), (\times)$$

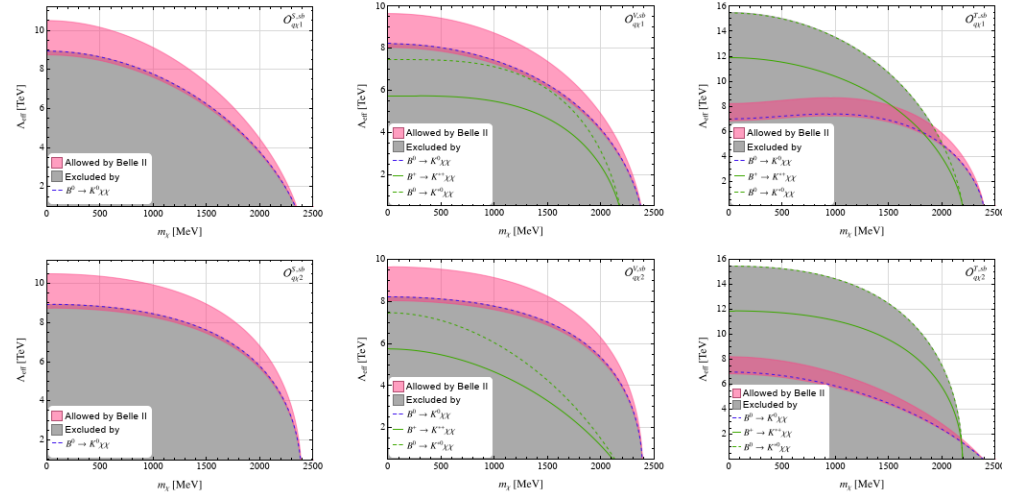
$$\mathcal{O}_{qX 2}^{V, sb} = (\bar{s}\gamma_\mu b)\partial_\nu(X^{\mu\dagger}X^\nu + X^{\nu\dagger}X^\mu),$$

$$\mathcal{O}_{qX 3}^{V, sb} = (\bar{s}\gamma_\mu b)(X_\rho^\dagger\overleftrightarrow{\partial}_\nu X_\sigma)\epsilon^{\mu\nu\rho\sigma},$$

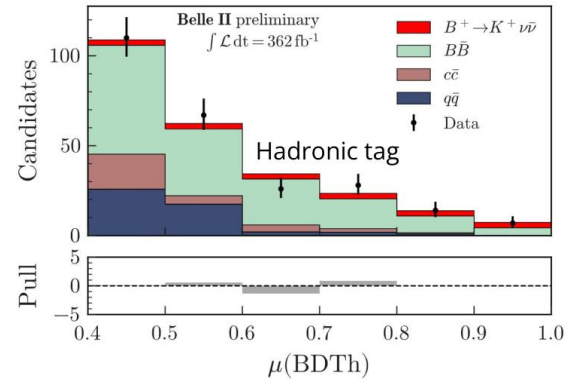
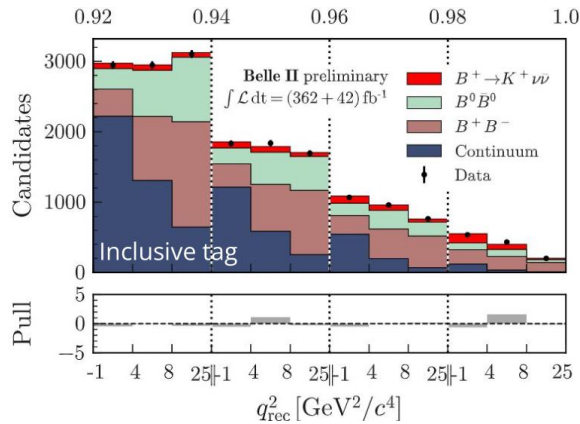
$$\mathcal{O}_{qX 4}^{V, sb} = (\bar{s}\gamma^\mu b)(X_\nu^\dagger i\overleftrightarrow{\partial}_\mu X^\nu), (\times)$$

$$\mathcal{O}_{qX 5}^{V, sb} = (\bar{s}\gamma_\mu b)i\partial_\nu(X^{\mu\dagger}X^\nu - X^{\nu\dagger}X^\mu), (\times)$$

$$\mathcal{O}_{qX 6}^{V, sb} = (\bar{s}\gamma_\mu b)i\partial_\nu(X_\rho^\dagger X_\sigma)\epsilon^{\mu\nu\rho\sigma}. (\times)$$



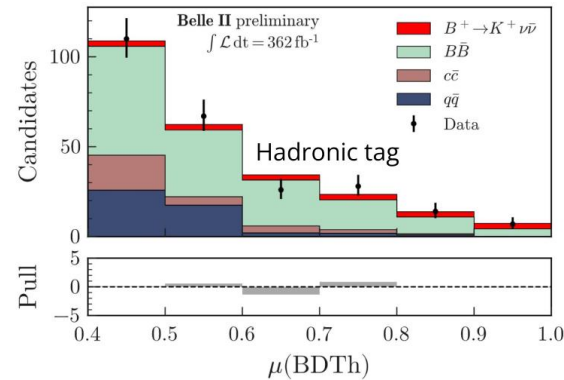
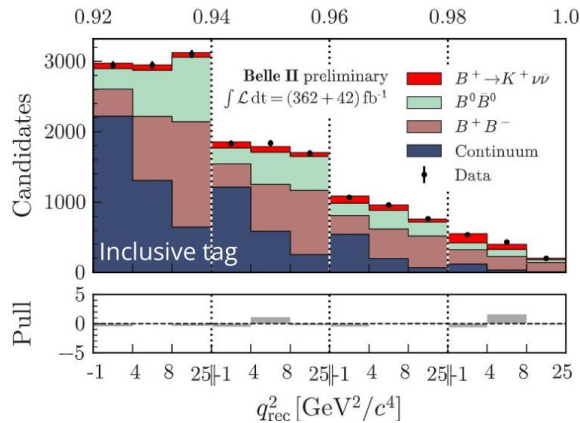
Solutions: 2- or 3-body decay



- Belle II provides information on the q_{rec}^2 spectrum
 - q_{rec}^2 : mass squared of the neutrino pair
 - A peak localized around $q_{rec}^2 = 4 \text{ GeV}^2$
 - Two-body decay ($B \rightarrow KX$), $m_X = 2 \text{ GeV}$

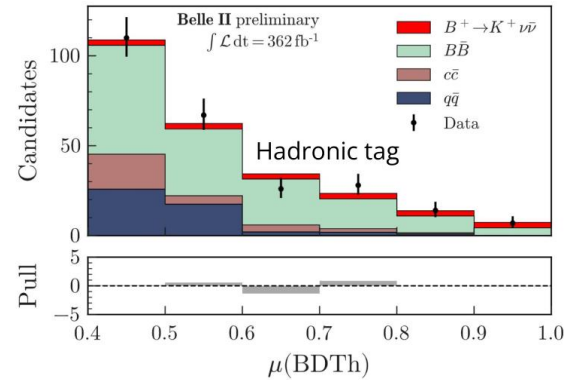
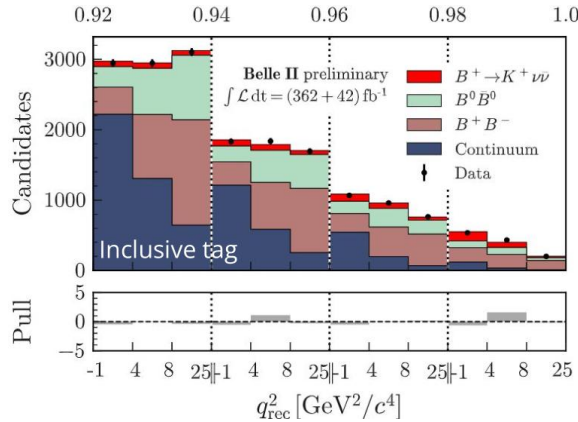
W. Altmannshofer et al, 2311.14629

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 - A peak localized around $q_{rec}^2 = 4 \text{ GeV}^2$
 - Two-body decay ($B \rightarrow KX$), $m_X = 2 \text{ GeV}$ W. Altmannshofer et al, 2311.14629
 - 2.8σ tension under the assumption of heavy new physics
 - No excess was found in the BaBar measurements of $B \rightarrow K^* \nu \bar{\nu}$
 - A global analysis of the BelleII and BaBar data leads to $Br(B \rightarrow KX) = (5.1 \pm 2.1) \times 10^{-6}$ with a reduced significance of $\approx 2.4\sigma$

Solutions: 2- or 3-body decay

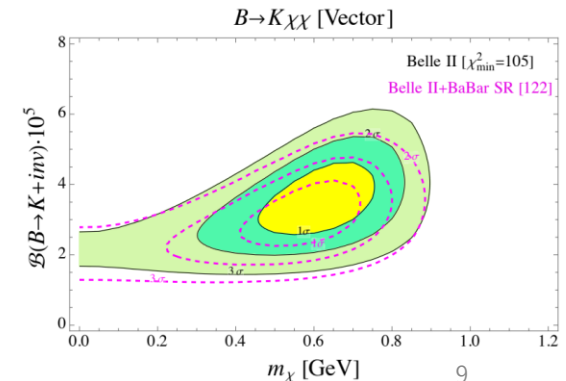
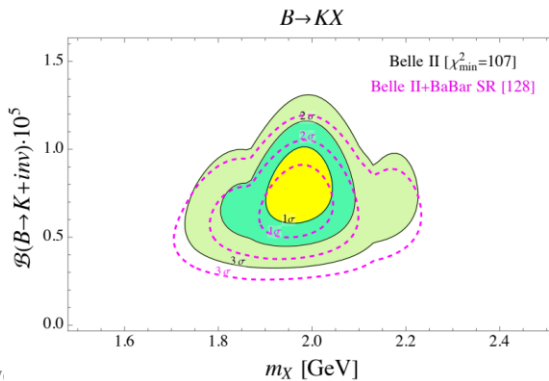
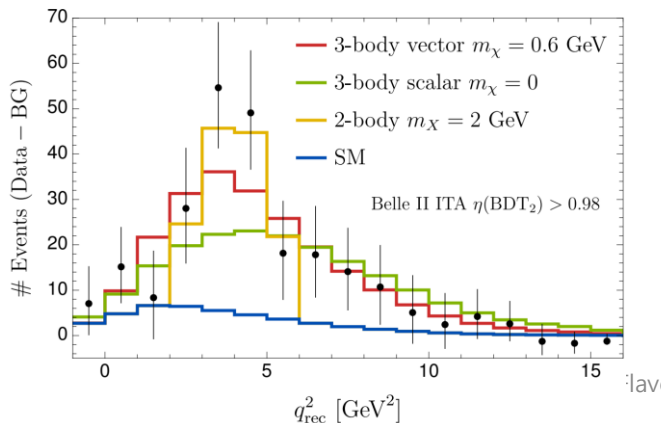


• Belle II provides information on the q_{rec}^2 spectrum

- q_{rec}^2 : mass squared of the neutrino pair
- A **peak** localized around $q_{rec}^2 = 4\text{GeV}^2$
- Two-body decay ($B \rightarrow KX$), $m_X = 2\text{ GeV}$
- Three-body decay ($B \rightarrow KXX$), $m_X < 0.6\text{ GeV}$

W. Altmannshofer et al, 2311.14629

K. Fridell et al, 2312.12507



Solutions: 2-body decay

W. Altmannshofer et al, 2311.14629

- Light particle X
 - Light neutral vector boson Z'
 - Flavoured axions and ALPs
- Light \rightarrow on-shell: $m_X < m_B - m_K$: $m_X = 2 \text{ GeV}$
- Undetected particle X is stable, long-lived or decays invisibly
 - Couplings to electrons, muons, and light quarks should be absent or sufficiently small
- For $B \rightarrow K^* \nu \bar{\nu}$, only BaBar data is available, there is no excess seen
 - Use the $B \rightarrow K^* \nu \bar{\nu}$ measurements of BaBar to set an upper limit on $\text{Br}(B \rightarrow K^* \nu \bar{\nu})$

Solutions: 2-body decay

- $B \rightarrow KZ'$ decay rate
 - $m_{Z'} = 2\text{GeV}$

$$\Gamma_{B \rightarrow KZ'}^{(4)} = \frac{|g_V^{(4)}|^2}{64\pi} \frac{m_B^3}{m_{Z'}^2} \lambda^{\frac{3}{2}} f_+,$$

$$\Gamma_{B \rightarrow KZ'}^{(5)} = \frac{|g_V^{(5)}|^2}{16\pi} \frac{m_B m_{Z'}^2}{\Lambda^2} \left(1 + \frac{m_K}{m_B}\right)^{-2} \lambda^{\frac{3}{2}} f_T,$$

$$\Gamma_{B \rightarrow KZ'}^{(6)} = \frac{|g_V^{(6)}|^2}{64\pi} \frac{m_B^3 m_{Z'}^2}{\Lambda^4} \lambda^{\frac{3}{2}} f_+,$$

W. Altmannshofer et al, 2311.14629

Including couplings up to dimension 6, the interaction Lagrangian is [47]

$$\mathcal{L}_{Z'} \supset \left\{ g_L^{(4)} Z'_\mu (\bar{s} \gamma^\mu P_L b) + \frac{g_L^{(5)}}{\Lambda} Z'_{\mu\nu} (\bar{s} \sigma^{\mu\nu} P_R b) + \frac{g_L^{(6)}}{\Lambda^2} \partial^\nu Z'_{\mu\nu} (\bar{s} \gamma^\mu P_L b) + \text{h.c.} \right\} + \{L \leftrightarrow R\}, \quad (2)$$

$$g_V^{(d)} = g_R^{(d)} + g_L^{(d)} \text{ and } g_A^{(d)} = g_R^{(d)} - g_L^{(d)}.$$

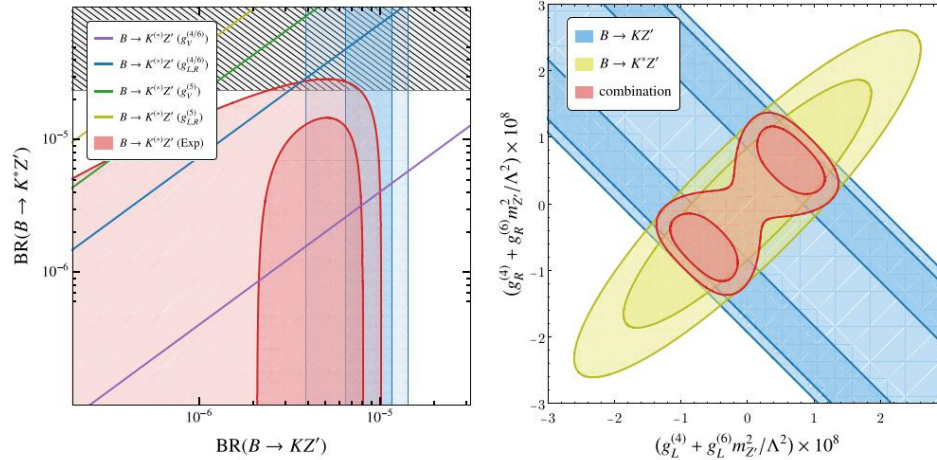
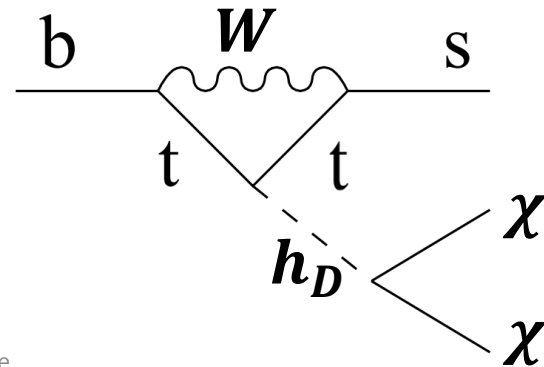
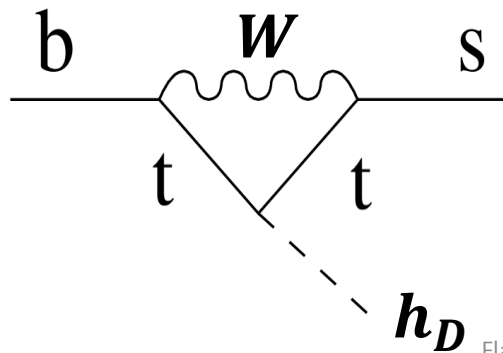
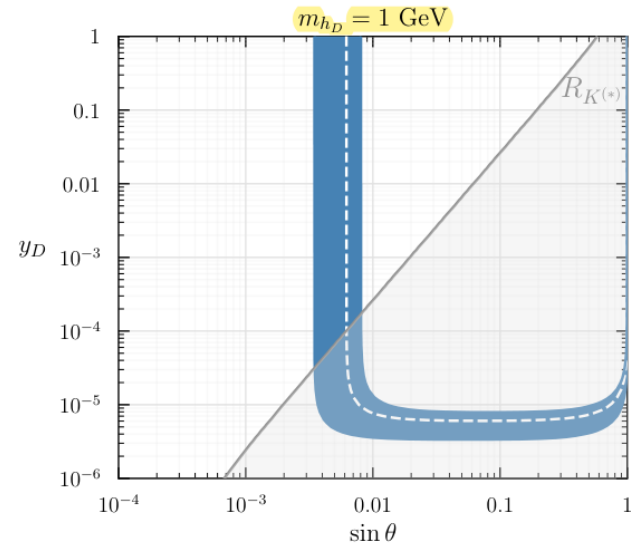
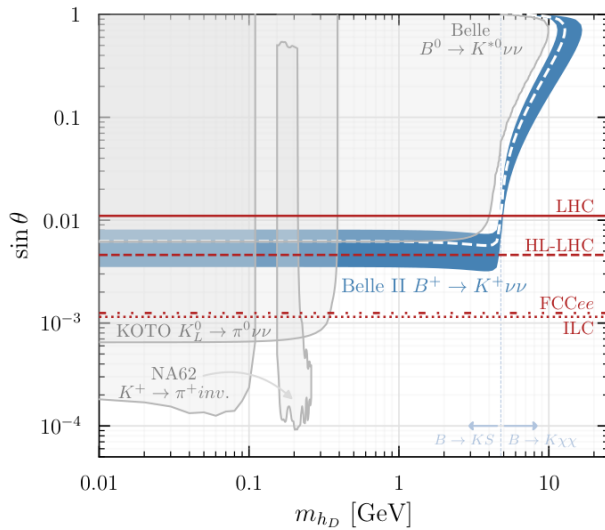


FIG. 2: *Left*: Correlations between $B \rightarrow KZ'$ and $B \rightarrow K^*Z'$ (colored lines) for the different $\bar{s}bZ'$ operators considered in this work. These are compared to the experimental data stemming from the combination of Belle-II, Babar and Belle measurements, which is represented by the red regions corresponding to $\Delta\chi^2 = 2.3$ and $\Delta\chi^2 = 6.18$. Belle's upper limit (hatched region at 2σ) and the new Belle II measurement (blue vertical band at 1σ and 2σ). *Right*: preferred regions in the $g_L - g_R$ plane. One can see that (approximately) vectorial couplings of the order of 10^{-8} are suggested by current data.

Solutions: 2- or 3-body decay

- Dark Higgs on-shell decay or three-body decay [McKeen et al, 2312.00982](#)

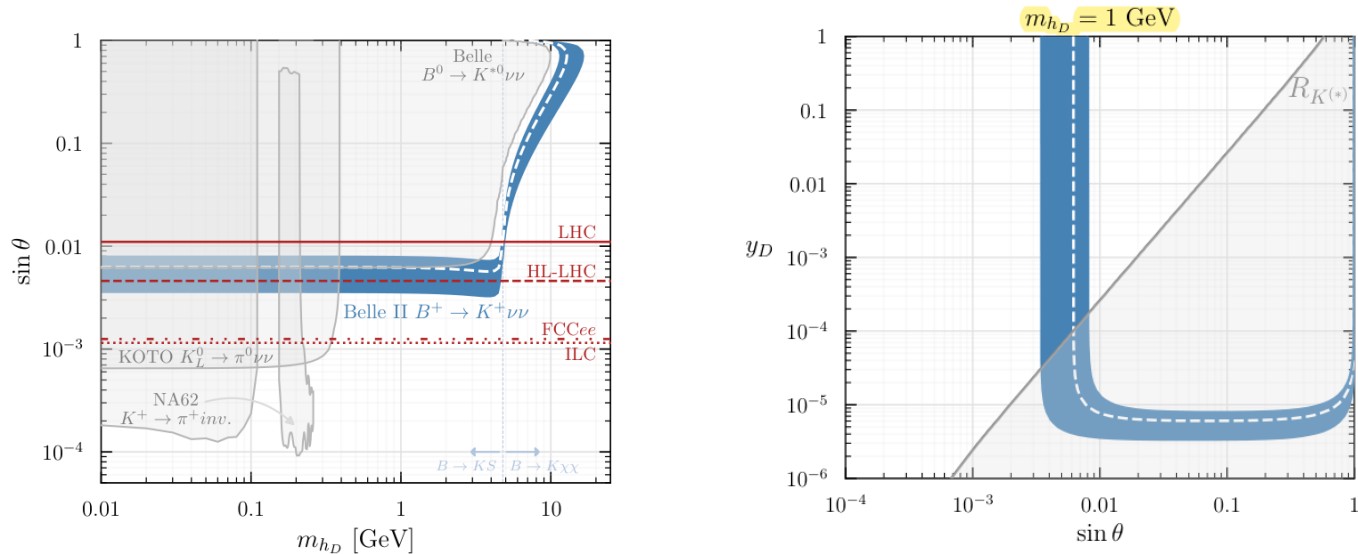
$$\mathcal{L}_{\text{DM}} = y_D \phi \bar{\chi} \chi$$



Solutions: 2- or 3-body decay

- Dark Higgs on-shell decay or three-body decay McKeen et al, 2312.00982

$$\mathcal{L}_{\text{DM}} = y_D \phi \bar{\chi} \chi$$



- **Extremely large relic density**

- $\Omega h^2 \simeq 10^{20} \left(\frac{10^{-4}}{y_D}\right)^2 \left(\frac{\sin \theta}{10^{-3}}\right)^2 \left(\frac{m_\chi}{100 \text{ MeV}}\right)^2 \left(\frac{1 \text{ GeV}}{m_{H_1}}\right)^2$: overclose the Universe
- Either introduce a new DM annihilation or allow DM to decay
- In that sense, **fermion DM does not work...**

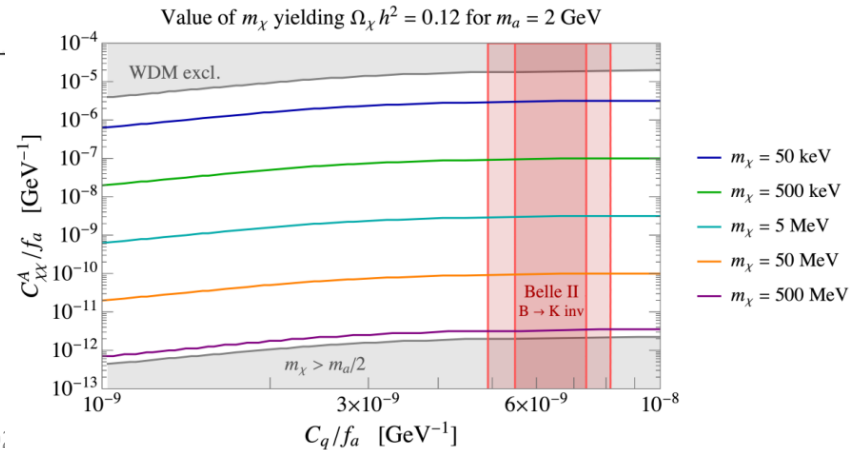
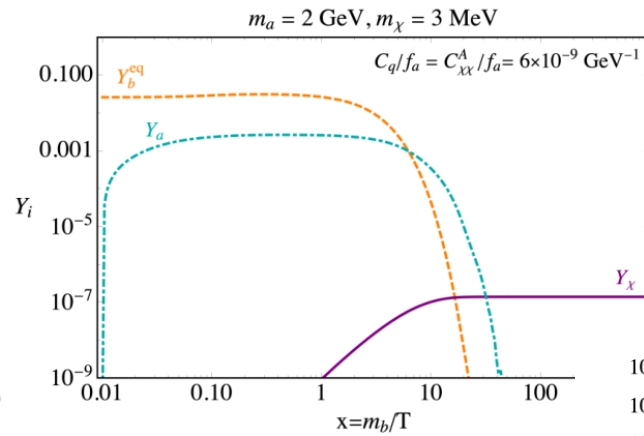
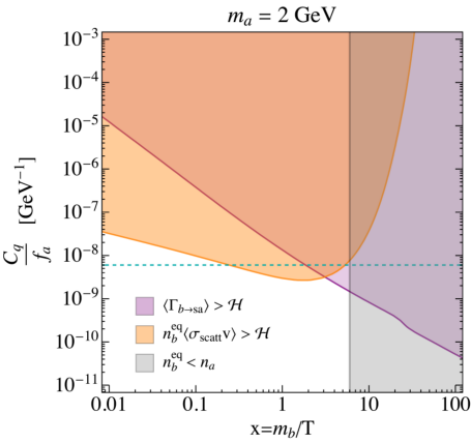
Solutions: 2-body decay

Lorenzo Calibbi et al, 2502.04900

- ALP portal

$$\mathcal{L}_{aff} = \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu \left(C_{fi f_j}^V + C_{fi f_j}^A \gamma_5 \right) f_j + \mathcal{L}_{a\chi\chi} = \frac{\partial_\mu a}{2f_a} \bar{\chi} C_{\chi\chi}^A \gamma^\mu \gamma_5 \chi$$

- DM freeze-in production: $\Gamma(b \rightarrow sa), \sigma(b\bar{b} \rightarrow ag), \sigma(bg \rightarrow ba)$



$$\text{BR}(a \rightarrow gg) \simeq 93\%, \quad \text{BR}(a \rightarrow s\bar{s}) \simeq 7\%, \quad \text{BR}(a \rightarrow \gamma\gamma) \simeq 2 \times 10^{-5}, \quad (17)$$

which is consistent with the results in Ref. [45]. The decay into DM is subdominant for $m_\chi \ll m_a$:

$$\text{BR}(a \rightarrow \chi\bar{\chi}) \simeq 2.6 \times 10^{-6} \times \left(\frac{C_{\chi\chi}^A}{C_q} \right)^2 \left(\frac{m_\chi}{1 \text{ MeV}} \right)^2. \quad (18)$$

The resulting ALP decay length is

$$c\tau_a \simeq 65 \text{ m} \times \left(\frac{10^8 \text{ GeV}}{f_a/C_q} \right)^2. \quad (19)$$

20;

Solutions: 2-body decay

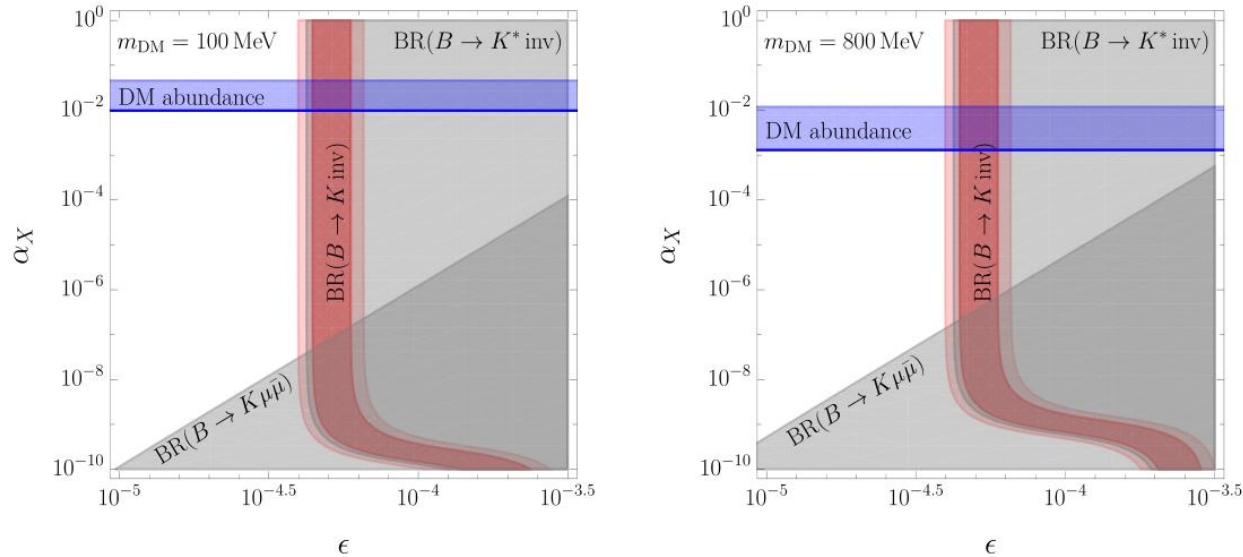
- Dark Photon portal through kinetic mixing [Lorenzo Calibbi et al, 2502.04900](#)

$$\mathcal{L} \supset \frac{1}{2} \bar{\psi}(i\not{\partial} - m_R)\psi + \frac{g_X}{2} \bar{\psi} \not{X} \gamma_5 \psi - \frac{y_R}{2\sqrt{2}} \bar{\psi} \psi \varphi - \frac{y_R}{2\sqrt{2}} \bar{\psi} i \gamma_5 \psi a$$

- BelleII excess ($B \rightarrow K + \text{Dark Photon with } 2\text{GeV}$)
 - The partial decay widths for decays to SM particles: suppressed by kinetic mixing
 - The partial width for decays of the dark photon to DMs: **Not** suppressed by the kinetic mixing
- DM freeze-out production
 - The relevant process is the DM annihilation into dark Higgs bosons, $\psi\psi \rightarrow \varphi\varphi$, which subsequently decay to SM particles
 - The annihilation process is **p-wave** suppressed
 - To satisfy BBN constraints, we require the dark Higgs lifetime to be shorter than $\tau_\varphi \lesssim 0.1 \text{ s} \rightarrow m_\varphi > 4 \text{ MeV}$
 - Relic density:
$$\Omega_\psi h^2 \approx 0.1 \times \left(\frac{0.5 \text{ GeV}}{m_{\text{DM}}} \right)^2 \left(\frac{0.002}{\alpha_X} \right)^2$$

Solutions: 2-body decay

Lorenzo Calibbi et al, 2502.04900



solid blue line corresponds to a dark Higgs with mass $m_\varphi = 4 \text{ MeV}$ and the blue shaded region displays the range $m_\varphi \in [4 \text{ MeV}, m_{\text{DM}}]$.

- DM scattering off a Xenon nucleus: five orders of magnitude below the DM direct detection limit
- DM self-interaction cross section

$$\frac{\sigma_{\text{SI}}}{m_{\text{DM}}} = \frac{16\pi\alpha_X^2 v_{\text{DM}}^2}{m_X^3} \frac{x_{\text{DM}}(3 - 20x_{\text{DM}}^2 + 40x_{\text{DM}}^4)}{(1 - 4x_{\text{DM}}^2)^2}$$

$$\approx 1.1 \times 10^{-14} \left(\frac{\alpha_X}{10^{-2}}\right)^2 \left(\frac{v}{10^3 \text{ km/s}}\right)^2 \frac{x_{\text{DM}}(3 - 20x_{\text{DM}}^2 + 40x_{\text{DM}}^4)}{(1 - 4x_{\text{DM}}^2)^2} \frac{\text{cm}^2}{\text{g}}$$

Solutions: 2- or 3-body decay

- $B \rightarrow (K, K^*)\chi\bar{\chi}$ decays via a scalar mediator [A. Berezhnoy et al, 2502.14313](#)

$$\mathcal{L}_{\text{int}} = -\frac{ym_t}{v}\phi\bar{t}t - \kappa\phi\bar{\chi}\chi$$

$$\mathcal{L}_{b\rightarrow s\phi} = g_{b\rightarrow s\phi}\phi\bar{s}_L b_R + \text{h.c.}, \quad g_{b\rightarrow s\phi} = \frac{ym_b}{v} \frac{3\sqrt{2}G_F m_t^2 V_{ts}^* V_{tb}}{16\pi^2}.$$

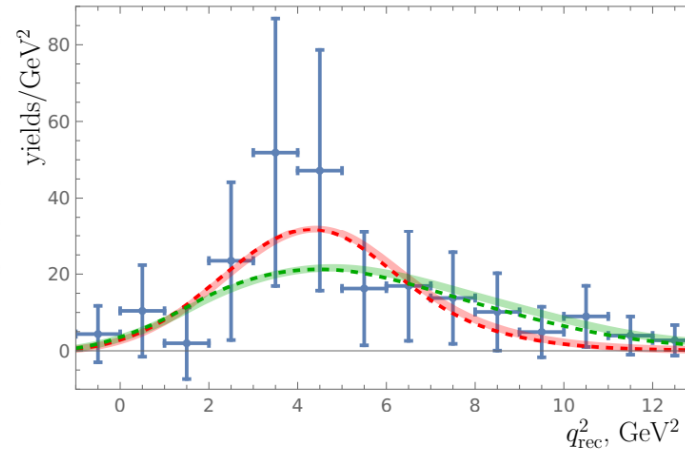
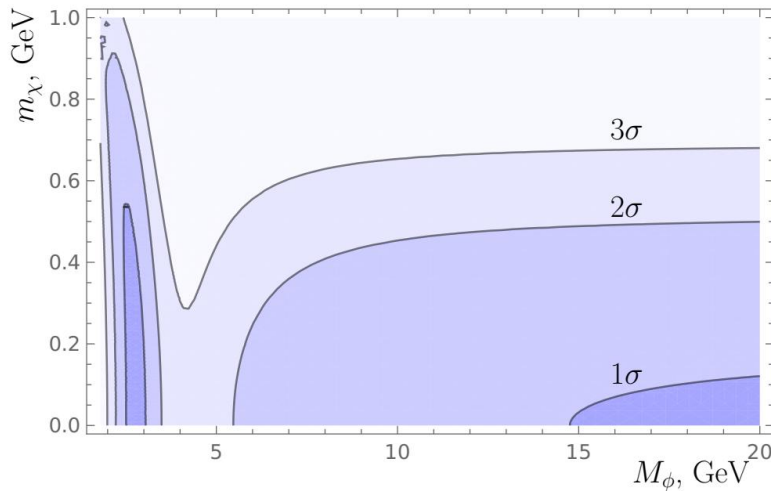
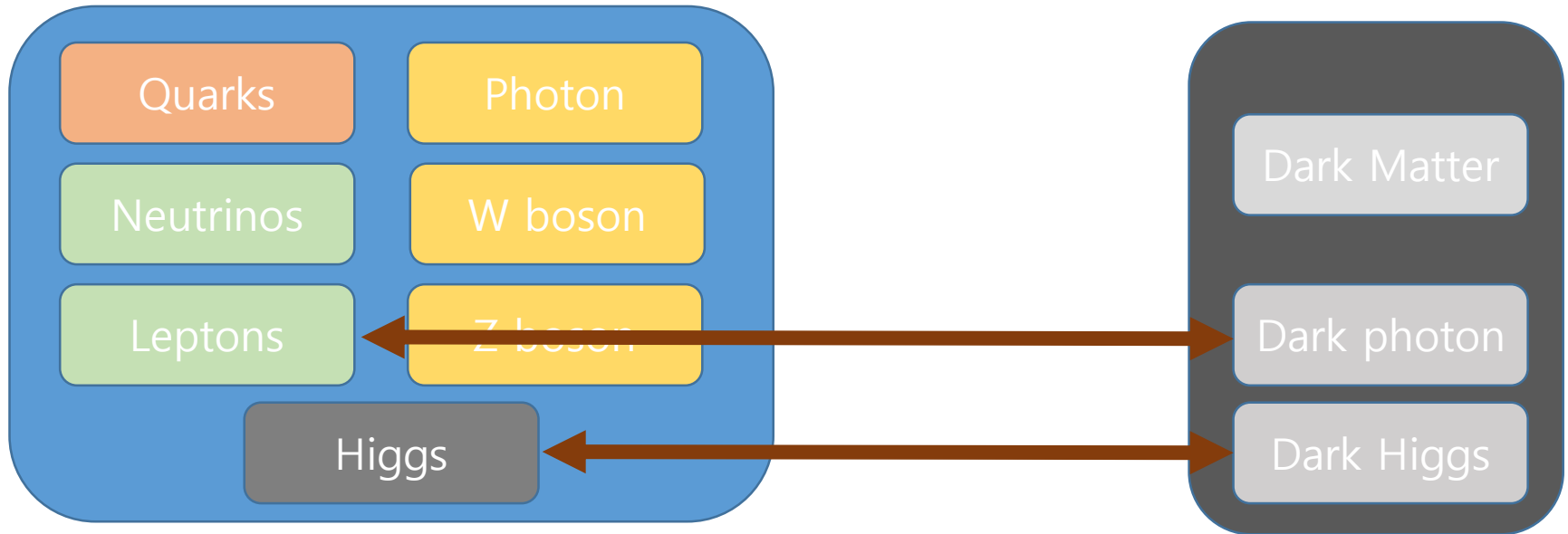


Figure 2: The Belle II data on the decay $B \rightarrow KM_X$ fitted by the DM model considered for different parameter values: $M_\phi = 2.8$ GeV, $\Gamma_\phi^0 = 2.8$ GeV and $m_\chi = 0$ GeV (red solid curve); $M_\phi = 20$ GeV, $\Gamma_\phi^0 = 0$ GeV and $m_\chi = 0$ GeV (green solid curve). The corresponding predictions for $B \rightarrow K^*M_X$ are also shown, assuming the same detection efficiency (red dashed and green dashed curves). Only excess events over the SM expectations are shown.

Can we find the integrated solution of **DM relic density** and $B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II?

$U(1)_{L_\mu-L_\tau}$ -charged DM + Dark Higgs

- $U(1)_{dark} \equiv U(1)_{L_\mu-L_\tau}$
 - Let's call Z' , $U(1)_{L_\mu-L_\tau}$ gauge boson, **dark photon** since it couple to DM

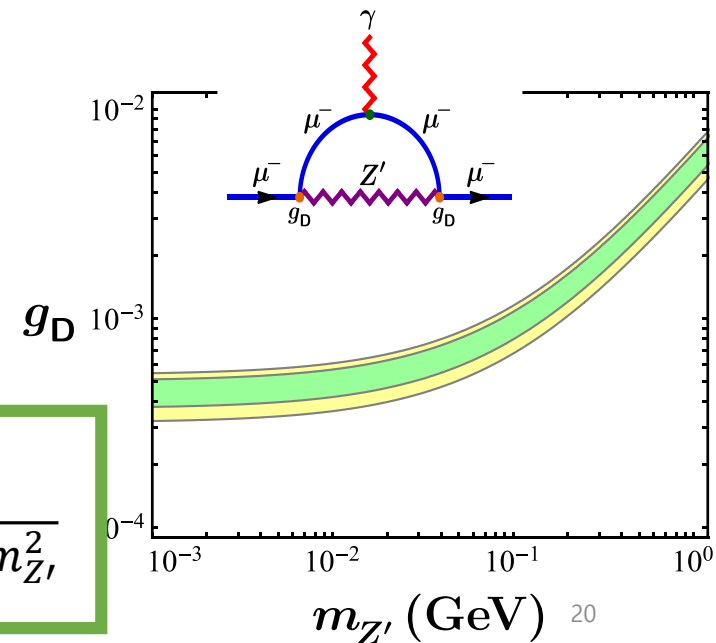
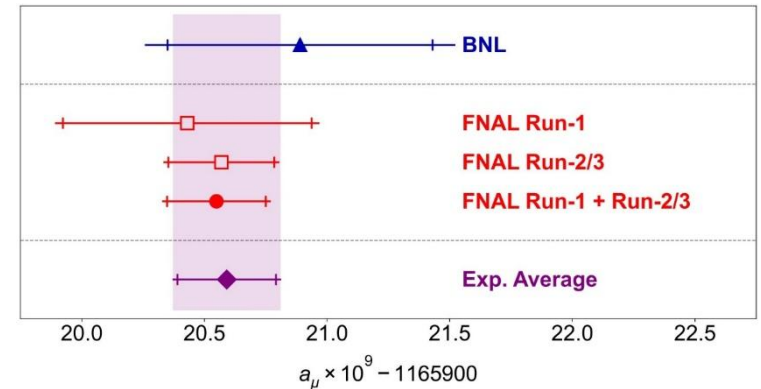
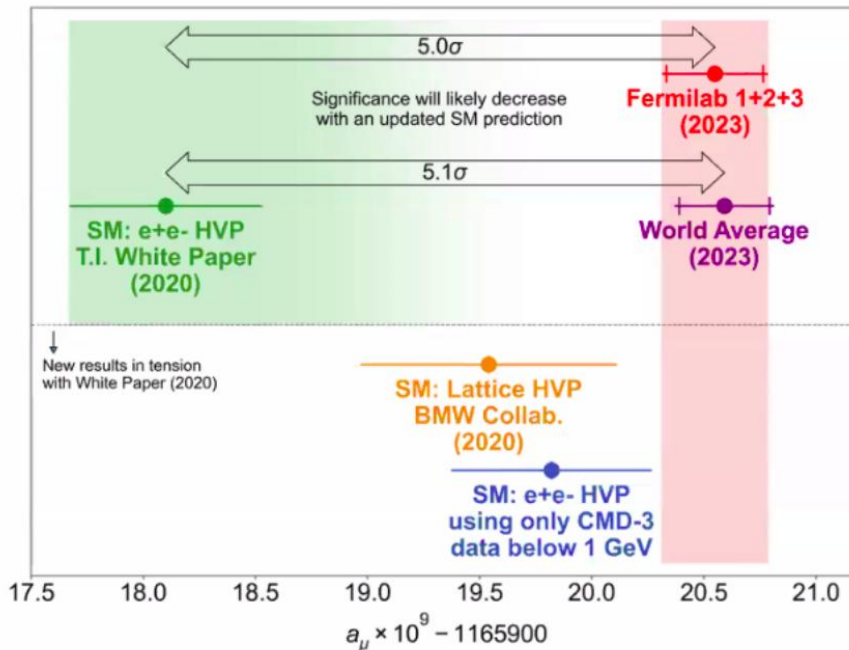


- **UV complete** $U(1)_{L_\mu-L_\tau}$ -charged **scalar** DM model
- Dark photon Z' gets massive through $U(1)_{L_\mu-L_\tau}$ breaking
- A new singlet scalar (**Dark Higgs**), which mixes with the SM Higgs

Evidences – Muon g-2

Muon g-2 collaboration, PRL 2023

- Muon g-2 experiment improves the precision of their previous result by a factor of 2



S. Baek, Deshpande, He, P. Ko, 2001

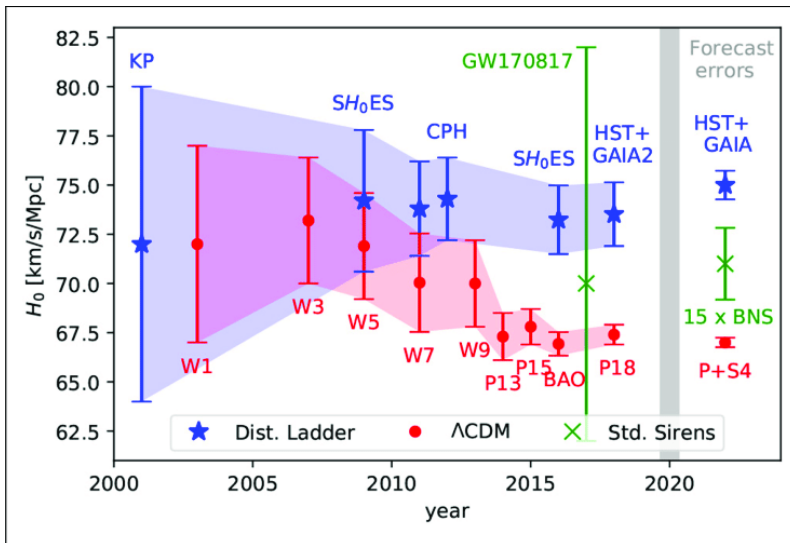
S. Baek, P. Ko, 2008

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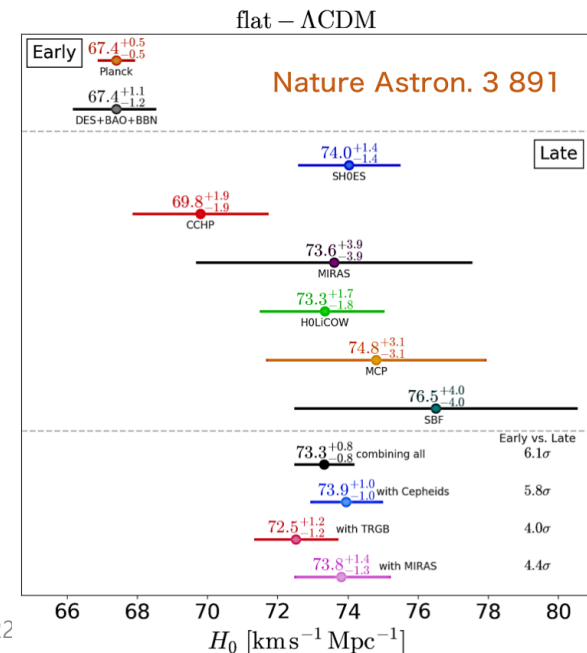
$$\Delta a_\mu = \frac{g_x^2}{4\pi^2} \int_0^1 dx \frac{m_\mu^2 x^2 (1-x)}{x^2 m_\mu^2 + (1-x)m_{Z'}^2}$$

Evidences – Hubble tension

- Large difference between early and late H_0 measurement
 - Late-time: $H_0 = 73.2 \pm 1.3 \text{ kms}^{-1}\text{Mpc}^{-1}$
 - Early-time: $H_0 = 67.4 \pm 0.5 \text{ kms}^{-1}\text{Mpc}^{-1}$
- The discrepancy either arises because
 - Our distance measurements are incorrect (ΔG_N)
 - Cosmological model we use to fit all those distances is incorrect (ΔN_{eff})



P. Shah et al, AAR 2021



Gauged $U(1)_{L_\mu - L_\tau}$ Z' model

- Gauge one of the differences of two lepton-flavor numbers

- $L_e - L_\mu, L_\mu - L_\tau, L_e - L_\tau$: **anomaly free** without extension of fermion contents

X. G. He et al, PRD 1991

- Symmetry including L_e is strongly constrained

- Charge assignments: $\widehat{Q}_{L_\mu - L_\tau}(\nu_\mu, \nu_\tau, \mu, \tau) = (1, -1, 1, -1)$

- No kinetic mixing between Z' and B @ high-energy

- Kinetic mixing is generated through



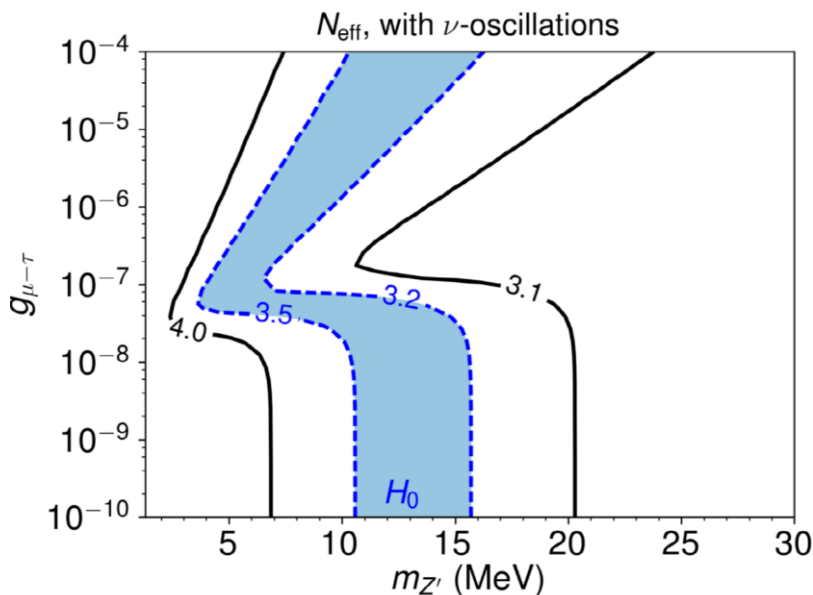
- $$\epsilon = -\frac{eg_{\mu-\tau}}{2\pi^2} \int_0^1 dx x(1-x) \log \left[\frac{m_\tau^2 - x(1-x)q^2}{m_\mu^2 - x(1-x)q^2} \right] \xrightarrow{m_\mu \gg q} -\frac{eg_{\mu-\tau}}{12\pi^2} \log \frac{m_\tau^2}{m_\mu^2} \simeq -\frac{g_{\mu-\tau}}{70}$$

Gauged $U(1)_{L_\mu-L_\tau}$ Z' model

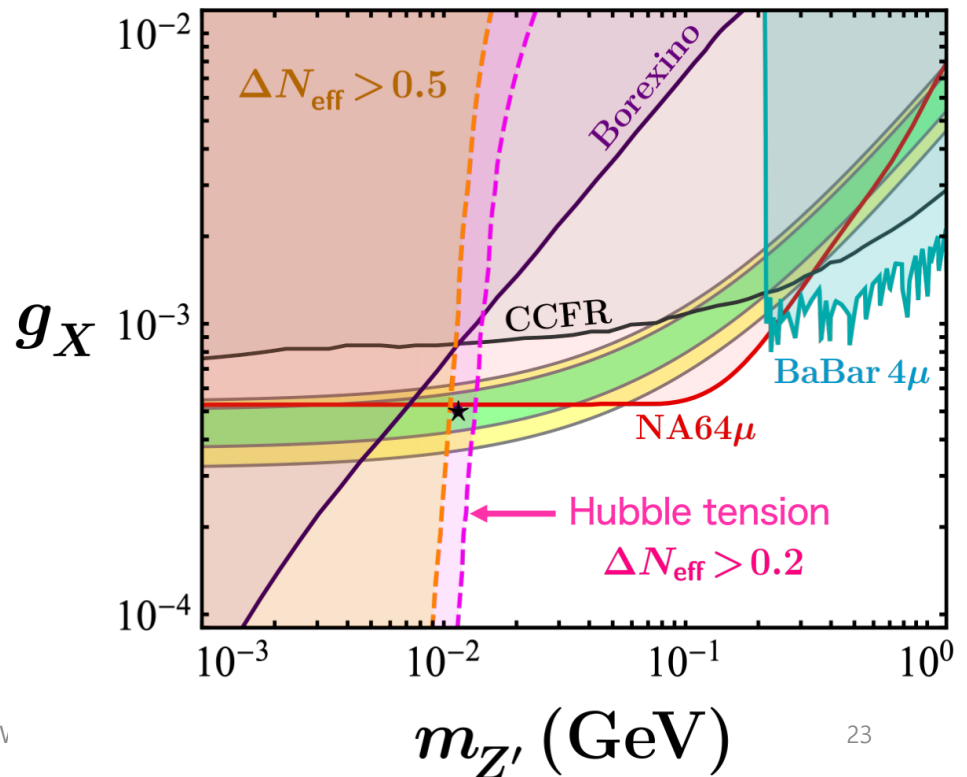
M. Escudero et al, JHEP 2019

• Hubble tension

- $\sim 10\text{MeV } Z'$ reached thermal equilibrium in the early Universe and decays, heating the neutrino population.
- The expansion rate of the universe departed from the predictions of standard ΛCDM cosmology at early times
- $0.2 < \Delta N_{\text{eff}} < 0.5$



• BP : $m_{Z'} = 11.5\text{MeV}$, $g_X = 5 \times 10^{-4}$



$U(1)_{L_\mu - L_\tau}$ -charged DM + Dark Higgs

- After electroweak and $U(1)_{L_\mu - L_\tau}$ symmetry breaking

$$\mathcal{H} = \frac{1}{\sqrt{2}}(0 \ v_H + h)^\top, \quad \Phi = \frac{1}{\sqrt{2}}(v_\Phi + \phi)$$

- Dark photon Z' gets massive: $m_{Z'} = g_X |Q_\Phi| v_\Phi$
- Two CP-even neutral scalar bosons mix each other due to non-zero of $\lambda_{H\Phi}$

$$H_1 = \phi \cos \theta - h \sin \theta, \quad H_2 = \phi \sin \theta + h \cos \theta$$

dark Higgs boson SM-like Higgs boson mixing angle

$$m_{H_1} < m_{H_2} \simeq 125 \text{ GeV}$$

$U(1)_{L_\mu - L_\tau}$ -charged DM + Dark Higgs

- Additional interactions with the dark Higgs

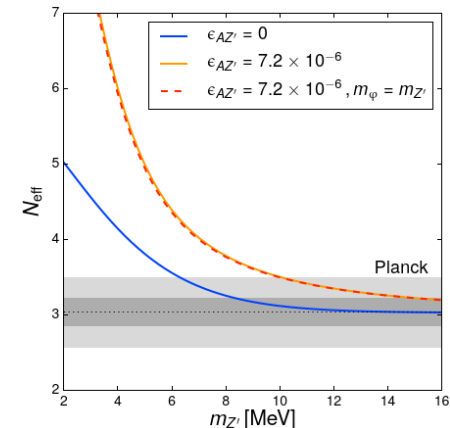
$$\mathcal{L}_\phi \supset \frac{1}{2} g_X^2 Q_\Phi^2 Z'^\mu Z'_\mu \phi^2 + g_X^2 Q_\Phi^2 v_\Phi Z'^\mu Z'_\mu \phi - \lambda_\Phi v_\Phi \phi^3 - \lambda_H v_H h^3 - \frac{\lambda_{\Phi H}}{2} v_\Phi \phi h^2 - \frac{\lambda_{\Phi H}}{2} v_H \phi^2 h$$

• The SM-like Higgs invisible decay

- $H_2 \rightarrow H_1 H_1, Z' Z', X X^\dagger$
- SM Higgs mainly decays into dark photon and dark Higgs

$$\Gamma_{H_2 \rightarrow H_1 H_1} \simeq \Gamma_{H_2 \rightarrow Z' Z'} \propto \frac{\sin^2 \theta m_{H_2}^3}{v_\Phi^2} \gg \Gamma_{H_2 \rightarrow X X^\dagger} \propto \frac{\sin^2 \theta \lambda_{\Phi X}^2 v_\Phi^2}{m_{H_2}}$$

- $\text{Br}(H_2 \rightarrow \text{inv.}) = \frac{\Gamma_{H_2}^{ZZ^* \rightarrow 4\nu} + \Gamma_{H_2}^{H_1 H_1} + \Gamma_{H_2}^{Z' Z'} + \Gamma_{H_2}^{X X^\dagger}}{\Gamma_{H_2}^{\text{SM}} + \Gamma_{H_2}^{H_1 H_1} + \Gamma_{H_2}^{Z' Z'} + \Gamma_{H_2}^{X X^\dagger}} < 13\%$
- $\sin \theta \leq 0.01$ to satisfy the Higgs invisible decay



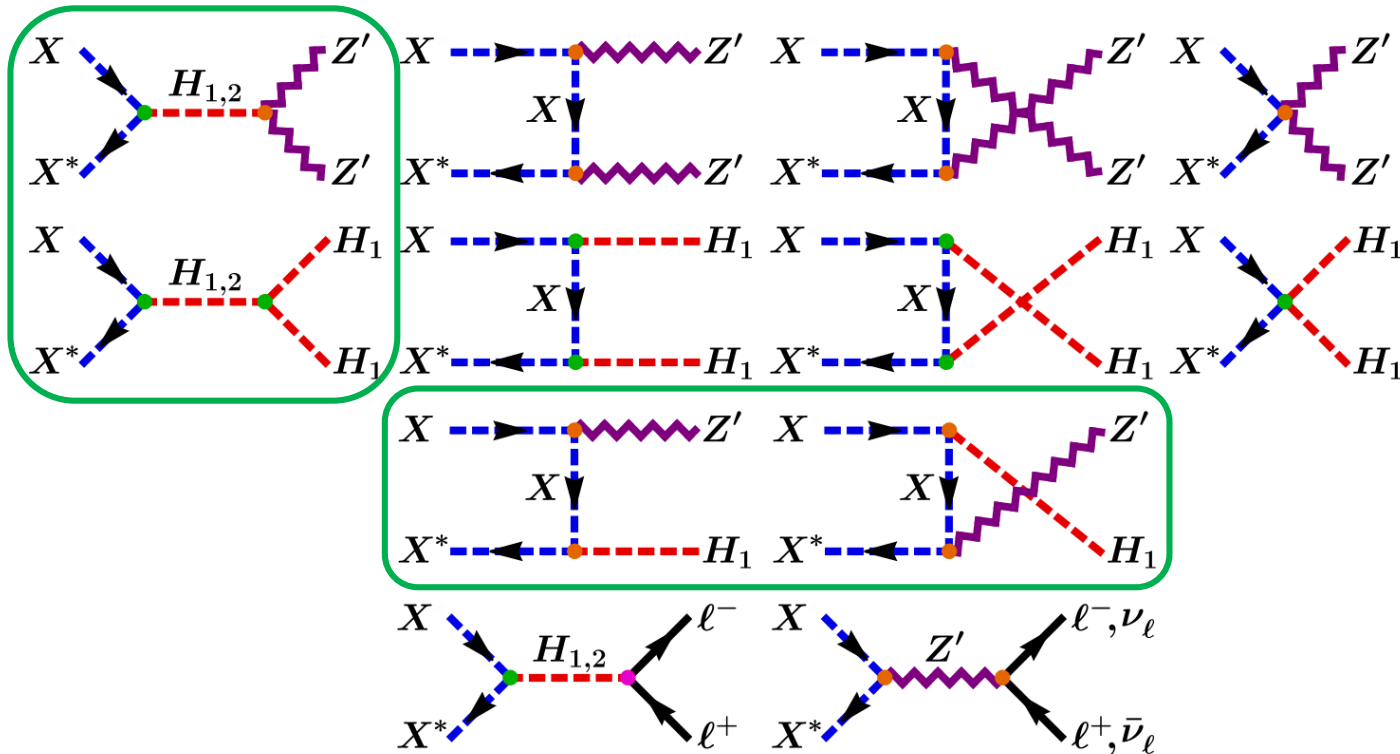
$U(1)_{L_\mu-L_\tau}$ -charged DM + Dark Higgs

- UV-complete $U(1)_{L_\mu-L_\tau}$ -charged scalar DM model

Baek, JK, Ko, 2204.04889

$$\mathcal{L}_{\text{DM}} = |D_\mu X|^2 - m_X^2 |X|^2 - \lambda_{\Phi X} |X|^2 \left(|\Phi|^2 - \frac{v_\Phi^2}{2} \right)$$

- DM annihilation channels



$U(1)_{L_\mu - L_\tau}$ -charged DM + Dark Higgs

Baek, JK, Ko, 2204.04889

- Thermal WIMP DM relic density

$$\Omega_{\text{WIMP}} \hat{h}^2 = 2\Omega_X \hat{h}^2 \simeq \frac{1.75 \times 10^{-10} \text{GeV}^{-2} x_f}{\sqrt{g_*} \langle \sigma v \rangle}$$

- DM direct detection

- $U(1)_{L_\mu - L_\tau}$ DM model without dark Higgs boson, DM-nucleon/electron scattering is highly suppressed: $\sigma_{\text{el}}^{X-p} \simeq 10^{-46} \text{cm}^2$, $\sigma_{\text{el}}^{X-e} \simeq 10^{-51} \text{cm}^2$
- We can have a sizable DM-nucleon scattering

$$\sigma_{\text{el}} \simeq \frac{4\mu_n^2 f_n^2 \lambda_{\Phi X}^2 \sin^2 \theta}{\pi} \left(\frac{m_n}{m_X} \right)^2 \left(\frac{v_\Phi}{v_H} \right)^2 \left(\frac{1}{m_{H_1}^2} - \frac{1}{m_{H_2}^2} \right)^2$$

$$\sigma_{\text{el}}^{X-n} \simeq \frac{\mu_n^2}{\pi} \frac{e^2 g_X^2 Z^2 \epsilon^2}{A^2 m_{Z'}^4}$$

BelleII excess: 2- or 3-body decay

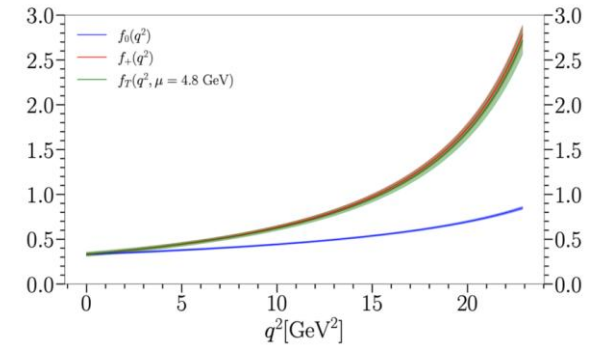
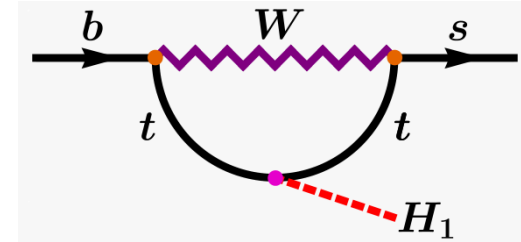
- When $m_{H_1} < m_B - m_K$, H_1 is on-shell

$$\Gamma_{B^+ \rightarrow K^+ H_1} \simeq \frac{|\kappa_{cb}|^2 \sin^2 \theta \left(\frac{m_{B^+}^2 - m_{K^+}^2}{m_b - m_s} \right)^2 \underbrace{[f_0(m_{H_1}^2)]^2}_{\text{form factor}}}{64\pi m_{B^+}^3} \sin \theta \ll 1$$

$$\times \sqrt{\mathcal{K}(m_{B^+}^2, m_{K^+}^2, m_{H_1}^2)}$$

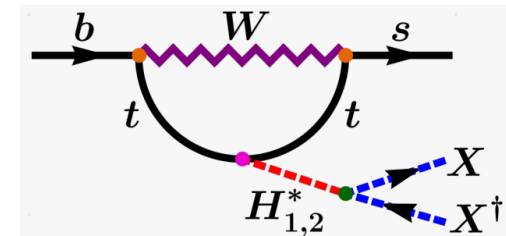
$$|\kappa_{cb}| \simeq 6.7 \times 10^{-6} \quad \mathcal{K}(a, b, c) = a^2 + b^2 + c^2 - 2(ab + bc + ca)$$

W. G. Parrott, C. Bouchard & C. T. H. Davies, ORD 2023



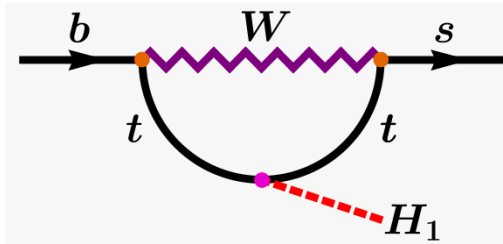
- When $m_{H_1} > m_B - m_K$, H_1 is off-shell \rightarrow three-body decay

$$\Gamma_{B^+ \rightarrow K^+ X X^\dagger} \simeq \frac{\lambda_{\Phi X}^2 v_\Phi^2 |\kappa_{cb}|^2 \sin^2 \theta \left(\frac{m_{B^+}^2 - m_{K^+}^2}{m_b - m_s} \right)^2 (m_{H_1}^2 - m_{H_2}^2)^2}{1024\pi^3 m_{B^+}^3} \times \int_{4m_X^2}^{(m_{B^+} - m_{K^+})^2} dq^2 \frac{\sqrt{1 - 4m_X^2/q^2} \sqrt{\mathcal{K}(m_{B^+}^2, m_{K^+}^2, q^2)} [f_0(q^2)]^2}{(q^2 - m_{H_1}^2)^2 (q^2 - m_{H_2}^2)^2}$$



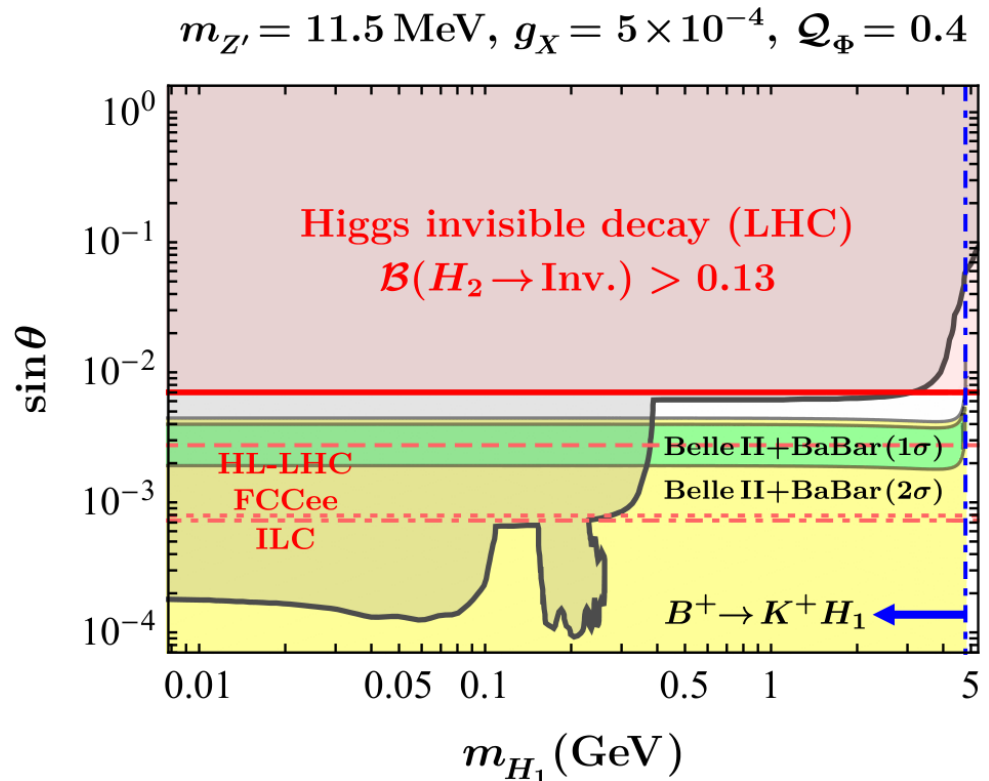
BelleII excess: 2-body decay

- When $m_{H_1} < m_B - m_K$, H_1 is on-shell
- The gray shaded area is excluded by BelleII $B^0 \rightarrow K^{*0} \nu \bar{\nu}$, KOTO $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ & NA62 $K^+ \rightarrow \pi^+ + \text{inv.}$



- H_1 decay process
 - $H_1 \rightarrow \mathbf{XX}^\dagger, \mathbf{Z}'\mathbf{Z}', ff^\dagger$

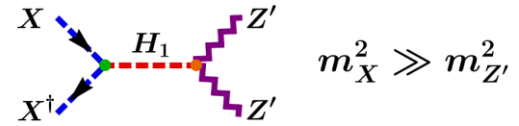
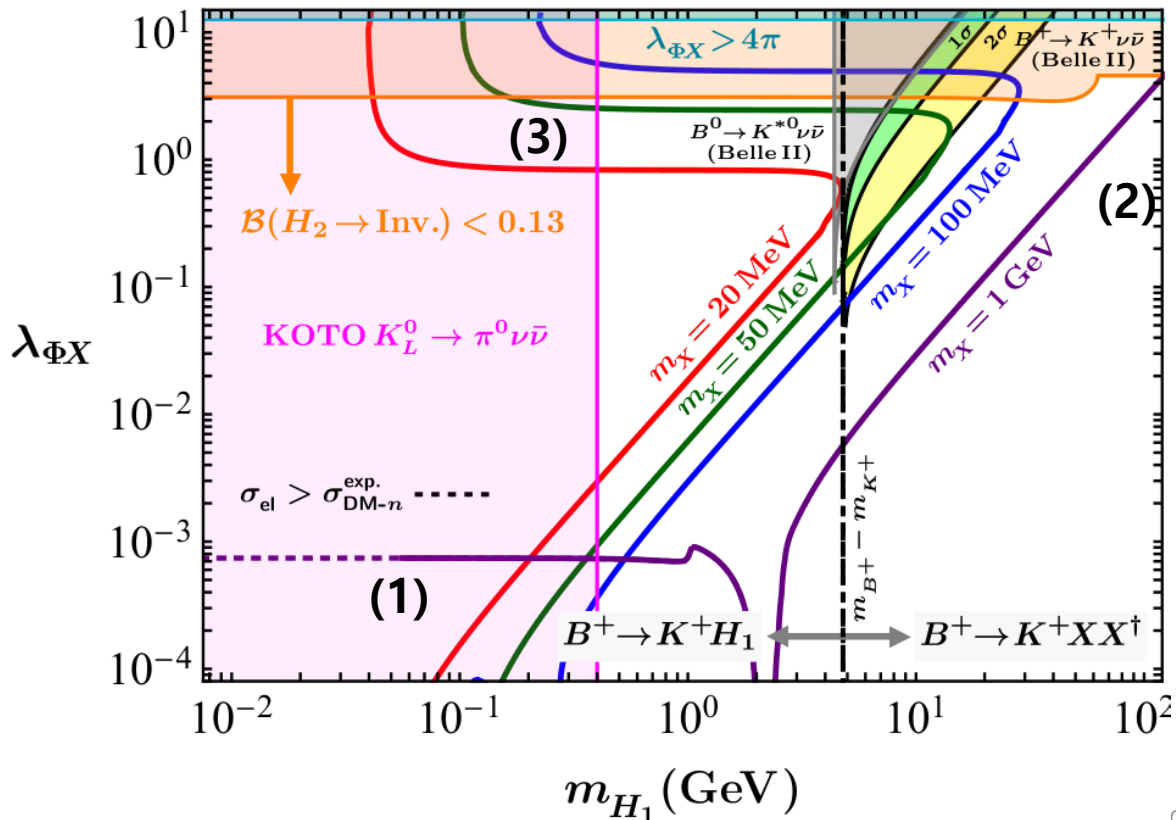
- Allowed value
 - $10^{-3} \leq \sin \theta \leq 5 \times 10^{-3}$
 - take $\sin \theta = 6 \times 10^{-3}$



BelleII excess : 2- or 3-body decay

- When $m_{H_1} > (<) m_B - m_K$, H_1 is off(on)-shell \rightarrow 3(2)-body decay
 - Two-body decay: $m_X \lesssim 1.2 \text{ GeV}$ ($m_{H_1} < m_B - m_K$)
 - Three-body decay: $20 \text{ MeV} < m_X \lesssim 60 \text{ MeV}$ ($m_{H_1} > m_B - m_K$)

$$m_{Z'} = 11.5 \text{ MeV}, g_X = 5 \times 10^{-4}, Q_\Phi = 0.4, s_\theta = 6 \times 10^{-3}$$



$$\langle \sigma v \rangle \propto \frac{\lambda_{\Phi X}^2 m_X^2}{(m_{H_1}^2 - 4m_X^2)^2 + \Gamma_{H_1}^2 m_{H_1}^2}$$

$$\Gamma_{H_1}^2 m_{H_1}^2 \propto \lambda_{\Phi X}^4 v_\Phi^4 \sqrt{1 - 4m_X^2/m_{H_1}^2}$$

(1) $\lambda_{\Phi X} \ll 1$ & $m_X^2 \gg m_{H_1}^2$

$$\Rightarrow \langle \sigma v \rangle \propto \frac{\lambda_{\Phi X}^2}{m_X^2} \Rightarrow \lambda_{\Phi X} \simeq \text{const.}$$

(2) $\lambda_{\Phi X} \ll 1$ & $m_{H_1}^2 \gg m_X^2$

$$\Rightarrow \langle \sigma v \rangle \propto \frac{\lambda_{\Phi X}^2 m_X^2}{m_{H_1}^4} \Rightarrow \lambda_{\Phi X} \propto m_{H_1}^2$$

(3) $\lambda_{\Phi X} \gg 1$ & $m_{H_1}^2 \gg m_X^2$

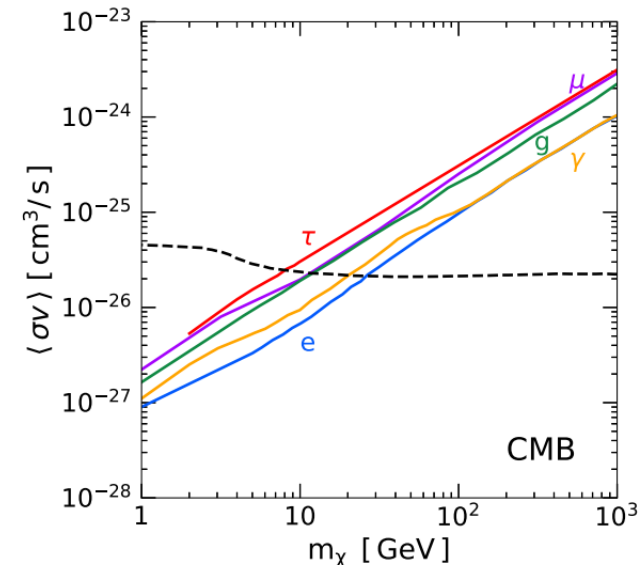
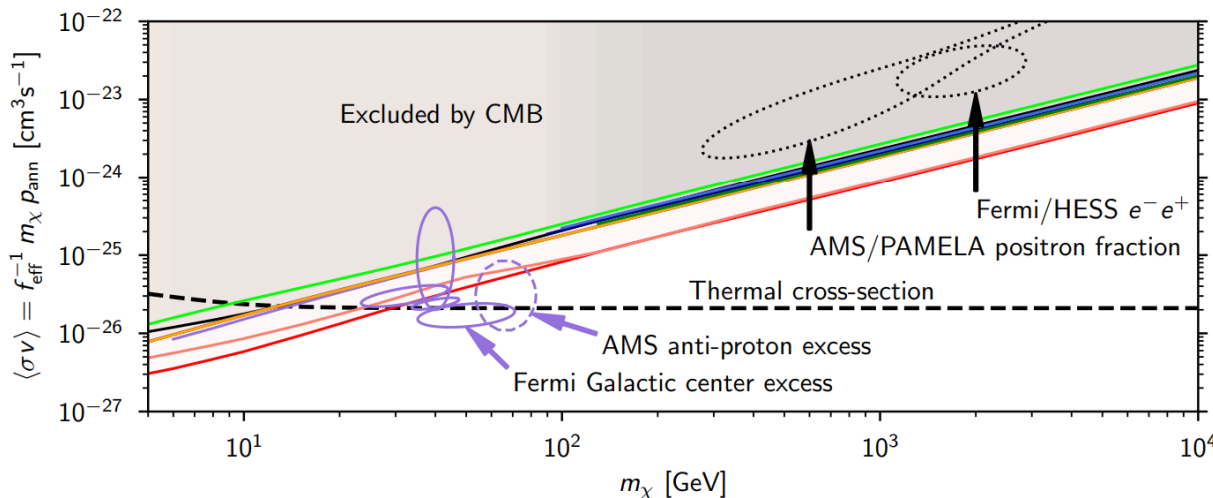
$$\Rightarrow \langle \sigma v \rangle \propto \frac{m_X^2}{\lambda_{\Phi X}^2 v_\Phi^4} \Rightarrow \lambda_{\Phi X} \simeq \text{const.}$$

CMB constraints

- Any injection of ionizing particles modifies the ionization history of hydrogen and helium gas, perturbing CMB anisotropies
 - DM annihilations to the charged SM particles
- Measurements of these anisotropies provide robust constraints on production of ionizing particles from DM annihilation products.

$$\langle \sigma v \rangle \leq \frac{4.1 \times 10^{-28} \text{ cm}^3 \text{ sec}^{-1}}{f_{\text{eff}}} \left(\frac{m_{\text{DM}}}{\text{GeV}} \right)$$

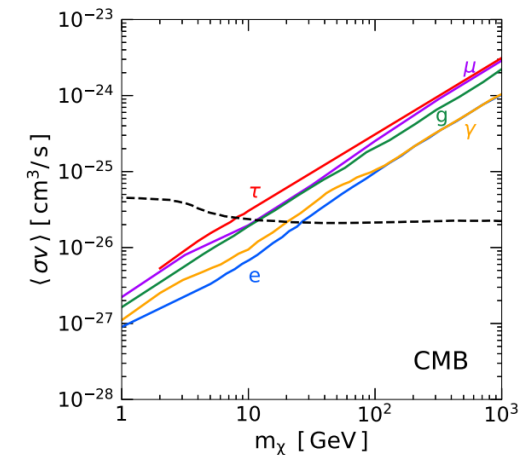
Planck 2018,
R. K. Leane et al, PRD 2018



CMB constraints

- For $m_X \lesssim 20\text{GeV}$, CMB bound (DM annihilation @ $T \sim eV$) excludes the thermal DM freeze-out determined by s-wave annihilation
 - DM annihilation should be mainly in **p-wave**
 - ...
- Dominant DM annihilation channel
 - $XX^\dagger \rightarrow Z'Z', H_1H_1$: **s-wave** annihilation
 - $XX^\dagger \rightarrow Z'H_1$: **p-wave** annihilation
- Z' decay
- H_1 decay

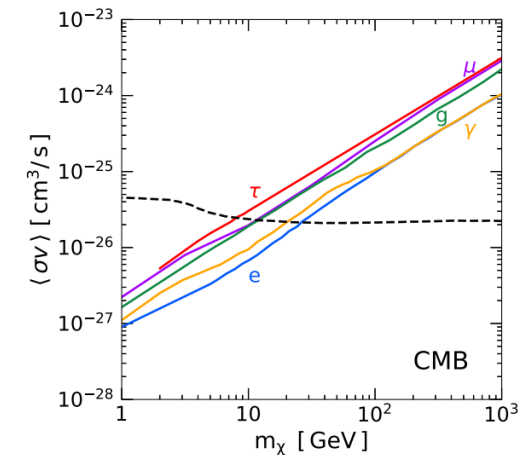
$$\sigma v = \underset{\substack{\uparrow \\ \text{s-wave}}}{a} + \underset{\substack{\downarrow \\ \text{p-wave}}}{b}v^2 + O(v^4)$$



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- Z' decay
 - A pair of ν
- H_1 decay
 - A pair of DM (open when $m_{H_1} > 2m_X$)
 - A pair of Z' ($Z' \rightarrow \nu\nu$)
 - SM particles (suppressed due to small Yukawa coupling & $\sin \theta$)

$$\sigma v = \underset{\substack{\uparrow \\ \text{s-wave}}}{a} + \underset{\substack{\downarrow \\ \text{p-wave}}}{b}v^2 + O(v^4)$$



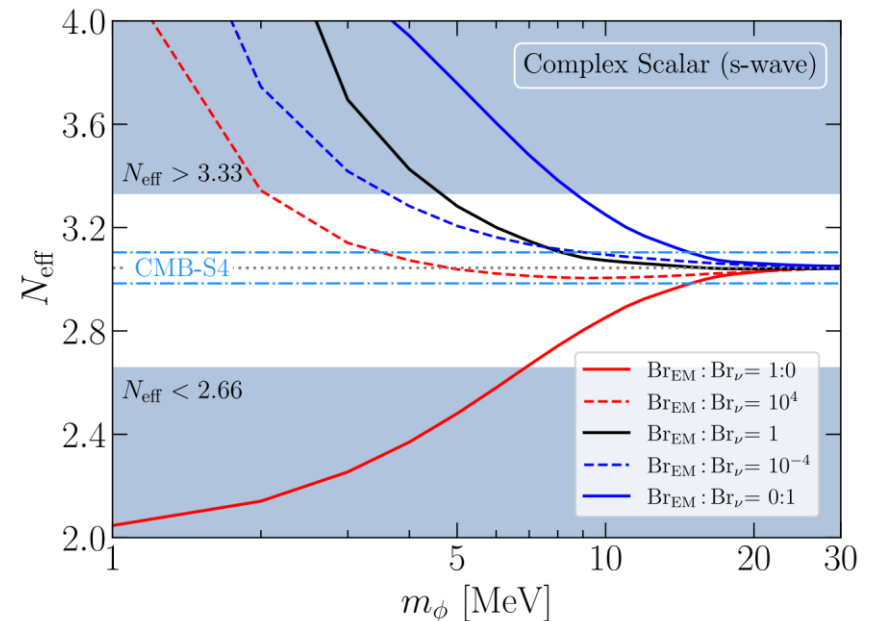
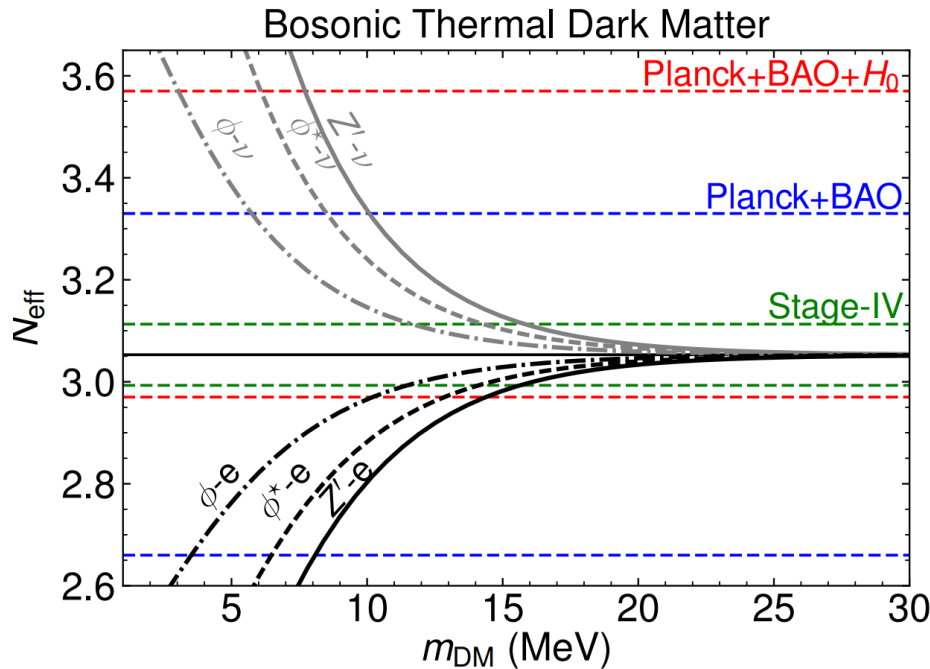
CMB constraints

- DM dominantly annihilates to neutrinos
- WIMPs of $m \leq 20$ MeV will generically alter neutrino decoupling and hence impact ΔN_{eff}

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M. Escudero, 1812.05605
X. Chu et al, 2310.06611



Conclusions

- BelleII data shows an excess of $B^+ \rightarrow K^+ \nu \bar{\nu}$ over the SM prediction
- This excess can be interpreted as $B^+ \rightarrow K^+ +$ dark sector particles
- CMB constraints can be evaded because DM pair annihilations into $H_1 H_1, H_1 Z', Z' Z'$, all of which are invisible
- We can accommodate the muon $g-2$ and subsequently relax the tension in the Hubble constant with extra radiation

Conclusions

- BelleII data shows an excess of $B^+ \rightarrow K^+ \nu \bar{\nu}$ over the SM prediction

- The pa

- CM int

- We can accommodate the muon $g-2$ and subsequently relax the tension in the Hubble constant with extra radiation

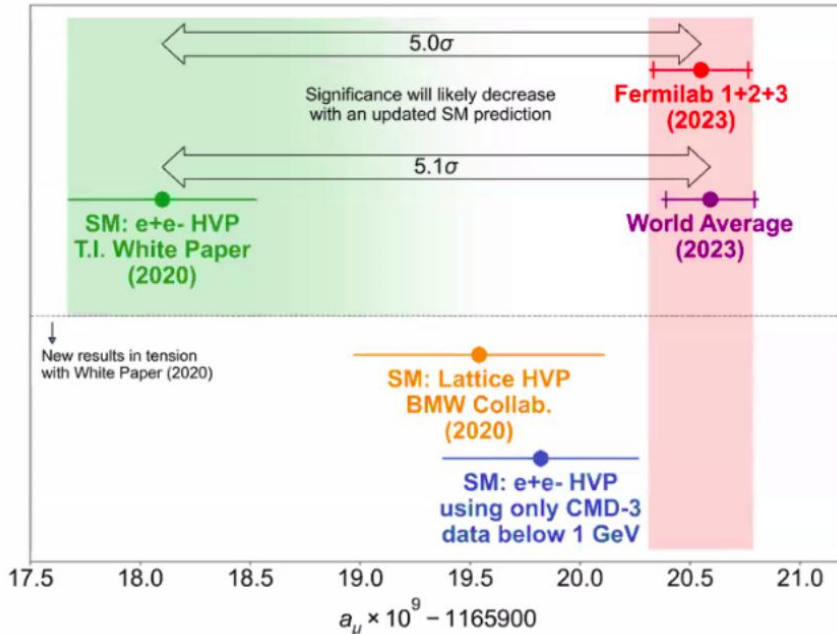
Thank you
very much

tions

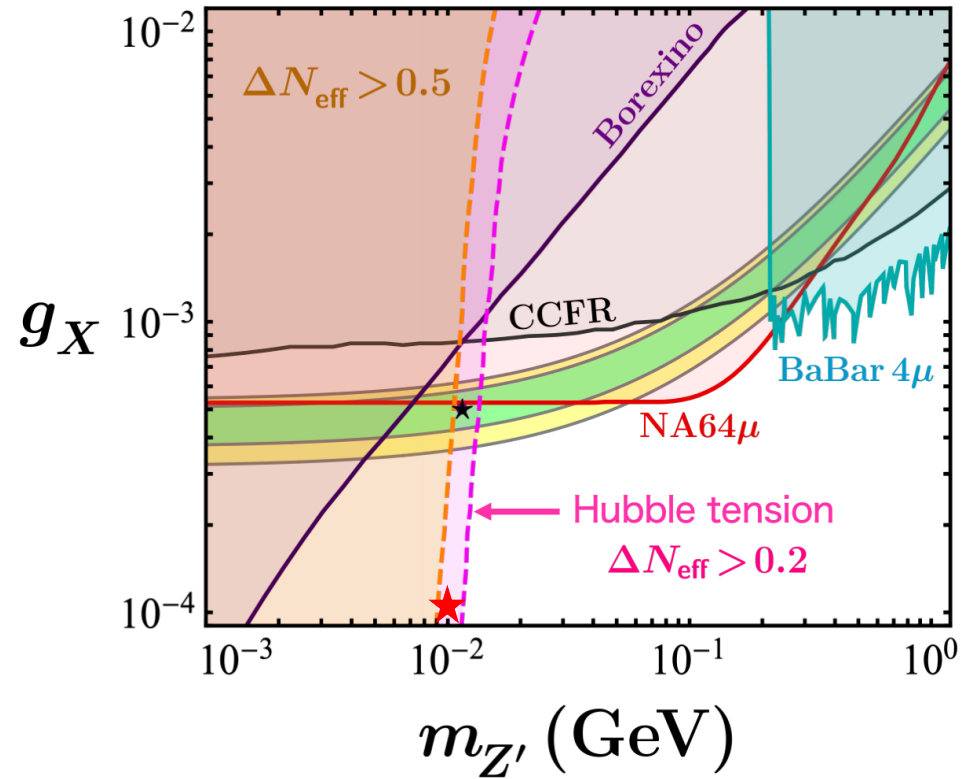
Back-up Slides

Evidences – Muon $g-2$

- **Muon $g-2$ experimental data from CMD-3 & BMW**
 - consistent with the combined experimental data from BNL and Fermilab muon $g-2$.



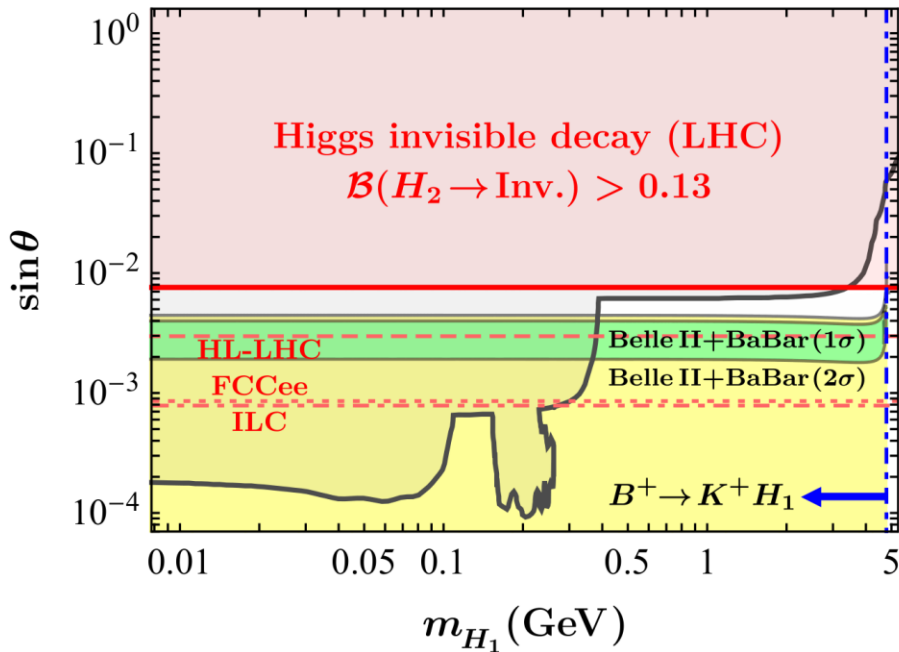
• New BP : $m_{Z'}$ = 10MeV, $g_X = 10^{-4}$



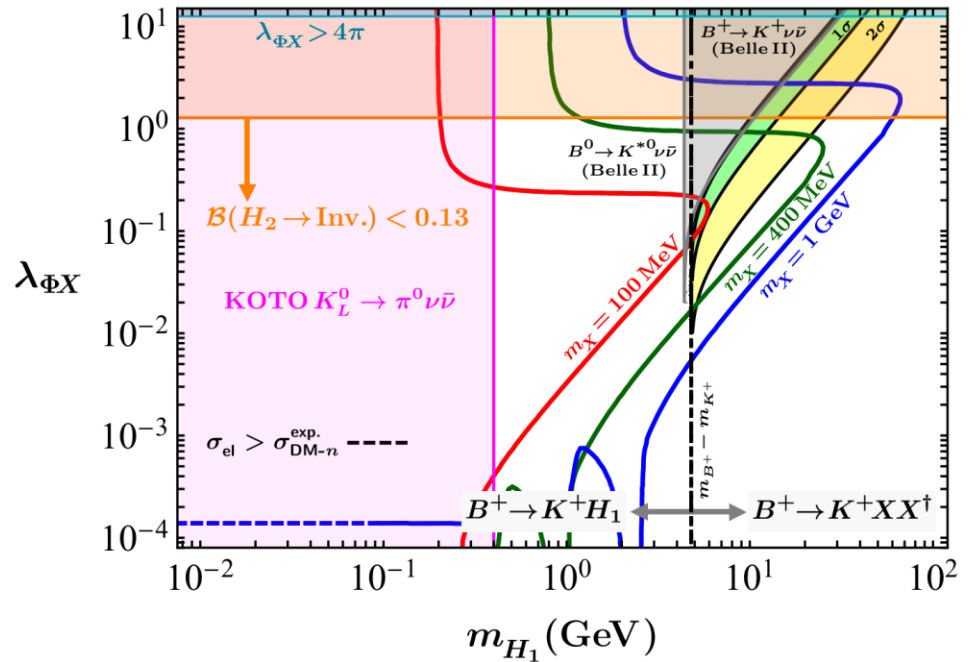
BelleII excess : 2- or 3-body decay

- $m_{Z'} = 10\text{MeV}$, $g_X = 10^{-4}$ ($m_{Z'} = g_X |Q_\Phi| v_\Phi \rightarrow$ Larger v_Φ)
 - Hubble tension can be relaxed
 - $\Delta a_\mu = 10^{-10}$ (BMW & CMD-3 collaboration)
 - Belle II (2-body decay): $m_X \lesssim 1.2\text{ GeV}$ ($m_{H_1} < m_B - m_K$)
 - Belle II (3-body decay): $\sim 90\text{MeV} < m_X \lesssim 450\text{MeV}$ ($m_{H_1} > m_B - m_K$)

$m_{Z'} = 10\text{ MeV}$, $g_X = 1 \times 10^{-4}$, $Q_\Phi = 0.4$

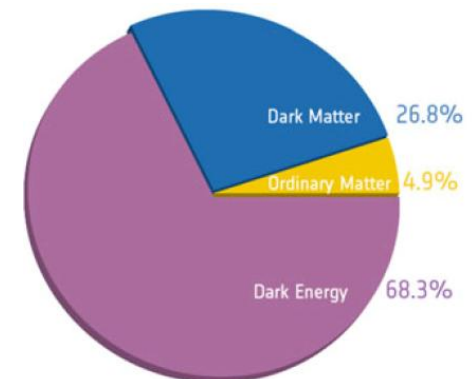


$m_{Z'} = 10\text{ MeV}$, $g_X = 1 \times 10^{-4}$, $Q_\Phi = 0.4$, $s_\theta = 6 \times 10^{-3}$



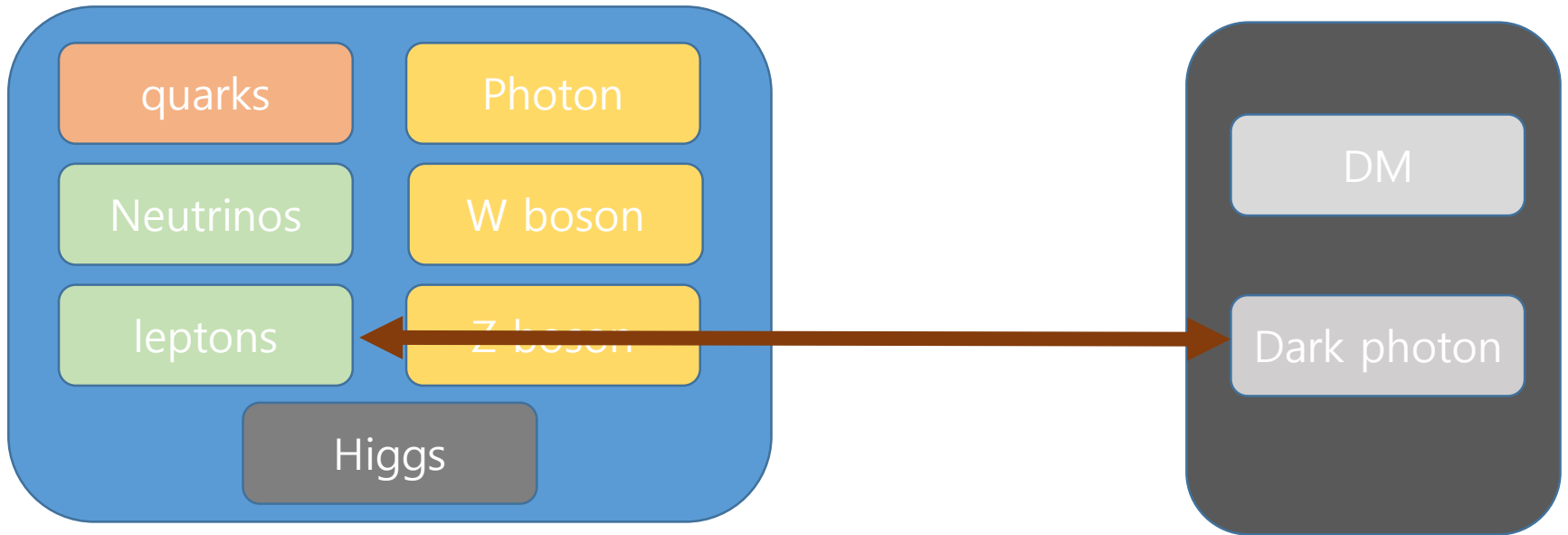
Evidences – Dark Matter

- **Dark Matter as a particle must be**
 - Non-baryonic
 - Massive
 - Have existed from early Universe up to now
 - **Stable** or lifetime longer than the age of Universe → new symmetry
 - **Dark** : No electromagnetic interaction → EM charge singlet
 - **27%** of the present energy density of the Universe → $\Omega h^2 = 0.12$
Planck 2018
 - **Cold** : non-relativistic at the time of formation of the first structures
- **Cold Dark Matter**
 - **Weakly Interacting Massive Particle**



$U(1)_{L_\mu-L_\tau}$ -charged DM model

- $U(1)_{dark} \equiv U(1)_{L_\mu-L_\tau}$



- Let's call Z' , $U(1)_{L_\mu-L_\tau}$ gauge boson, dark photon since it couple to DM

$U(1)_{L_\mu - L_\tau}$ -charged DM model

- $U(1)_{L_\mu - L_\tau}$ -charged scalar DM model

$$\mathcal{L}_{\text{int}} = ig_X Z'_\mu (X^* \partial^\mu X - X \partial^\mu X^*) + g_X Z'_\alpha \sum Q_{\ell} \bar{\ell} \gamma^\alpha \ell$$

- Free parameters: $\{m_{Z'}, g_X, m_X, Q_X\}$
- Dark Photon Z' plays a role of messenger particle between DM and the SM leptons
- Dark Photon mass is generated Proca or Stueckelberg mechanism



Only when $m_X > m_{Z'}$

- Consider Z' boson only & $g_X \sim (3 - 5) \times 10^{-4}$ for the muon $g-2$
 - $X\bar{X} \rightarrow f_{SM}\bar{f}_{SM}$: dominant annihilation channels

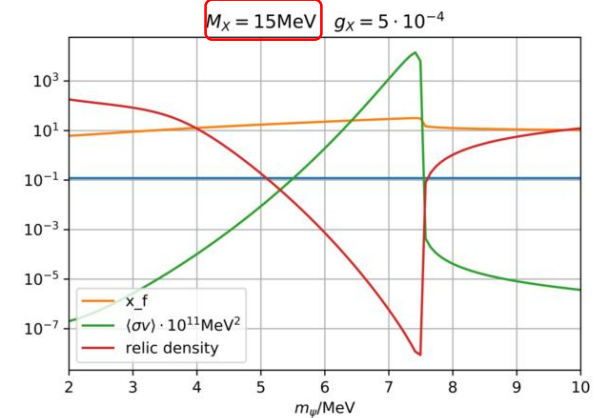
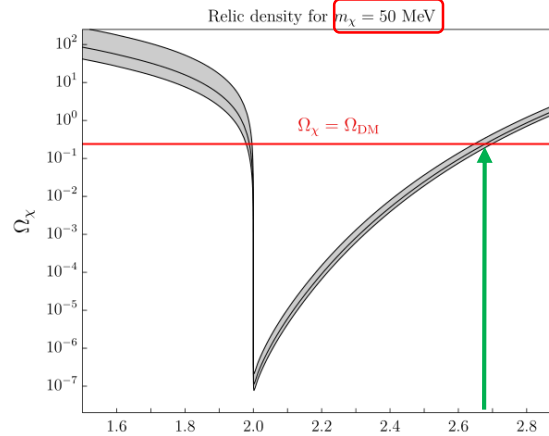
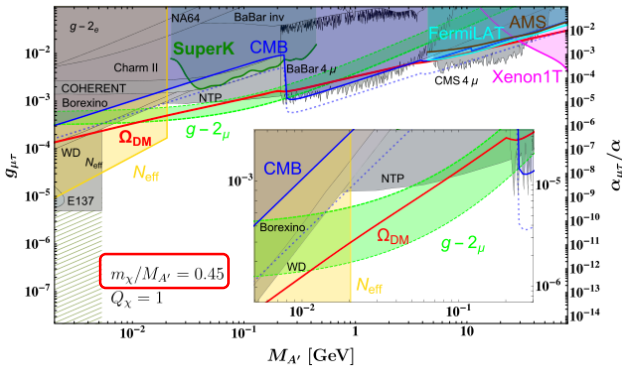
$U(1)_{L_\mu - L_\tau}$ -charged DM model

- $XX^\dagger \rightarrow Z'^* \rightarrow \nu\bar{\nu}$: dominant annihilation channels
 - $m_{Z'} \sim 2m_\chi$ with the **s-channel Z' resonance** only gives the correct relic density

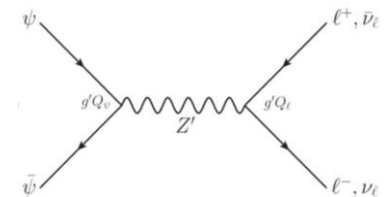
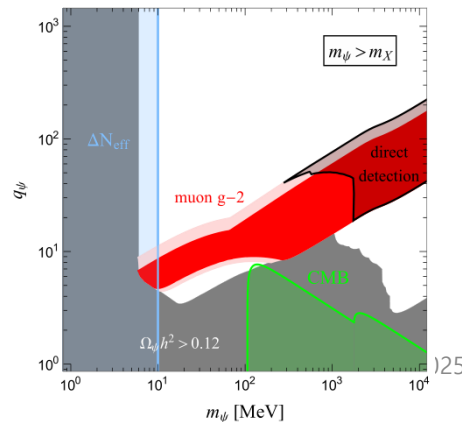
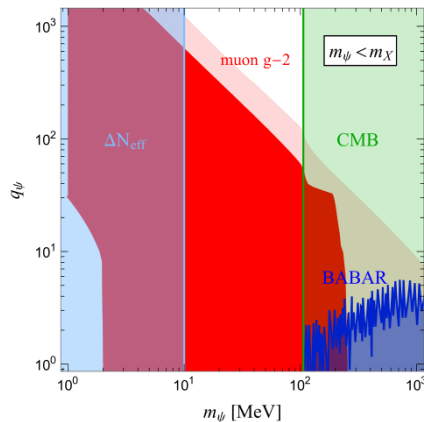
P. Foldenauer, PRD 2019

I. Holst, D. Hooper, G. Krnjaic, PRL 2022

M. Drees, W. Zhao, PLB 2022



- Large DM charges Asai, Okawa, Tsumura, JHEP 2021



$U(1)_{L_\mu - L_\tau}$ -charged DM model

- **Muon g-2**

- $m_{Z'} \sim O(10)\text{MeV}$, & $g_X \sim 10^{-4}$ is **too small** to get $\Omega h^2 = 0.12$
- $m_{Z'} \sim 2m_X$ with the **s-channel Z' resonance**
- Only sub-GeV **DM** available
- Tight correlation between DM mass and Z' mass

- **No DM direct detection bound**

- DM-nucleon scattering: $\sigma_{\text{el}}^{X-p} \simeq 10^{-46} \text{cm}^2$
- DM-electron scattering: $\sigma_{\text{el}}^{X-e} \simeq 10^{-45} \text{cm}^2$

$U(1)_{L_\mu - L_\tau}$ -charged DM model

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- **BelleII excess**

- $B \rightarrow KZ'$ (2-body decay)
→ disfavored by q^2 spectrum
- $B \rightarrow KXX^\dagger$ (3-body decay)
→ suppressed by kinetic mixing and $g_X \sim 10^{-4}$

Gauged $U(1)_{L_\mu - L_\tau}$ Z' model

- **Neutrino trident production**

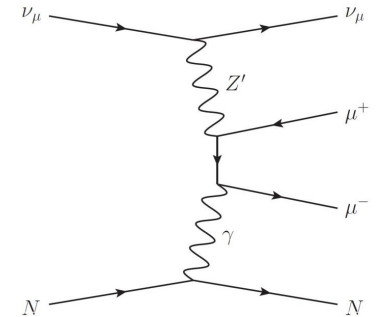
W. Altmannshofer et al, PRL 2014

- Production of a muon pair from the scattering of a muon neutrino with heavy nuclei

- $R_{\text{CCFR}} \equiv \frac{\sigma_{\text{CCFR}}}{\sigma_{\text{SM}}} = 0.82 \pm 0.28.$

- **NA64** Y. Andreev, 2401.01708

- $\mu^- N \rightarrow \mu^- N Z', (Z' \rightarrow \text{inv.})$
- Upper limit on g_X for $1\text{MeV} \leq m_{Z'} \leq 1\text{GeV}$



- **ΔN_{eff}**

M. Escudero et al, JHEP 2019

- Z' will reheat the neutrino gas, resulting in a higher expansion rate
- Increase the effective number of neutrinos N_{eff}
- $\Delta N_{\text{eff}} < 0.5$

- **BOREXINO**

R. Harnik et al, JCAP 2012

- $\nu - e$ scattering

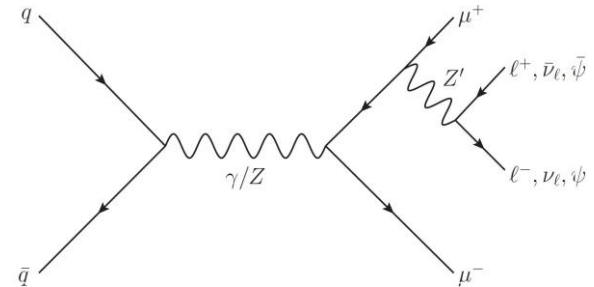
BaBar, LHC 4μ channels

- $e^+e^- \rightarrow \mu^+\mu^-Z', Z' \rightarrow \mu^+\mu^-$
 - Upper limit on g_X for $200\text{MeV} \leq M_{Z'} \leq 10\text{GeV}$

BaBar Collaboration, PRD 2016

CMS Collaboration, PLB 2019

- The lowest order Z' production process at collider
 - Produce a charged lepton pair through Drell-Yan process
 - Z' is radiated from one of leptons



- Final states
 - two pair of charged-leptons
 - A pair of charged-lepton plus missing energy

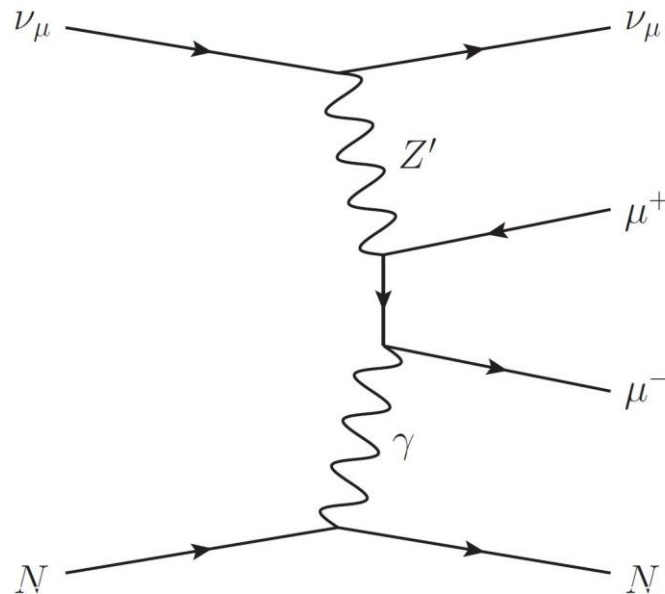
Neutrino trident production

- Production of a muon pair from the scattering of a muon neutrino with heavy nuclei

- $R_{\text{CCFR}} \equiv \frac{\sigma_{\text{CCFR}}}{\sigma_{\text{SM}}} = 0.82 \pm 0.28.$

W. Altmannshofer et al, PRL 2014

- The leading order Z' contribution:



Borexino: $\nu - e$ scattering

- Borexino is a liquid scintillator experiment measuring solar neutrino scattering off electron
 - Probe non-standard interactions between neutrinos and target
 - Limits from Borexino for the $U(1)_{B-L}$ gauge boson have been derived.

R. Harnik et al, JCAP 2012

- Rescale the constraints on $U(1)_{B-L}$ boson as

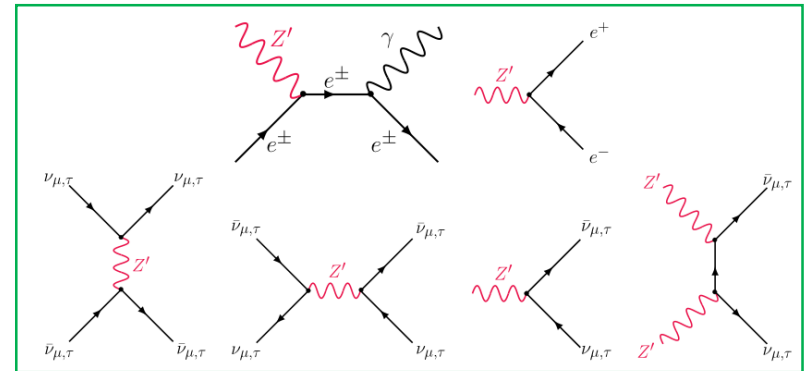
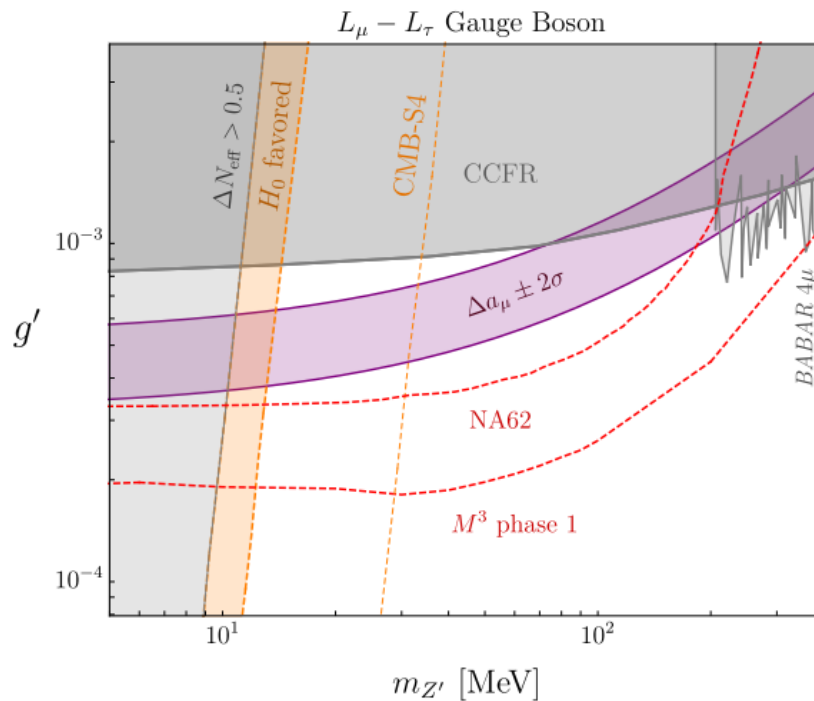
$$\alpha_{B-L}^2 \rightarrow \begin{cases} \left[\sum_{i,j=1}^3 f_i |(U^\dagger Q_{\mu e} U)_{ij}|^2 \right]^{1/2} \alpha_{\mu e}^2, & \text{for } U(1)_{L_\mu - L_e}, \\ \left[\sum_{i,j=1}^3 f_i |(U^\dagger Q_{e\tau} U)_{ij}|^2 \right]^{1/2} \alpha_{e\tau}^2, & \text{for } U(1)_{L_e - L_\tau}, \\ \left[\sum_{i,j=1}^3 f_i |(U^\dagger Q_{\mu\tau} U)_{ij}|^2 \right]^{1/2} \alpha \alpha_{\mu\tau} \epsilon_{\mu\tau}(q^2), & \text{for } U(1)_{L_\mu - L_\tau}, \end{cases}$$

$$Q_{\mu\tau} = \text{diag}(0, 1, -1)$$

CMB & Hubble tension

M. Escudero et al, JHEP 2019

- Z' will reheat the neutrino gas
 - Resulting in a higher expansion rate
 - Increase the effective number of neutrinos N_{eff}
- Taking into account kinetic mixing



$U(1)_{L_\mu - L_\tau}$ -charged DM model

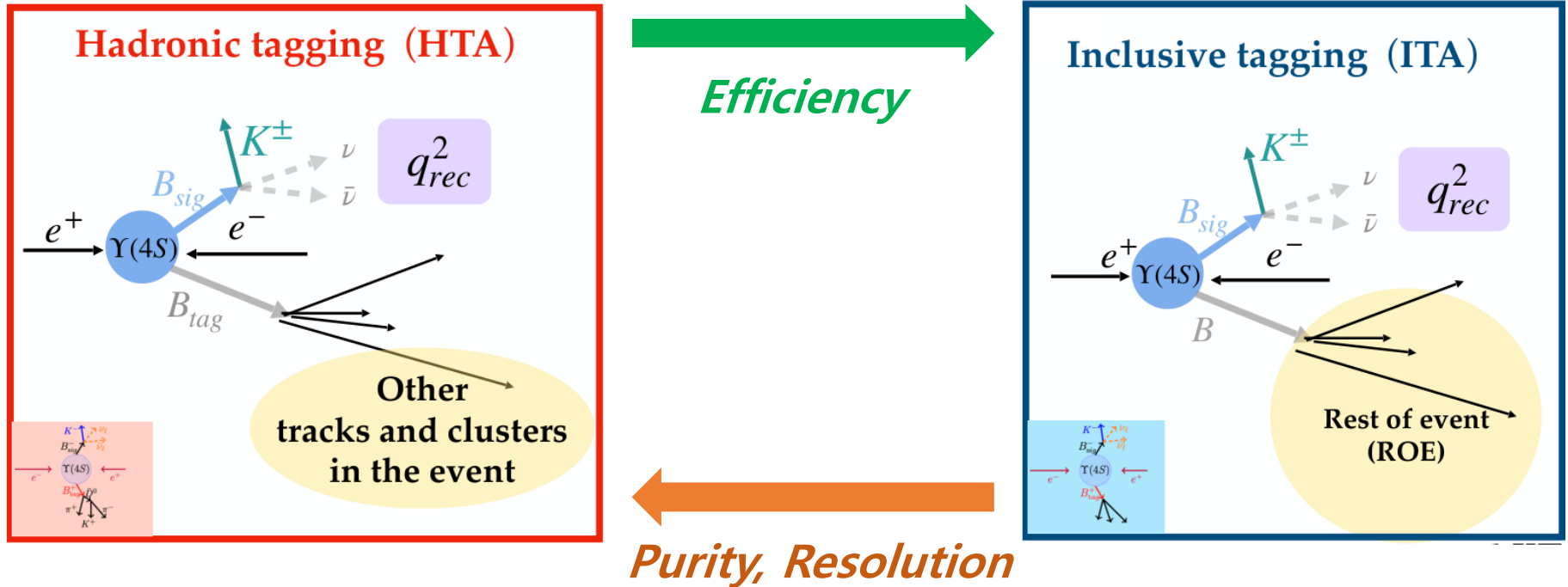
- Conventional $U(1)_{L_\mu - L_\tau}$ -charged fermion DM model

$$\mathcal{L} \supset \mathcal{L}_{\text{SM}} - \frac{1}{4} Z'_{\alpha\beta} Z'^{\alpha\beta} + \frac{1}{2} m_{Z'}^2 Z'_\alpha Z'^\alpha + i \bar{\chi} \gamma^\alpha \partial_\alpha \chi - m_\chi \bar{\chi} \chi + g_X Q_\chi Z'_\alpha \bar{\chi} \gamma^\alpha \chi + g_X Z'_\alpha \sum Q_{\ell} \bar{\ell} \gamma^\alpha \ell$$

- Dark Photon Z' plays a role of messenger particle between DM and the SM leptons
- Dark Photon mass is generated by hand or Stueckelberg mechanism
- New parameters: $\{g_X, m_{Z'}, m_\chi, Q_\chi\}$
- Consider Z' boson only & $g_X \sim (3 - 5) \times 10^{-4}$ for the muon $g-2$
 - $\chi \bar{\chi} (X \bar{X}) \rightarrow f_{\text{SM}} \bar{f}_{\text{SM}}$: dominant annihilation channels
 - $g_X \sim 10^{-4}$ is too small to get $\Omega_\chi h^2 = 0.12$

Measurement of $B^+ \rightarrow K^+ \nu \bar{\nu}$

- Two ways of tagging



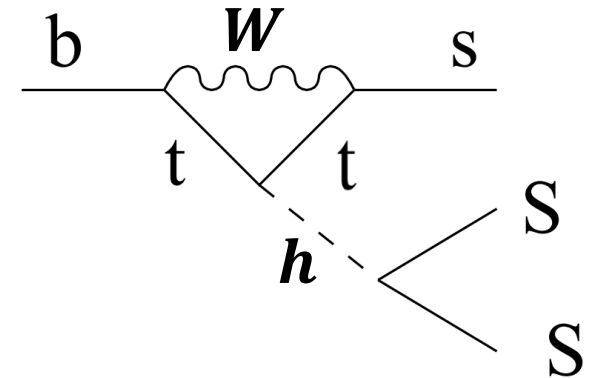
- q_{rec}^2 : mass squared of the neutrino pair
- Inclusive tagging: It allows one to reconstruct inclusively the decay $B^+ \rightarrow K^+ \nu \bar{\nu}$ from the charged kaon

Solutions: 3-body decay

- Singlet scalar DM model ($m_s \leq 2.3\text{GeV}$)

Bird et al, PRL 2004

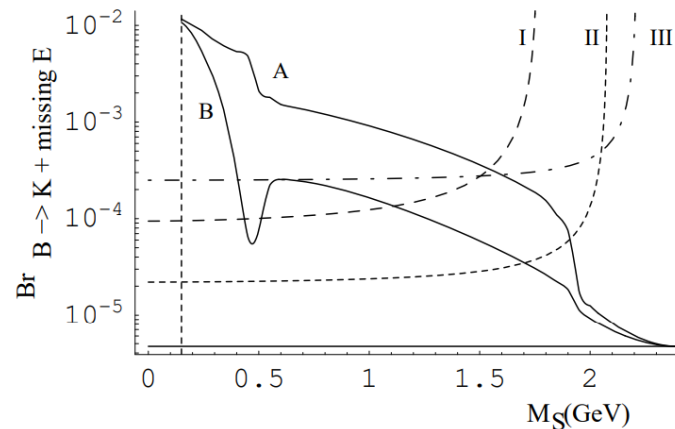
$$\begin{aligned}
 -\mathcal{L}_S &= \frac{\lambda_S}{4} S^4 + \frac{m_0^2}{2} S^2 + \lambda S^2 H^\dagger H \\
 &= \frac{\lambda_S}{4} S^4 + \frac{1}{2} (m_0^2 + \lambda v_{EW}^2) S^2 + \boxed{\lambda v_{EW} S^2 h} + \frac{\lambda}{2} S^2 h^2,
 \end{aligned}$$



- Belle $\rightarrow \frac{C_{DM}}{C_\nu} \simeq \frac{4.4\lambda M_W^2}{g_W^2 m_h^2}$

- Relic density: $\sigma_{\text{ann}} v_{\text{rel}} = \frac{8v_{EW}^2 \lambda^2}{m_h^4} \left(\lim_{m_{\tilde{h}} \rightarrow 2m_s} m_{\tilde{h}}^{-1} \Gamma_{\tilde{h}X} \right)$.

- λ should be large to fit the relic as well as Belle II
- $m_s \leq 1\text{GeV}$ is already excluded by BABAR limits (2004 data).



Solutions: 3-body decay

Bird et al, PRL 2004

- Singlet scalar DM model ($m_s \leq 2.3\text{GeV}$)

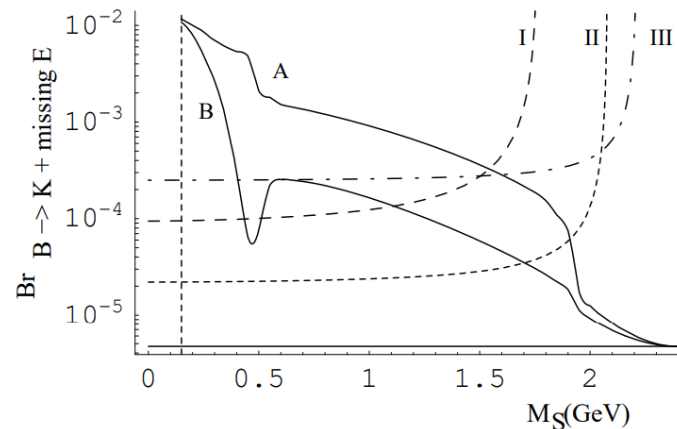
$$V = \lambda_S \phi^4 + \frac{m_0^2}{2} \phi^2 + \lambda \phi^2 H^\dagger H$$

b W S

S S

- For $m_\chi \lesssim 10\text{GeV}$, CMB bound (DM annihilation @ $T \sim \text{eV}$) excludes the thermal DM freeze-out determined by s-wave annihilation
- At that time, the authors did not consider the CMB bounds.
This model does not work anymore.

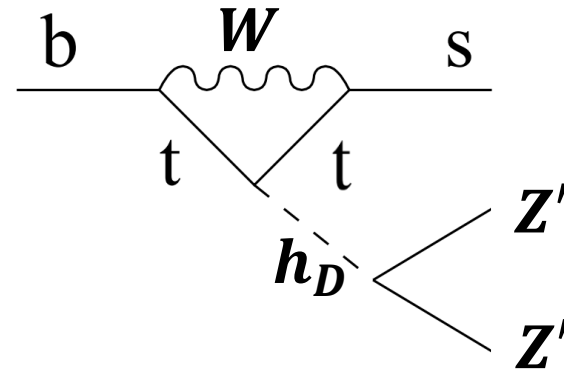
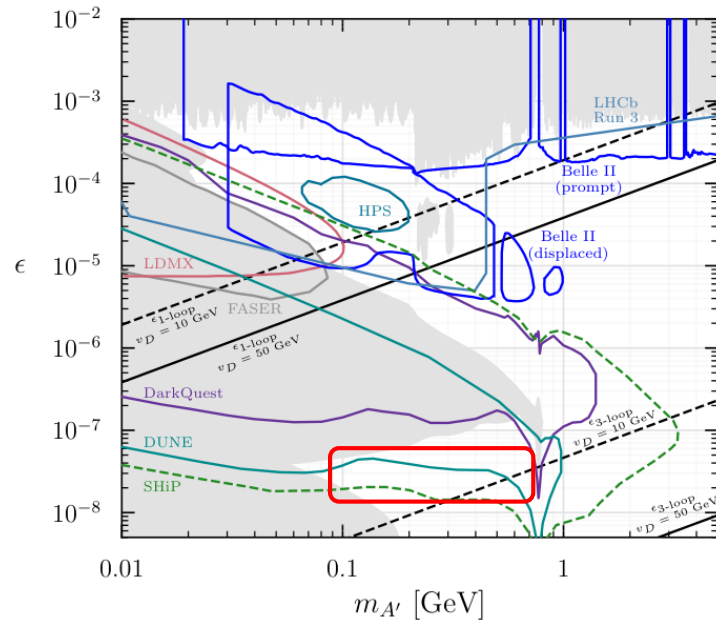
- λ should be large to fit the relic as well as Belle II
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Solutions: 3-body decay

McKeen et al, 2312.00982

- Dark Higgs decays to dark Photon
 - Dark Photon can be long-lived \rightarrow appear missing energy at BelleII
 - $\mathcal{L} \supset g_D^2 v_D A'_\mu A'^\mu (-h \sin \theta + h_D \cos \theta)$
- Two-regions for sub-GeV dark photon that unconstrained by existing experimental searches:



1. $m_{A_D} \gtrsim 100 \text{ MeV}$ with $10^{-8} \lesssim \epsilon \lesssim 10^{-7}$
2. $m_{A_D} \gtrsim 50 \text{ MeV}$ with $10^{-6} \lesssim \epsilon \lesssim 10^{-4}$.