

# Search for Axion-Like Particle through

$B \rightarrow K^{(*)} a' (\rightarrow \gamma\gamma)$  Decay at Belle

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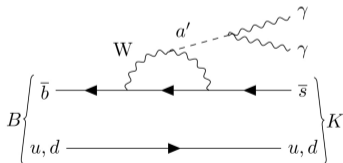
Feb 22nd, 2025

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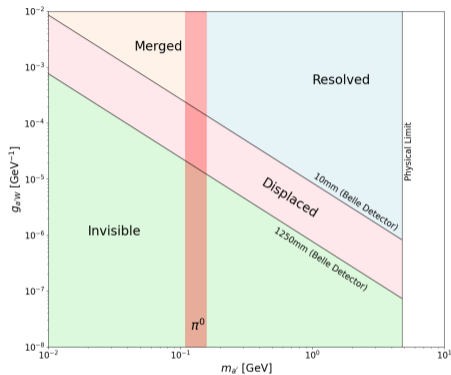
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# Introduction: $B \rightarrow K^{(*)} a' (a' \rightarrow \gamma\gamma)$

- Searching for **Axion-Like-Particles (ALPs or  $a'$ )**
- **ALP ( $a'$ ):**
  - ▶ Spin-0 pseudoscalar particle (pNGB)
  - ▶ **promptly decays into  $\gamma\gamma$  100%**
  - ▶ The lifetime is concerned as signal efficiency  
constraint:  $\Gamma_{a'} = g_{a'W}^2 M_{a'}^3 \sin^4 \theta_W / 64\pi$
- Without significant excess above background, we set the upper on **ALP – W coupling ( $g_{a'W}$ ) [1]**.



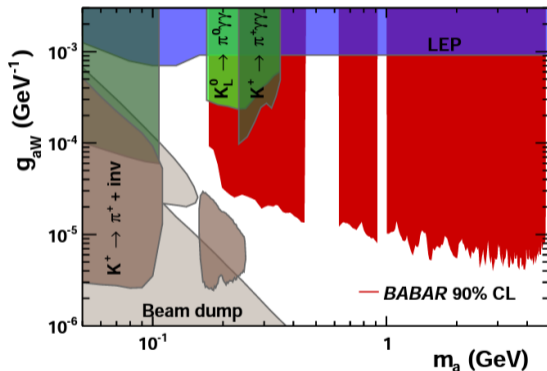
[Figure 1]



- **Mass Scanning** :  $0.160 \sim 4.50(4.20)\text{GeV}/c^2$
  - Mass region is decided by our detector limits and physical limits.
  - $\pi^0, \eta, \eta'$  mass region is excluded
- [1] [Phys. Rev. Lett. 118, 111802 \(2017\)](#)

# Introduction: Advantage over previous studies

- Previous result from *BaBar*,  
 $B^+ \rightarrow K^+ a' (a' \rightarrow \gamma\gamma)$  with  $424\text{fb}^{-1}$  [1].
- Belle I Full Dataset ( $711\text{fb}^{-1}$ )  
is used for analysis
- $B \rightarrow K^{(*)} a' (a' \rightarrow \gamma\gamma)$
- Four *K* modes :  $K_S^0$ ,  $K^+$ ,  $K^{*0}$ , and  $K^{*+}$
- Expand the exclusion region with more total integrated luminosity and combining multiple kaon modes.



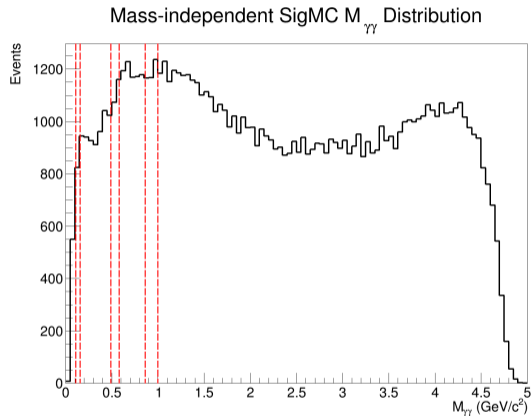
[1] Phys.Rev.Lett. 128, 131802 (2022)

# Data Sample: Signal MC

- Generated with EvtGen + gsim
- tested ALP mass hypothesis :  
 $0.160, [0.200..1.000..0.050], [1.0..4.7..0.1]$

Process	Gen. Cond.
Signal $B \rightarrow K a'$	PHOTOS PHSP
Signal $B \rightarrow K^* a'$	PHOTOS SVS
$a' \rightarrow \gamma\gamma$	PHSP
Other $B$	Free Decay
$K$	Free Decay

- Mass Independent Signal MC :  
used for FBBDT training and optimization.
- include  $M_{a'}$  generated uniformly from 10-4780 MeV with 10 MeV interval.

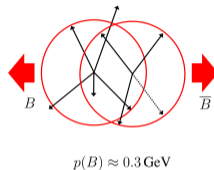
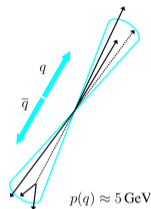


# Data Sample: Background MC

- Every event passes our signal selection criteria
- Any process appears in our signal region.
  - ▶  $B\bar{B}$  background
  - ▶  $q\bar{q}$  continuum background
  - ▶ Peaking Background
  - ▶ Combinatorial Background

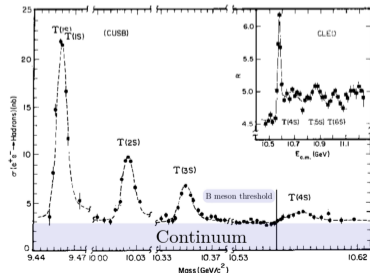
Tested Bkg Process	MC Streams
$B\bar{B}$	10
$e^+e^- \rightarrow q\bar{q}$ ( $q = u, d, s, c$ )	6
Rare $B\bar{B}$	50
$B \rightarrow X_u l \nu$	20

- A 'stream' refers to the data amount of  $711\text{fb}^{-1}$  data accumulated in  $\Upsilon(4S)$  resonance in the Belle experiment.
- A generic background stream 00 is used for FBBDT.



$$e^+e^- \rightarrow q\bar{q} \quad (q \in \{u, d, s, c\})$$

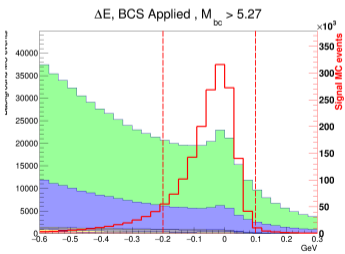
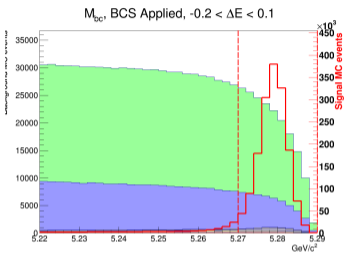
$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$



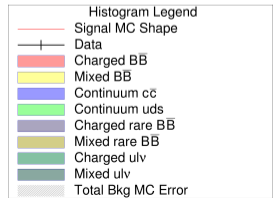
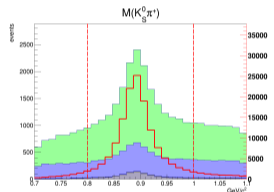
# Event Selection and Reconstruction

Particle List	Selection Criteria
Charged track	$ d0  < 3.0$ cm $ z0  < 4.0$ cm eIDBelle < 0.9 muIDBelle < 0.9 or muIDBelleQuality = 0
$K^+$	$\mathcal{L}(K\pi) > 0.6$ & $\mathcal{L}(Kp) > 0.4$
$\pi^+$	$\mathcal{L}(\pi K) > 0.4$ & $\mathcal{L}(\pi p) > 0.7$
$\gamma$	$E > 50$ MeV; barrel $E > 100$ MeV; forward endcap $E > 150$ MeV; backward endcap
$K_S^0$	ksnbStandard = 1 (nisKs) $p > 0.06$ GeV/c $ \Delta M  < 20$ MeV/c <sup>2</sup>
$K^*$	$0.8 < M(K\pi) < 1.0$ GeV $K^{*0} \rightarrow K^\pm \pi^\mp$ $K^{*+} \rightarrow K_S^0 \pi^+$
ALP	$\pi^0, \eta, \eta'$ mass region excluded
B	$M_{bc} > 5.27$ GeV $-0.2 < \Delta E < 0.1$ GeV Best Candidate Selection min( $\Delta E$ )

Kinematic fit to  $B \rightarrow K_S^0 \pi^0$  mass



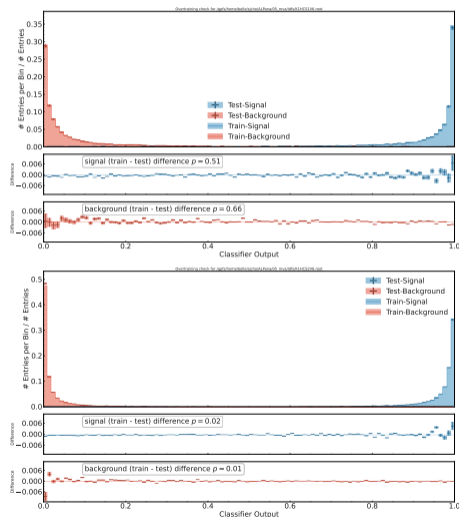
- $K_S^0$  reconstructed with charged pion modes.
- $\pi^0$  not used in  $K^*$  reconstruction.
- The dominant source of background is continuum.



# Continuum Suppression

- 2 Fast-BDT (FBDT) for Continuum Suppression
- Generate mass-independent Signal MC (0.01~4.78 GeV, 10 MeV interval).
- Background MC data from CHM/UDS (0th stream)
- CS2 FBDT trained with data pass CS1 loose cut (0.1)

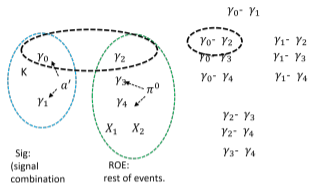
CS1 Variables	CS2 Additional Variables
thrustOm	aplanarity
cosTBz	sphericity
cosTBTO	cosHelicityAngle Beam momentum ( $\kappa$ )
R2	CleoCone Thrust
KSFW(6)	Hemisphere Momentum
	FoxWolfram moment and ratio
	cosHelicityAngle ( $\gamma$ )
	number on ALP candidates
	harmonic Moment Thrust
	$\Delta\theta(a')$
	<i>Easy</i>





# $\gamma\pi^0$ Suppression

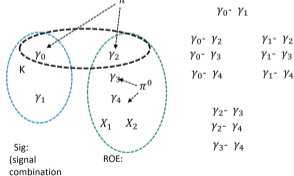
## Signal



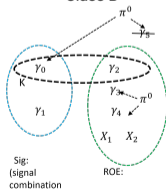
- $\gamma\pi^0$  suppression consist of 3 classes of subclassifiers :

Classifier	Training sample for "good" pair	Training sample for "bad" pair
class A	Photon pairs, $(\gamma^{SIG}, \gamma^{ROE})$ , in Sig MC	Photon pairs from a single $\pi^0$ in Bkg MC
class B	Photon pairs, $(\gamma^{SIG}, \gamma^{ROE})$ , in Sig MC	Photon pairs from a single $\pi^0$ in Bkg MC but the photon in ROE is not reconstructed.
class C	Photon pairs from different $\pi^0$ or other source of photons in Bkg MC.	Photon pairs form a single particle in Bkg MC

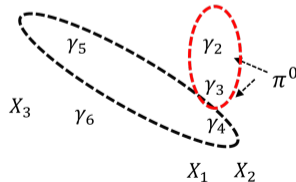
## Class A



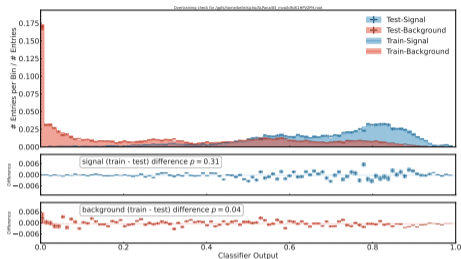
## Class B



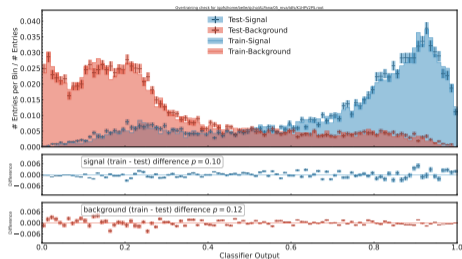
## Class C



# $\gamma \pi^0$ Suppression



Hard Photon  $\pi^0$  probability (High mass region)

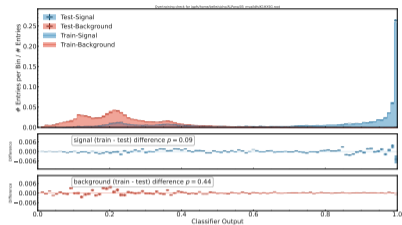


Soft Photon  $\pi^0$  probability (High mass region)

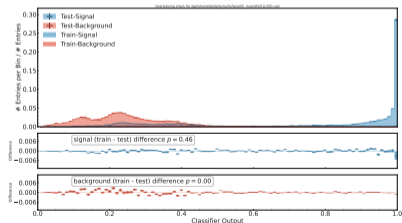
- Trained with FastBDT, mass-independent Signal MC and background MC (stream 00)
- Training for Hard photon ( $\gamma_0$ ) and Soft photon ( $\gamma_1$ ), ( $E_{\gamma_0} > E_{\gamma_1}$ ) is performed separately.
- Among the ( $\gamma^{SIG}, \gamma^{ROE}$ ) photon pairs, the pair with lowest subclassifier output value (most  $\pi^0$ -like) is selected for each subclassifiers.
- Phpton pair of ( $\gamma^{SIG}, \gamma^{ROE}$ ) is handled seperately when ( $E_{\gamma^{SIG}} > E_{\gamma^{ROE}}$ ) and ( $E_{\gamma^{SIG}} < E_{\gamma^{ROE}}$ ).
- subclassifier output is combined with FastBDT.
- Each subclassifiers and  $\pi^0$  veto classifiers are trained for signal hard photon and signal soft photon seperately in high/low ALP mass region.

Photon	Photon Pair
$E^*$	$E^*$
E9E25	$p_t$
ErrorPhi	deltaAngle
HighestE	$E_{asy}^*$
LAT	$M_{\gamma\gamma}$
NHits	

# $B \rightarrow X_S \gamma$ Veto



High  $M_{a'}$

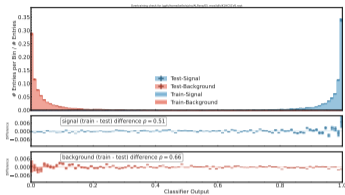


Low  $M_{a'}$

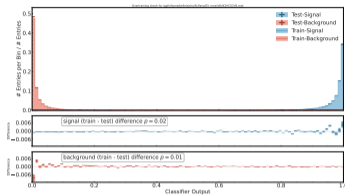
Photon	photon pair
$E^*$	$E^*$
E9E25	nALP
HighestE	$E_{asy}^*$
	deltaAngle
	cosHelicityAngle(a')
	cosHelicityAngleBeamMomentum(K)

- $B \rightarrow X_S \gamma$  decay can mimic  $B \rightarrow Ka'$  final state
- $X_S$  : Hadron system involving kaon
- Neutral (or excited state kaon) mesons, their final state particle contains at least one  $\gamma$  with high probability which can be reconstructed to fake ALP with  $\gamma$  from  $B$  directly.
- training dataset : [mass-indep  $B \rightarrow Ka'$  vs  $B \rightarrow X_S \gamma$ ]
- No Optimization (Not for global background suppression)

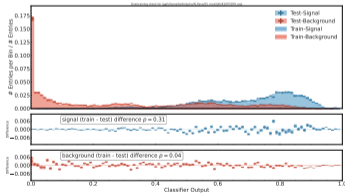
# Optimization



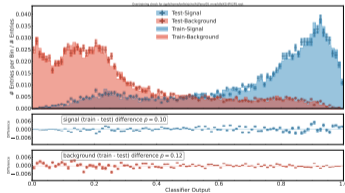
(a) CS1



(b) CS2



(c)  $P_{\pi^0}(\gamma_0)$



(d)  $P_{\pi^0}(\gamma_1)$

- $CS1/CS2/P_{\pi^0}(\gamma_0)/P_{\pi^0}(\gamma_1)$  are 4D Optimized for Low/High mass region with grid-scanning method
- Mass-indep  $B \rightarrow Ka'$  MC samples are used
- All stream BkgMC EXCEPT 00 generic are used
- Punzi Figure of Merit (PFM) is adopted for optimization

$$PFM = \frac{\epsilon_{sig}}{a/2 + \sqrt{N_{bkg}}},$$

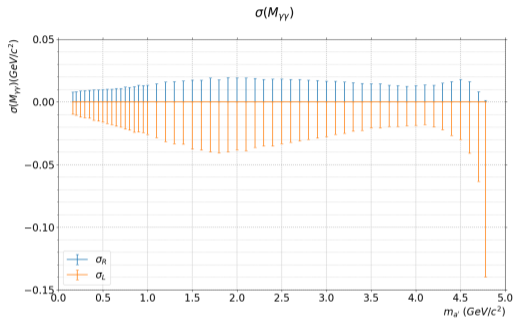
where  $a = 3$  is targeting  $\sigma$  value.

$K^+$  mode optimized values

M(a')	CS1	CS2	$P_{\pi^0}(\gamma_0)$	$P_{\pi^0}(\gamma_1)$
Low	0.929	0.944	0.115	0.130
High	0.914	0.839	0.189	0.150

- Events are accepted in each value is greater than the optimal value.

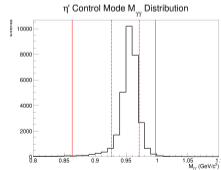
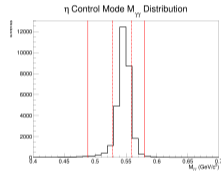
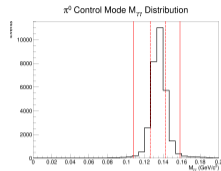
# Analysis Region



- calculate  $\sigma$  for each  $a'$  mass sig MC
- $\sigma = \sqrt{\frac{\sum(M_{\gamma\gamma} - M_{a'})^2}{N_{evt}}}$
- Signal Region :  $3\sigma_L$  to  $3\sigma_R$ .  $w = 3(\sigma_L + \sigma_R)$
- Fitting Region :  $3\sigma_L + w$  to  $3\sigma_R + w$
- Mass Scanning Step Size :  $\sigma_R$
- $M_{\gamma\gamma}$  : diphoton system invariant mass
- $M_{a'}$  : ALP mass hypothesis

- $\pi^0, \eta, \eta'$  are 3 major gamma pair generating SM background.
- $\sigma^h = \sqrt{\frac{\sum(M_{\gamma\gamma} - m_h)^2}{N_{evt}}}$
- $3\sigma$  of each mass region of peaking background is removed from the analysis and used for Control Mode Validation

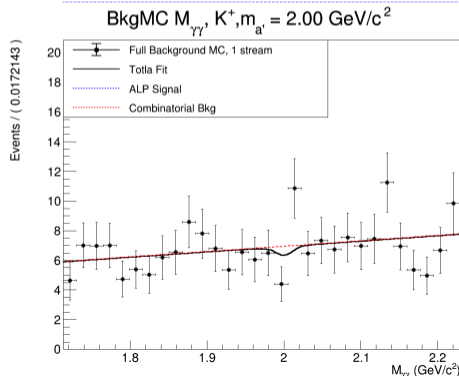
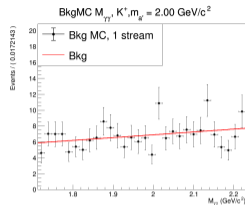
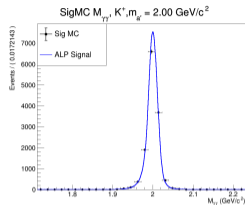
h' veto region	
Type	$3\sigma$ $M_{\gamma\gamma}$ region (GeV/c <sup>2</sup> )
$\pi^0$	0.109 ~ 0.158
$\eta$	0.497 ~ 0.578
$\eta'$	0.882 ~ 0.997



# Fitting

Dataset	$M_{\gamma\gamma}$
ALP Signal	2-Side Crystal Ball
Combinatorial Bkg	2nd Chebychev Poly

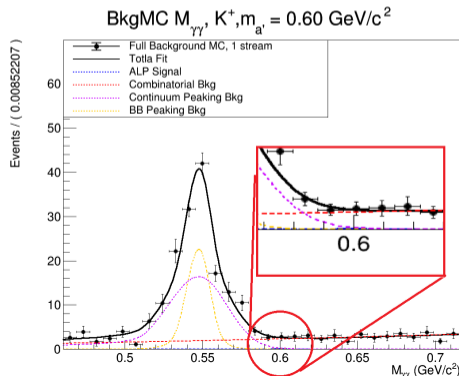
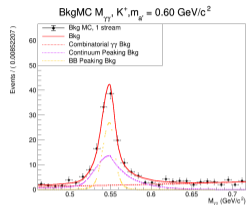
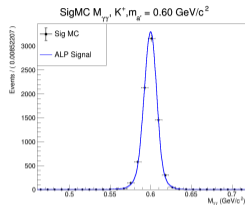
- Unbinned 1D Maximum Likelihood fit is performed to  $M_{\gamma\gamma}$  distributions.
- Signal Yield earned with S+B fitting

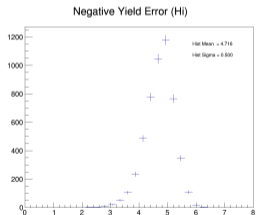
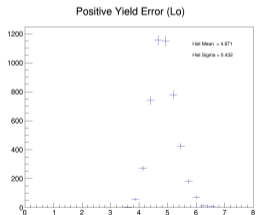
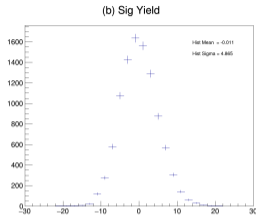
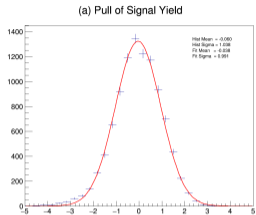


# Fitting

Dataset	$M_{\gamma\gamma}$
ALP Signal	2-Side Crystal Ball
Combinatorial Bkg	2nd Chebychev Poly
Continuum Peaking Bkg	2-Side Crystal Ball
BB Peaking Bkg	2-Side Crystal Ball

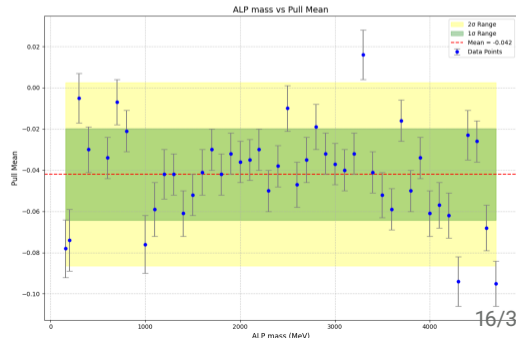
- Unbinned 1D Maximum Likelihood fit is performed to  $M_{\gamma\gamma}$  distributions.
- Additional pdf is assigned for control events when peaking background appears in fitting region.
- Signal Yield earned with S+B fitting
- Continuum Peaking backgrounds :  $e + e^- \rightarrow qq \rightarrow h' X$ .
- BB Peaking backgrounds :  $B \rightarrow Kh'$





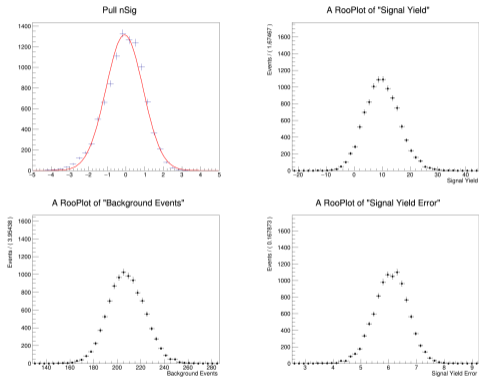
ToyMC Study with  $K^+$ ,  $M_{a^1} = 2.0 \text{ GeV}/c^2$  mode. nSig=0.13 and nBkg=241.4

- Signal Extraction Strategy Biasness is tested with pdf based ToyMC study
- 10000 ToyMC datasets are generated / fitted
- nSig/nBkg Toy events are from pdf fit result
- Number of Sig/Bkg events in each ToyMC dataset follows MC result as poisson.
- Fit Bias (4.2%) is applied as calibration factor to B.F and U.L.

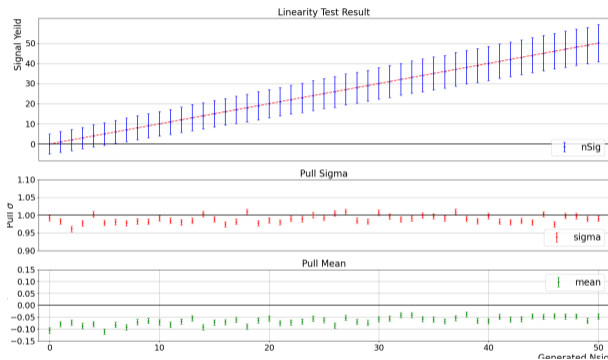




# Linearity Test

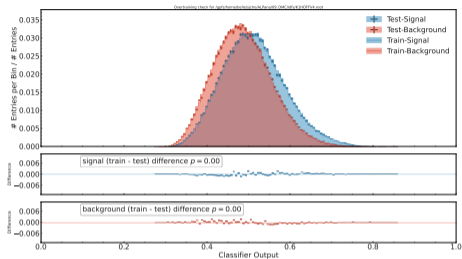


sample output of LT of  $B^+ \rightarrow K^+ a'(2500) (\rightarrow \gamma\gamma)$  (0 Input)



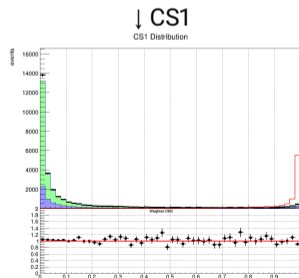
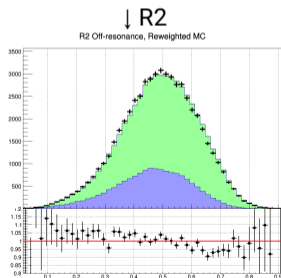
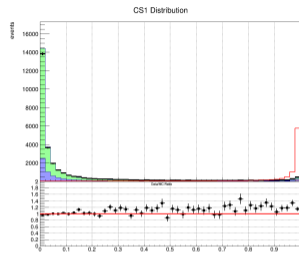
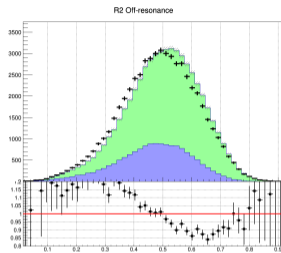
Linearity Test Result.  $N_{sig}^{in}$  vs  $N_{sig}^{out}$ , red dashed line is expected value(Upper). Pull Mean and Sigma (Middle/Bottom)

# Continuum re-weighting

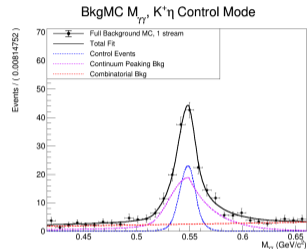
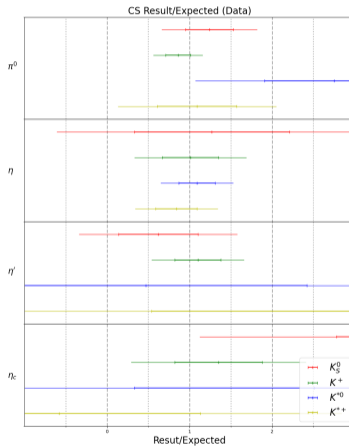
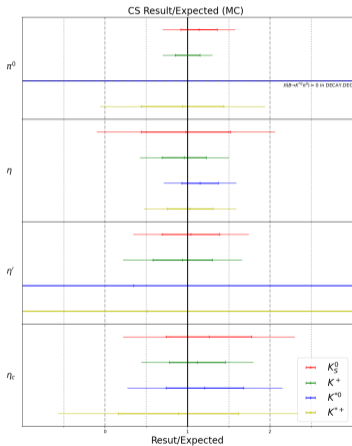


Re-weighting FBBDT score( $p$ ) of Data(Signal) and MC(Background)

- FBBDT Classifier which trained to Data/MC discrepancy.
- The classifier output shows how much the data and MC disagrees
- All variables Used in Continuum Suppression.
- Full skim-passed off-resonance dataset.
- Re-weighting factor  $w = \frac{p}{1-p}$



# Control Modes : $B \rightarrow K \eta' (\rightarrow \gamma\gamma)$ Validation



- Control Mode Validation with  $B \rightarrow K^{(*)} \eta (\eta' \rightarrow \gamma\gamma)$  where  $\eta' = \pi^0, \eta, \eta', \eta_c$ .
- Generally good agreement except some very low ( $\mathcal{O}(10^{-8})$ ) B.F. modes

# Long Lived ALP

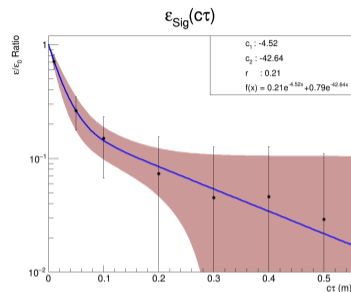
- ALP lifetime is determined by  $M_{a'}$  and  $g_{a'W}$  (ALP-W coupling).
- Not negligible in low ALP mass hypothesis.
- Long-lived Particle (LLP) signal MC are generated and signal efficiency drop down ratio is calculated.

$$\Gamma_{a'} = g_{a'W}^2 M_{a'}^3 \sin^4 \theta_W / 64\pi$$

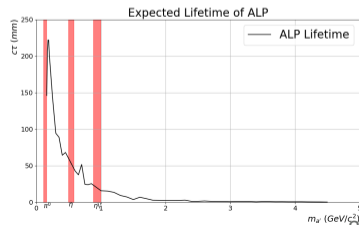
$$c\tau = \frac{c\hbar}{\Gamma_{a'}}$$

$$\varepsilon(x)/\varepsilon_0 = r e^{c_1 x} + (1-r) e^{c_2 x}$$

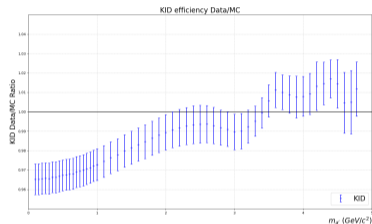
- where  $x$  is  $c\tau$  in meter(m),  $c_1, c_2$  and  $r$  are floating parameters.
- LLP efficiency drop function included into  $g_{a'W}$  limit calculation.
- Plots show a sample of LLP signal efficiency drop ratio function and expected lifetime of ALP with 90 C.L. upper limit  $g_{a'W}$  value.



Relative Efficiency vs ALP life time  $\varepsilon(c\tau)/\varepsilon_0$



Source	$K_S^0$ mode	$K^+$ mode	$K^{*0}$ mode	$K^{*+}$ mode
Selection Efficiency			19.0	
Long lived ALP Efficiency			6.0	
Continuum shape correction			4.1	
Photon Detection efficiency			4.0	
$K^+$ Identification efficiency	-	3.6	3.6	-
$f^{00} / f^{+-}$	1.7	2.1	1.7	2.1
$K_S^0$ reconstruction efficiency	1.6	-	-	1.6
$N_{B\bar{B}}$			1.4	
Tracking efficiency	0.7	0.4	0.7	1.1
Total	20.9	20.9	20.9	21.0

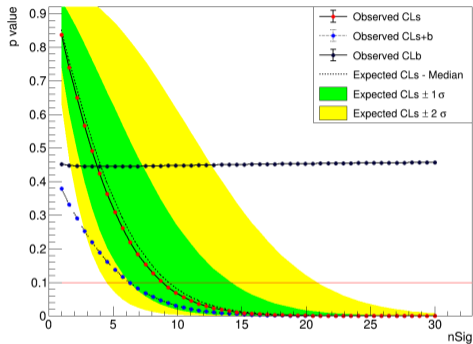


Kaon ID Data/MC

- $\epsilon_{KID} = \frac{\text{number of tracks identified as Kaon}}{\text{number of Kaon tracks}}$
- $K_S^0$  reconstruction : nisKsFinder recon efficiency

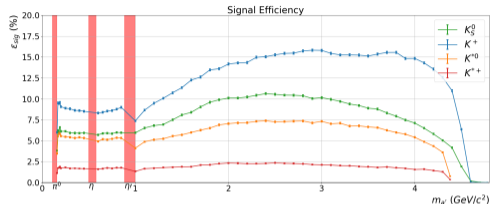
# Upper Limit estimation

HypoTest Scan Result



[90CL Upper Limit  $N_{Sig}$  : 9.28]

- Use CLs frequentist method to estimate upper limit.
- Testing Number of Signal Yields for each Kaon modes.
- 90 C.L. U.L of B.F sett around  $1 \times 10^{-7}$ .



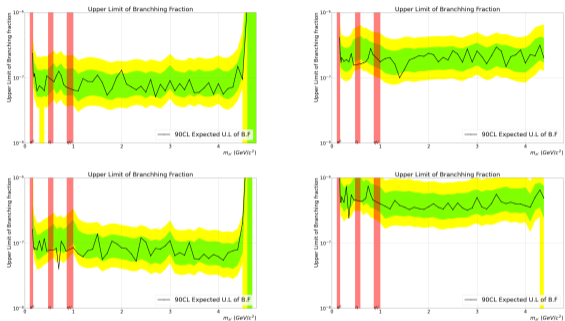
$$\epsilon_0 = \frac{N_{Sig}^{remain}}{N_{Sig}^{gen}}$$

$$\text{Expected } \mathcal{B}(B \rightarrow Ka'(a' \rightarrow \gamma\gamma)) = \frac{N_{Sig}}{\epsilon_0 \times N_B}$$

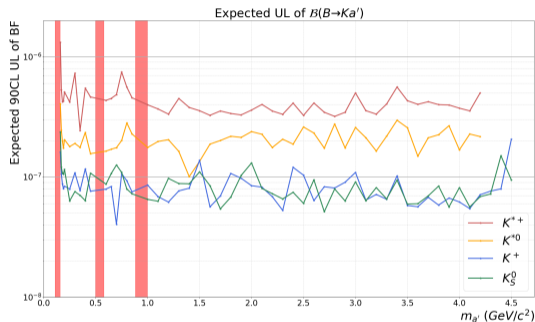
$$\mathcal{L}(\mathcal{B}, \epsilon) \sim \text{Poisson}(N_{Sig} + N_{Bkg}) \times \text{Gauss}(\epsilon, \epsilon_0, \sigma_\epsilon)$$

$$\text{Gauss}(\epsilon, \epsilon_0, \sigma_\epsilon) \sim \exp\left(-\frac{(\epsilon - \epsilon_0)^2}{2\sigma_\epsilon^2}\right)$$

# Upper Limit estimation

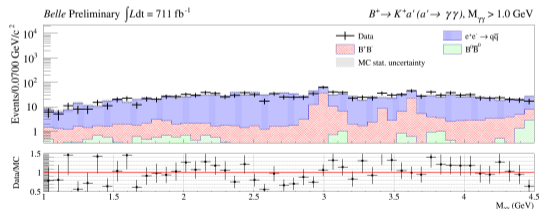
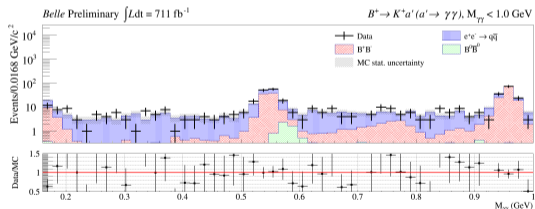
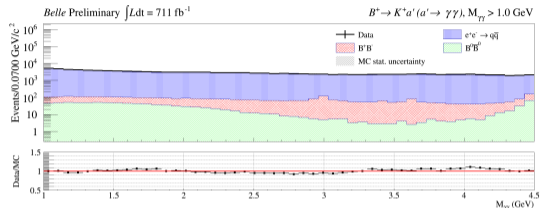
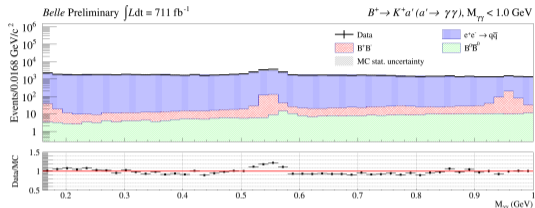


Expected upper limit of branching fraction of  $K_S^0$  mode (Upper left),  $K^+$  mode (Bottom left),  $K^{*0}$  mode (Upper right),  $K^{*+}$  mode (Bottom right), and its 1 and 2 sigma range earned by background only model.



Expected U.L. of  $\mathcal{B}(B \rightarrow K a' (a' \rightarrow \gamma\gamma))$ .

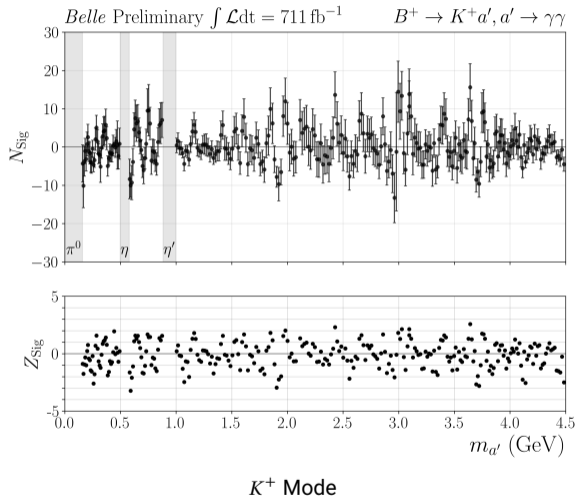
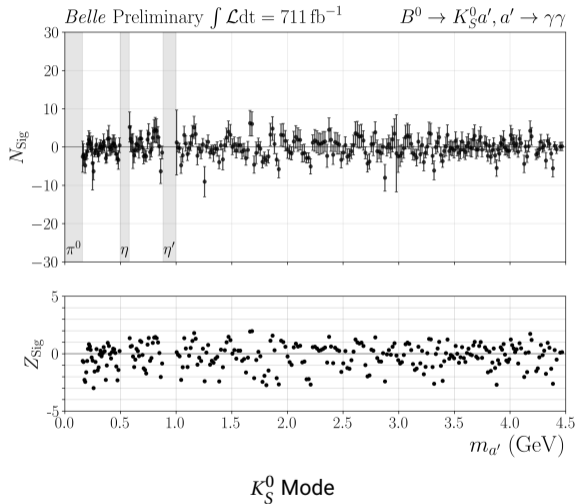
# Unblinding Result : Data/MC Comparison



[Figure 2] Before (top) and After(bottom) the MVA cuts

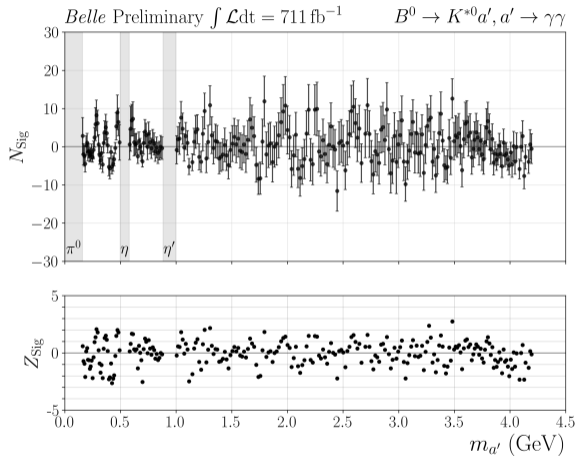


# Unblinding Result : Signal Extraction

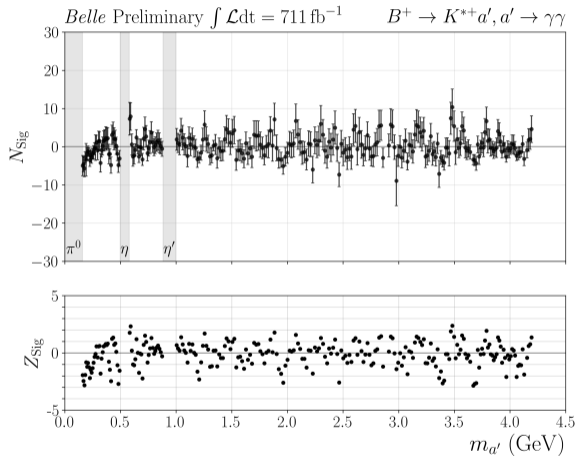


[Figure 3] signal extraction result :  $K_S^0$  and  $K^+$

# Unblinding Result : Signal Extraction



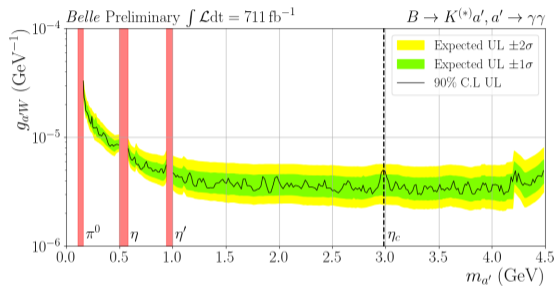
$K^{*0}$  Mode



$K^{*+}$  Mode

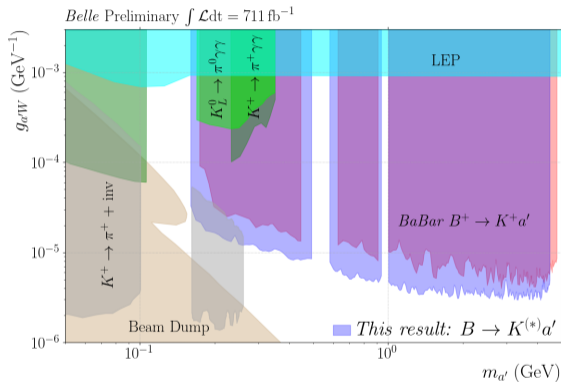
[Figure 3] Signal extraction result :  $K^{*0}$  and  $K^{*+}$

# Unblinding Result : $g_{a'W}$ limitation



[Figure 4]

- Simultaneous fit on 4 kaon modes for  $g_{a'W}$  limitation.
- Set more stringent limitation than *BaBar*.



[Figure 5]

## Summary

- Searching for **Axion-Like Particle (ALP)** through  $B \rightarrow K^{(*)} a'$  ( $a' \rightarrow \gamma\gamma$ ) Decay at Belle
- Promptly decaying ALP.  $a' \rightarrow \gamma\gamma$ .
  - ▶ The lifetime considered as signal efficiency constraint.
- Analysis strategy established with MC:
  - ▶ Include event selection, background suppression, selection optimization, signal extraction and upper limit calculations
- Result shows more stringent constraint on  $g_{a'W}$  than existing limit from *BaBar*.
  - ▶ This is one of **most powerful limitation on  $g_{a'W}$  in the world**.
- Long-lived ALP study with more integrated luminosity is expected from Belle II experiment.



# $g_{a'W}$ Calculation

$$\Gamma(B \rightarrow K a') = \frac{M_B^3}{64\pi} |g_{a'bs}|^2 \left(1 - \frac{M_K^2}{M_B^2}\right)^2 f_0^2(M_{a'}^2) \lambda_{K a'}^{1/2}$$

$$\Gamma(B \rightarrow K^* a') = \frac{M_B^3}{64\pi} |g_{a'bs}|^2 A_0^2(M_{a'}^2) \lambda_{K^* a'}^{3/2},$$

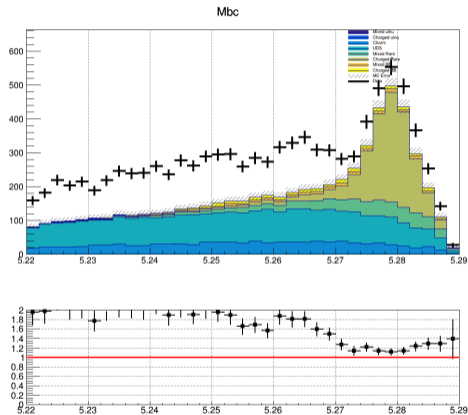
$$g_{a'bs} = -\frac{3\sqrt{2}G_F M_W^2 g_{a'W}}{16\pi^2} \sum_{\alpha=c,t} V_{cb} V_{\alpha s}^* f\left(\frac{M_\alpha^2}{M_W^2}\right)$$

$$f(x) \equiv \frac{x[1 + x(\log x - 1)]}{(1-x)^2}$$

$$f_0(M_{a'}^2) = \frac{0.330}{1 - M_{a'}^2/37.46}$$

$$A_0(M_{a'}^2) = \frac{1.364}{1 - M_{a'}^2/27.88} - \frac{0.990}{1 - M_{a'}^2/36.78}.$$

# Continuum Data/MC Calibration

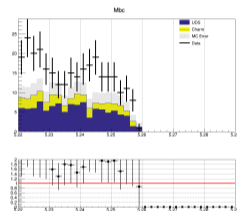


- $M_{bc}$  of  $B^+ \rightarrow K^+ a' (\rightarrow \gamma\gamma)$  at  $\pi^0$  mass window
- $\pi^0$  veto is applied in inverted way

- $q\bar{q}$  seems have large Data/MC discrepancy
- continuum correction with Off-resonance data
- Off-resonance data from Exp 31 to Exp 65

Window	Data/MC Ratio
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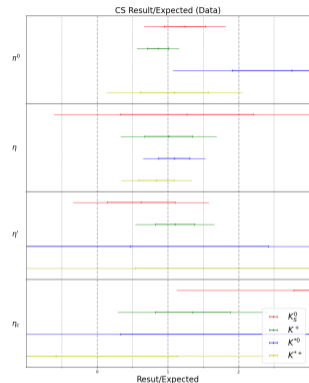
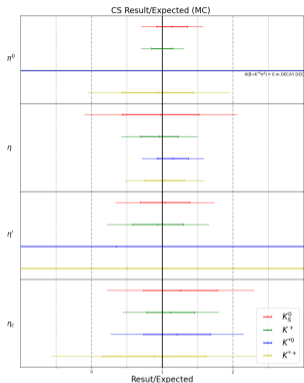
$\pi^0$	1.98
$\eta$	2.83
$\eta'$	1.49



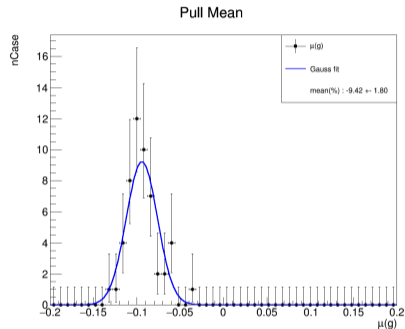
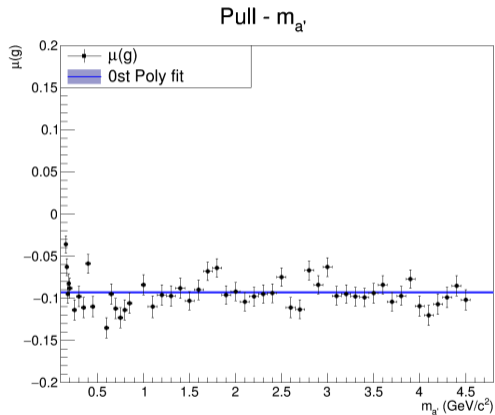
- Apply correction factor to each mass window dataset :

# Control Mode : $B \rightarrow Kh'(\rightarrow \gamma\gamma)$

Mode	Result(MC)	$\Gamma_1 \times \Gamma_2(\text{DECAY.DEC})$
$B^0 \rightarrow K_S^0 \pi^0$	$4.44 \pm 0.42 \times 10^{-6}$	$4.89 \times 10^{-6}$
$B^+ \rightarrow K^+ \pi^0$	$1.14 \pm 0.05 \times 10^{-5}$	$1.27 \times 10^{-5}$
$B^0 \rightarrow K^{*0} \pi^0$	$-.81 \pm 0.64 \times 10^{-7}$	$0.00 \times 10^{-7}$
$B^+ \rightarrow K^{*+} \pi^0$	$3.72 \pm 1.48 \times 10^{-6}$	$6.81 \times 10^{-6}$
$B^0 \rightarrow K_S^0 \eta$	$6.74 \pm 1.60 \times 10^{-7}$	$3.74 \times 10^{-7}$
$B^+ \rightarrow K^+ \eta$	$0.90 \pm 0.31 \times 10^{-6}$	$1.06 \times 10^{-6}$
$B^0 \rightarrow K^{*0} \eta$	$6.88 \pm 8.42 \times 10^{-6}$	$6.26 \times 10^{-6}$
$B^+ \rightarrow K^{*+} \eta$	$7.51 \pm 1.45 \times 10^{-6}$	$7.60 \times 10^{-6}$
$B^0 \rightarrow K_S^0 \eta'$	$8.02 \pm 1.58 \times 10^{-7}$	$6.88 \times 10^{-7}$
$B^+ \rightarrow K^+ \eta'$	$1.44 \pm 0.19 \times 10^{-6}$	$1.49 \times 10^{-6}$
$B^0 \rightarrow K^{*0} \eta'$	$2.06 \pm 1.92 \times 10^{-7}$	$0.81 \times 10^{-7}$
$B^+ \rightarrow K^{*+} \eta'$	$1.69 \pm 3.57 \times 10^{-7}$	$1.04 \times 10^{-7}$
$B^0 \rightarrow K_S^0 \eta_c$	$2.82 \pm 0.88 \times 10^{-7}$	$1.74 \times 10^{-7}$
$B^+ \rightarrow K^+ \eta_c$	$3.94 \pm 0.92 \times 10^{-7}$	$3.09 \times 10^{-7}$
$B^0 \rightarrow K^{*0} \eta_c$	$7.41 \pm 2.62 \times 10^{-7}$	$4.80 \times 10^{-7}$
$B^+ \rightarrow K^{*+} \eta_c$	$4.13 \pm 5.45 \times 10^{-7}$	$5.10 \times 10^{-7}$







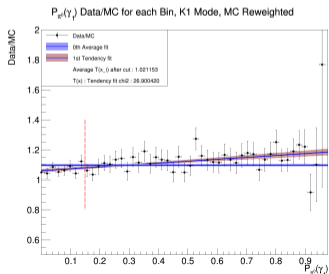
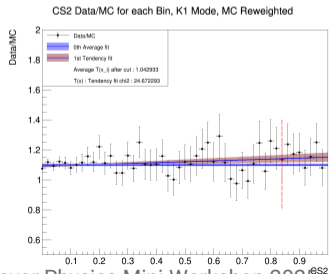
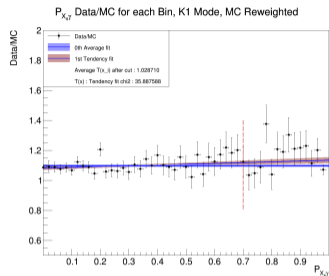
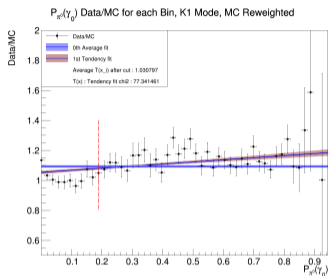
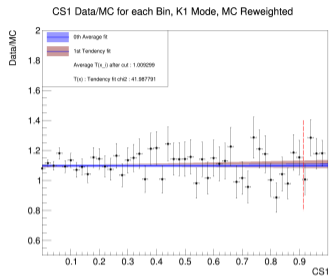
- fitting bias
- Average level as systematics

- Scanning points :
- $K_S^0, K^+ : 324$
- $K^{*+}, K^{*0} : 193$
- Significance  $S = \sqrt{2(NLL_{s+b} - NLL_b)}$
- $p_{global} = p_{local} + \langle N_{up}(Z_0) \rangle e^{\frac{z_0^2 - z^2}{2}}$
- $Z_0 : 1\sigma$

## LEE calculation example

- $B^+ \rightarrow K^+ A(3500)$
- $N_{up}(1\sigma) / N_{toy} = 0.1648$
- $3.53\sigma$  global significance at  $5\sigma$  local significance

# Systematics : FBBDT Data/MC



- Use off-resonance data
- Direct comparison easily affected by statistical fluctuation
- 1st order polynomial fit to Data/MC hist for each FBBDT result
- Compare poly function average with total average value after cut
- quadratic summation 5 FBBDT Data/MC efficiency result.

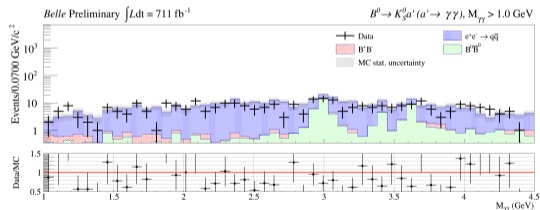
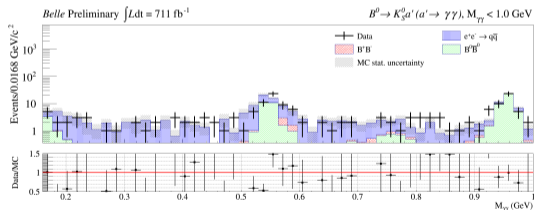
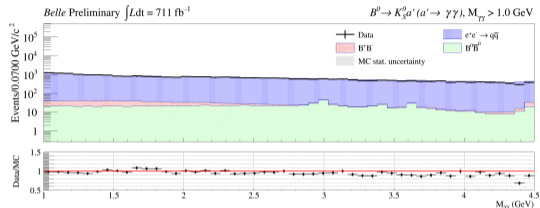
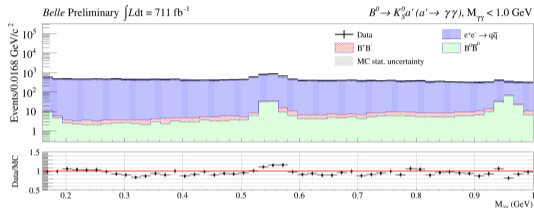
# Systematic Study : reference

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Source	reference
nBB	nBB
$\Upsilon(4S) \rightarrow B^+ B^-$	pdg
$\Upsilon(4S) \rightarrow B^0 \bar{B}^0$	pdg
Photon Detection	BN499
Tracking efficiency	BN1165
KID	BN779
PID	BN779
$K_S^0$ recon	BN1472

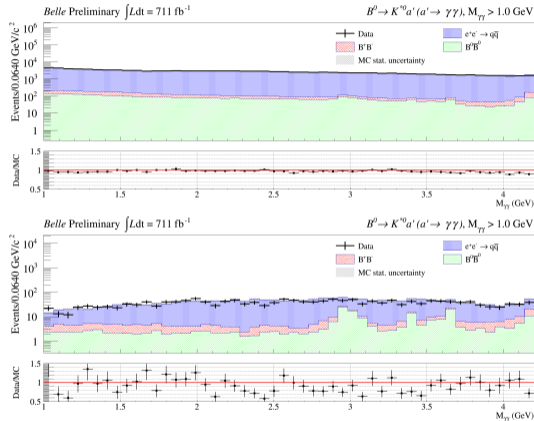
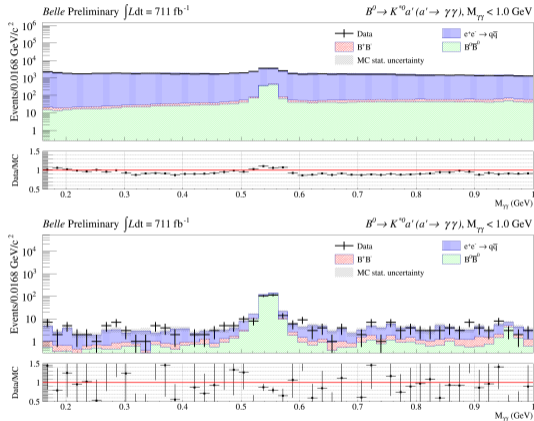
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# Unblinding Result : $K_S^0$ Data/MC Comparision



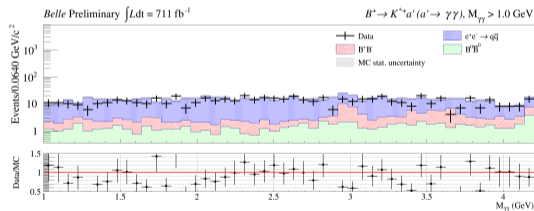
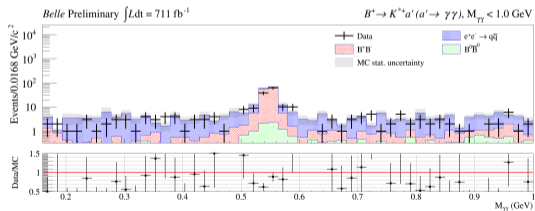
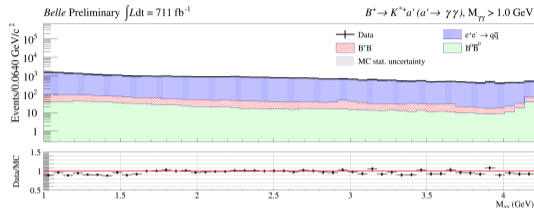
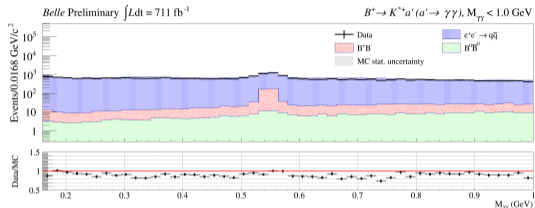
[Figure 6] (Supplemental) Before (top) and After(bottom) the MVA cuts

# Unblinding Result : $K^{*0}$ Data/MC Comparision



[Figure 6] (Supplemental) Before (top) and After(bottom) the MVA cuts

# Unblinding Result : $K^{*+}$ Data/MC Comparison



[Figure 6] (Supplemental) Before (top) and After (bottom) the MVA cuts