

# Study of $D^0$ decays to the invisible final states at Belle II

Yonsei University  
Chanho Kim

[ckh424@yonsei.ac.kr](mailto:ckh424@yonsei.ac.kr)

# Introduction to analysis

- In SM, heavy (B or D) decays to  $\nu\bar{\nu}$  is helicity suppressed with an expected branching fraction of  $\text{Br}(D^0 \rightarrow \nu\bar{\nu}) = 1.1 \cdot 10^{-30}$ , which is beyond the reach of current collider experiments.

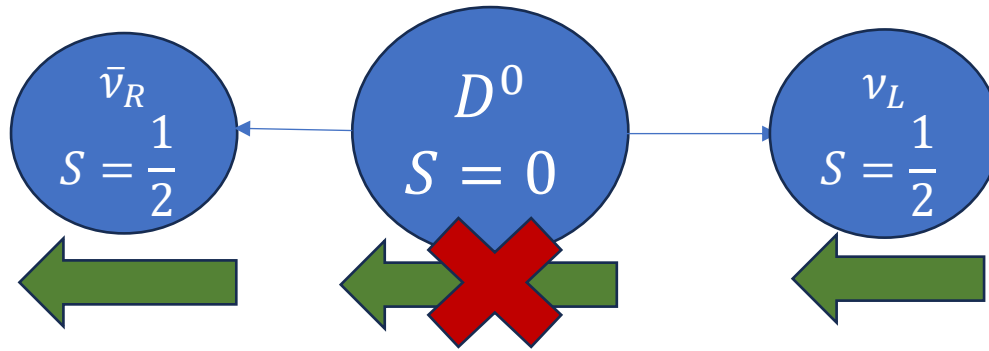


Figure1: Scheme of helicity suppressing

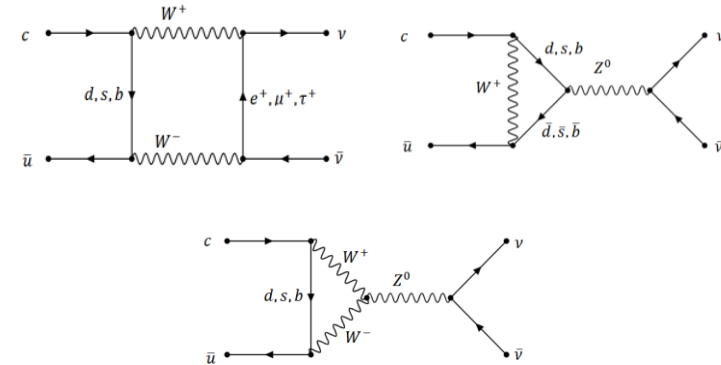
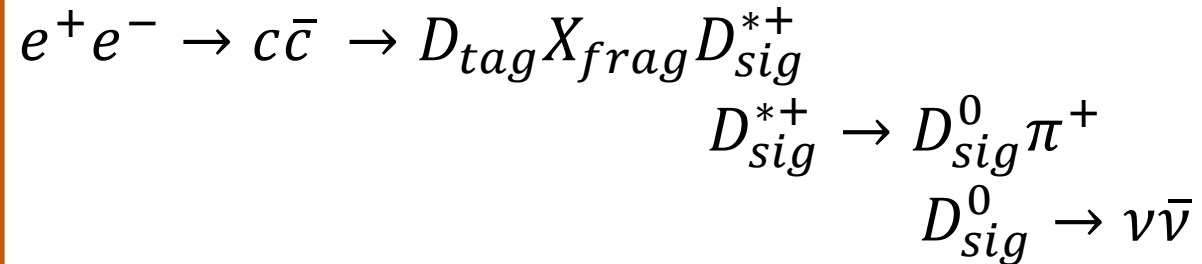


Figure2: Feynman diagram for  $D^0 \rightarrow \nu\bar{\nu}$

- Therefore, search for  $D^0 \rightarrow$  invisible final states is sensitive to new physics
- The previous result is  $BR_{UL} = 9.4 \times 10^{-5}$  on  $924 \text{ fb}^{-1}$  data samples at 90% CL at belle [Phys. Rev. D 95, 011102(R)]

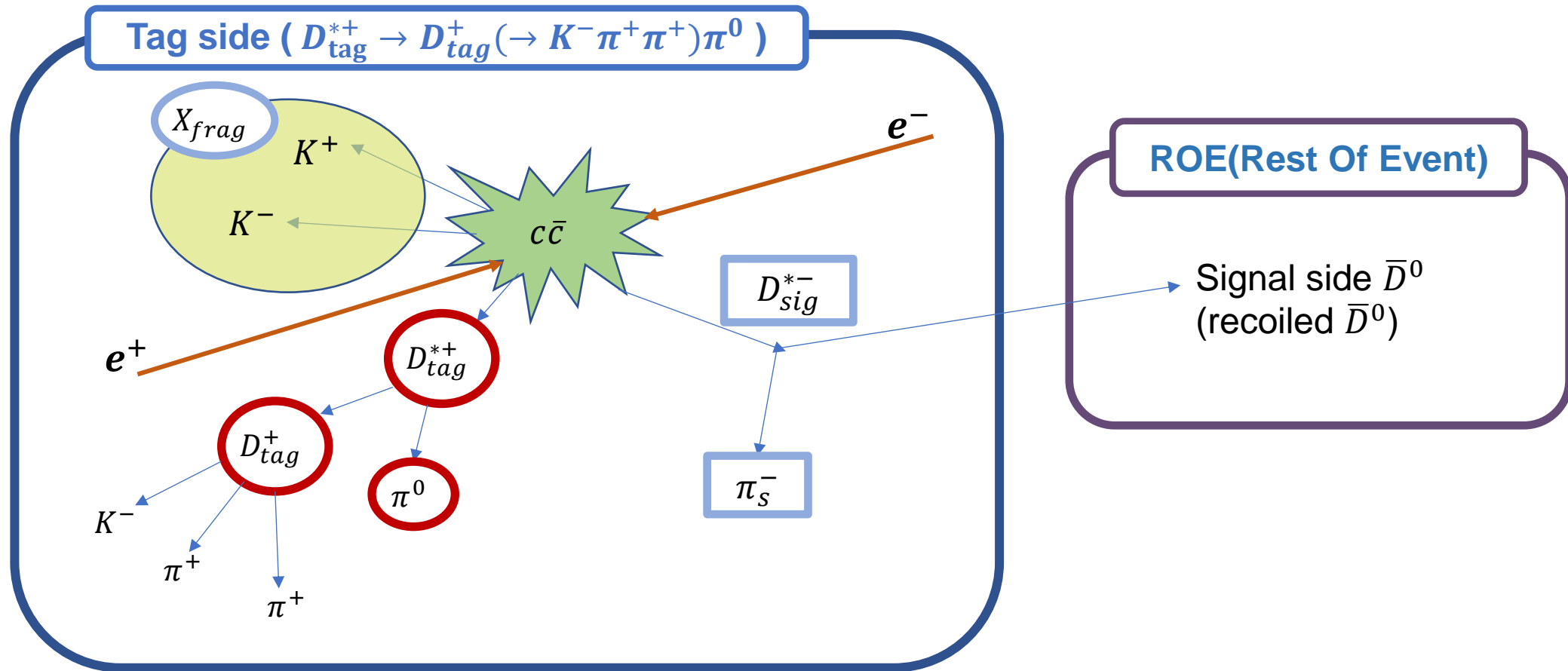
# MC simulation samples

- 20M signal MC samples were used
- Signal Event used for simulation :



- MC15ri generic MC( $1ab^{-1}$ ) is used as generic background MC sample
- 20M Control sample ( $D^0 \rightarrow K^-\pi^+$ )

# Analysis Method : Charm Tagger



**Figure3:** schematics of signal event with tag side decay  $D_{tag}^{*+} \rightarrow D_{tag}^+ (\rightarrow K^- \pi^+ \pi^+) \pi^0$

# Description of Charm tagging Procedure

## Reconstruction $D_{tag}, D_{tag}^*$

1. Reconstruct  $D_{tag}$  using the pre-chosen decay channels
2. Reconstruct  $D_{tag}^*$

## Recoil part 1 ( $D^{*+}$ )

1. Calculate  $M_{miss}(D_{tag}^* X_{frag})$  which is regarded as mass of  $D_{sig}^{*+}$
2. Apply kinematic mass constrained Fit on  $M_{miss}(D_{tag}^* X_{frag})$  to  $m_{D^{*+}}$
3. BCS of  $D_{sig}^{*+}$  by using chiProb from step 2

## Recoil part 2 ( $D^0$ )

5. Using slow pion, calculate  $M_{miss}(D_{tag}^* X_{frag} \pi_s^+)$  which is regarded as mass of signal side  $D^0$
6. BCS of  $D^0$  by using angle between  $D_{sig}^0$  and tag side hadron in cm frame

**Table1.** Tag reconstruction channels

$D^0$ decay	$Br(\%)$	$D^+$ decay	$Br(\%)$	$\Lambda_c^+$ decay	$Br(\%)$	$D_s^+$ decay	$Br(\%)$
$K^-\pi^+$	3.9	$K^-\pi^+\pi^+$	9.4	$pK^-\pi^+$	5.0	$K^+K^-\pi^+$	5.5
$K^-\pi^+\pi^0$	13.9	$K^-\pi^+\pi^+\pi^0$	6.1	$pK^-\pi^+\pi^0$	3.4	$K_S^0K^+$	1.5
$K^-\pi^+\pi^+\pi^-$	8.1	$K_S^0\pi^+$	1.5	$pK_S^0$	1.1	$K_S^0K_S^0\pi^+$	5.4
$K^-\pi^+\pi^+\pi^-\pi^0$	4.2	$K_S^0\pi^+\pi^0$	6.9	$\Lambda^0\pi^+$	1.1	$K^+K^-\pi^+\pi^0$	5.6
$K_S^0\pi^+\pi^-$	2.9	$K_S^0\pi^+\pi^+\pi^-$	3.1	$\Lambda^0\pi^+\pi^0$	3.6	$K_S^0K^-\pi^+\pi^+$	1.5
$K_S^0\pi^+\pi^-\pi^0$	5.4	$K^+K^-\pi^+$	1.0	$\Lambda^0\pi^+\pi^+\pi^-$	2.6	$K^+\pi^-\pi^+K_S^0$	1.0
$K^-\pi^+\pi^0\pi^0$	8.9	$K^-K^+\pi^+\pi^0$	0.7	$p^+\pi^-\pi^+$	0.5	$\pi^+\pi^-\pi^+$	1.0
$\pi^-\pi^+$	0.1	$\pi^-\pi^+\pi^+$	0.3	$p^+K^-K^+$	0.1	$\pi^+K_S^0$	0.1
$\pi^-\pi^+\pi^-\pi^+$	0.8	$\pi^-\pi^+\pi^+\pi^0$	1.2	$p^+K^-\pi^+\pi^0\pi^0$	0.1	$\pi^+\pi^0K_S^0$	0.5
$\pi^-\pi^+\pi^0$	1.5	$K^+K_S^0K_S^0$	0.3	$p^+\pi^-\pi^+\pi^-\pi^+$	0.2	$K^-K^+\pi^+\pi^-\pi^+$	0.7
$\pi^-\pi^+\pi^0\pi^0$	1.0	$\pi^+\pi^0$	0.1	$p^+K_S^0\pi^0$	2.0		
$K^-K^+$	0.4			$p^+K_S^0\pi^+\pi^-$	1.6		
$K^-K^+\pi^0$	0.3			$\pi^+\pi^-\Sigma^+$	4.5		
$K^-K^+K_S^0$	0.4			$\pi^+\pi^-\pi^0\Sigma^+$	1.2		
$\pi^0K_S^0$	1.2			$\pi^0\Sigma^+$	1.2		
sum	53.1	sum	30.5	sum	28.2	sum	22.8

# $D_{tag}^*$ reconstruction channels and fragmentations for each tag particle

$D^{*+}$ decay	Br(%)	$D^{*0}$ decay	Br(%)	$D_s^{*+}$ decay	Br(%)
$D^0\pi^+$	67.7	$D^0\pi^0$	61.9	$D_s^+\gamma$	93.5
$D^+\pi^0$	30.7	$D^0\gamma$	38.1		
sum	98.4	sum	100.0	sum	93.5

**Table3:**  $D_{tag}^*$  channel

$D^{*+}$ or $D^+$	$D^{*0}$ or $D^0$	$\Lambda_c^+$	$D_s^{*+}$ or $D_s^+$
nothing( $K^+K^-$ )	$\pi^+(K^+K^-)$	$\pi^+\bar{p}$	$K_S^0$
$\pi^0(K^+K^-)$	$\pi^+\pi^0(K^+K^-)$	$\pi^+\pi^0\bar{p}$	$\pi^0K_S^0$
$\pi^+\pi^-(K^+K^-)$	$\pi^+\pi^+\pi^-(K^+K^-)$	$\pi^+\pi^-\pi^+\bar{p}$	$\pi^+K^-$
$\pi^+\pi^-\pi^0(K^+K^-)$			$\pi^+\pi^+\pi^-K_S^0$
			$\pi^+\pi^-\pi^0K_S^0$
			$\pi^+K^-$
			$\pi^+\pi^0K^-$
			$\pi^+\pi^-\pi^+K^-$

**Table4:**  $X_{frag}$  channel (total 25 channels)

# fastBDT training for Charm Tagging

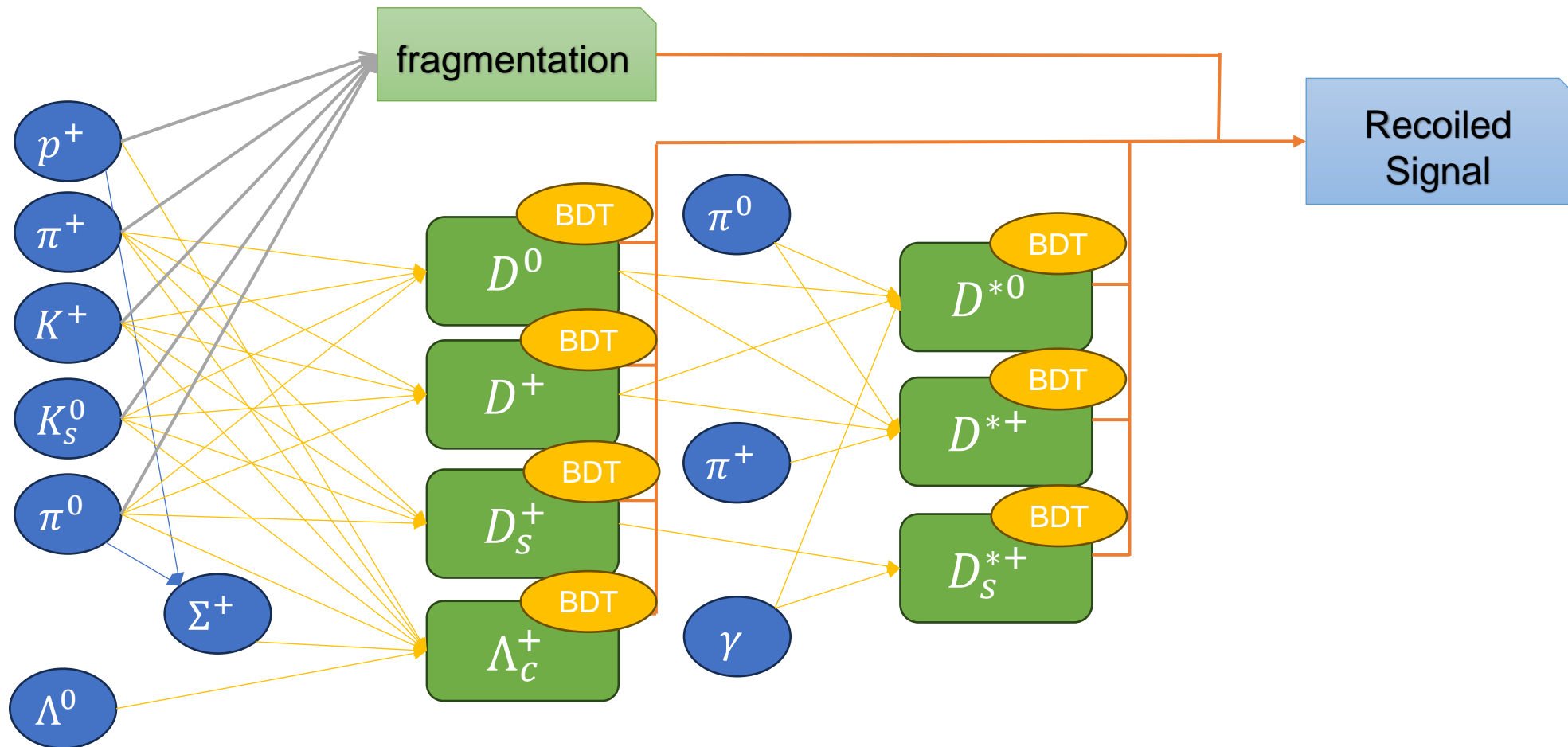
- Input Variables of fastBDT
  - For  $D_{tag}$  training  
M, p, dr(flight length), chiProb, Q, E, cosToThrustOfEvent,  
cosAngleBetweenMomentumAndVertexVectorInXYPlane, ImpactXY,  
xp, PID of daughters, cosHelicityAngle(2 body or 3 body decays),  
angle between 2 daughters of  $\pi^0(\rightarrow \gamma\gamma)$ ,  $K_S^0(\rightarrow \pi^+\pi^-)$ ,  $\Lambda^0(\rightarrow p^+\pi^-)$ ,  $\Sigma^+(\rightarrow p^+\pi^0)$ ,  
 $|\frac{E_{d_1}-E_{d_2}}{E_{d_1}+E_{d_2}}|$  of  $\pi^0(\rightarrow \gamma\gamma)$ ,  $K_S^0(\rightarrow \pi^+\pi^-)$ ,  $\Lambda^0(\rightarrow p^+\pi^-)$ ,  $\Sigma^+(\rightarrow p^+\pi^0)$  etc...
  - For  $D_{tag}^*$  training  
 $\Delta M(= M_{D_{tag}^*} - M_{D_{tag}})$ , momentum of  $\pi_S^\pm$ ,  $\gamma$ ,  $\pi^0$ ,  
angle between  $D_{tag}$  and  $\pi_S^\pm$ ,  $\gamma$ ,  $\pi^0$  etc...
- Hyper Parameters of BDT was optimized by applying grid search for each tag training



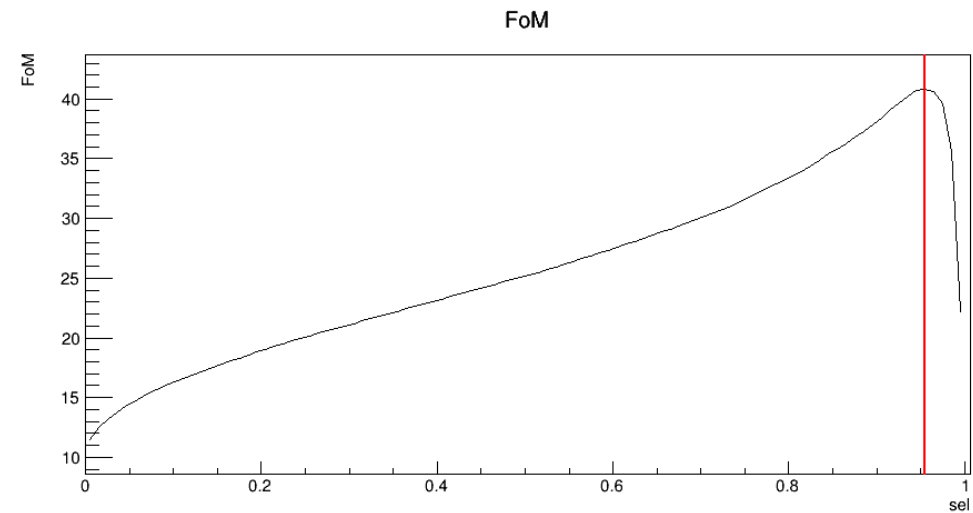
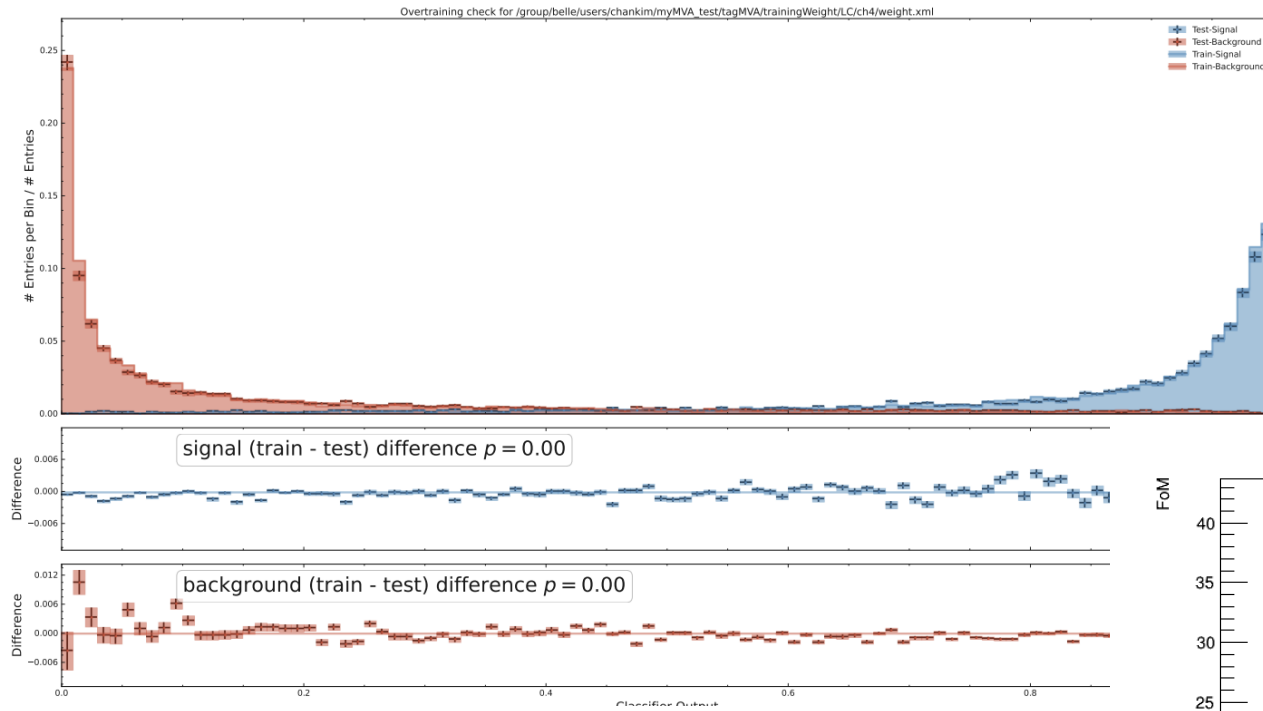
# Preselection of Charm Tagger

- For tracks :  $dr < 1.0$  ,  $|dz| < 3.0$  and InCDCAcceptance
- $\pi^\pm$  : 15 candidates with Highest pionID after pionID  $> 0.01$
- $K^\pm$  : 10 candidates with Highest kaonID after kaonID  $> 0.1$
- $p^\pm$  : 10 candidates with highest protonID after protonID  $> 0.1$
- for fragmentations, PID selection of  $\pi^\pm$ ,  $K^\pm$ ,  $p^\pm$  is on 0.1, 0.9, 0.9 and additionally require  $p > 0.1$  GeV
  
- $K_S^0, \Lambda^0$  :
  - mass and  $dr$  and  $\chi^2$  and angle between Momentum and Vertex Vector selection on  $\Lambda^0$
  - goodBelleKshort for  $K_S^0$  (similar selection to  $\Lambda^0$ )
- $\Sigma^+$  : reconstructed from  $\Sigma^+ \rightarrow p^+ \pi^0$  and mass cut ( $1.08 < M < 1.28$ )

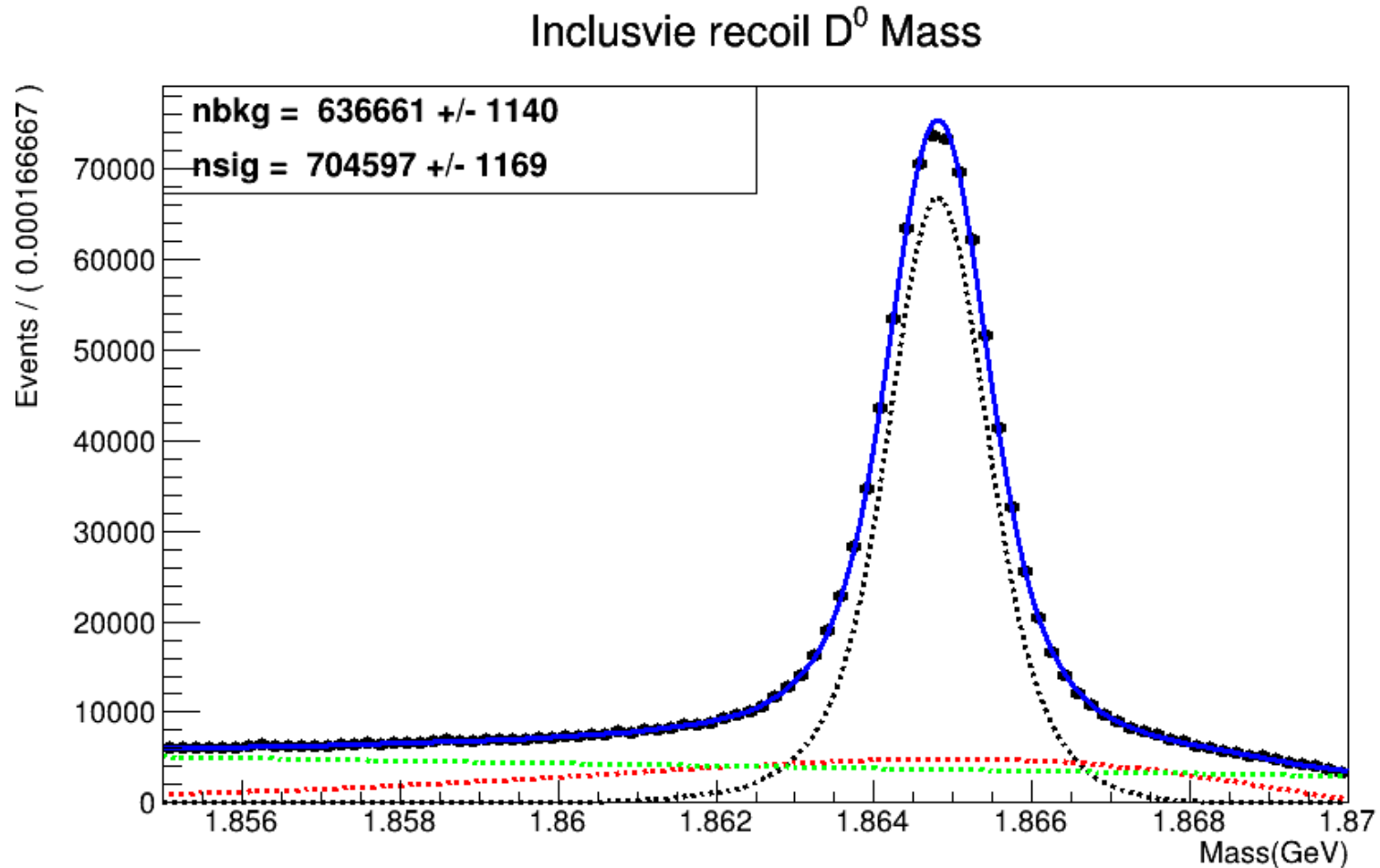
# Flow of Charm Tagger



# One example about training :



# Reconstructed $D^0$ from charm tagger on generic $c\bar{c}$ MC



# Variables for extracting signal side D

- Recoil mass ( $M_{miss}(D_{tag}^* X_{frag} \pi_s^\pm)$  or  $M_{recoil}(D^0)$ )
  - $e^+ e^- \rightarrow D_{tag}^* X_{frag} \pi_s^\pm D^0$
  - $p^\mu(e^+) + p^\mu(e^-) - (p^\mu(D_{tag}^*) + p^\mu(X_{frag}) + p^\mu(\pi_s^\pm)) = p^\mu(D_{sig}^0)$
  - $M_{recoil}(D^0) = \sqrt{p^\mu(D^0) * p_\mu(D^0)}$
  - Inclusive  $D^0$  : recoiled  $D^0$  (no requirement on signal side)  
=> 1D fit on signal side recoil  $M_{D^0}$
- $E_{ECL}$  : sum of energies from roe of tag side remained in electromagnetic calorimeter(ECL) cluster
  - Exclusive  $D^0$  : recoiled  $D^0$  (requirement on signal side)  
=> 2D fit on signal side ( $M_{D^0}, E_{ECL}$ )

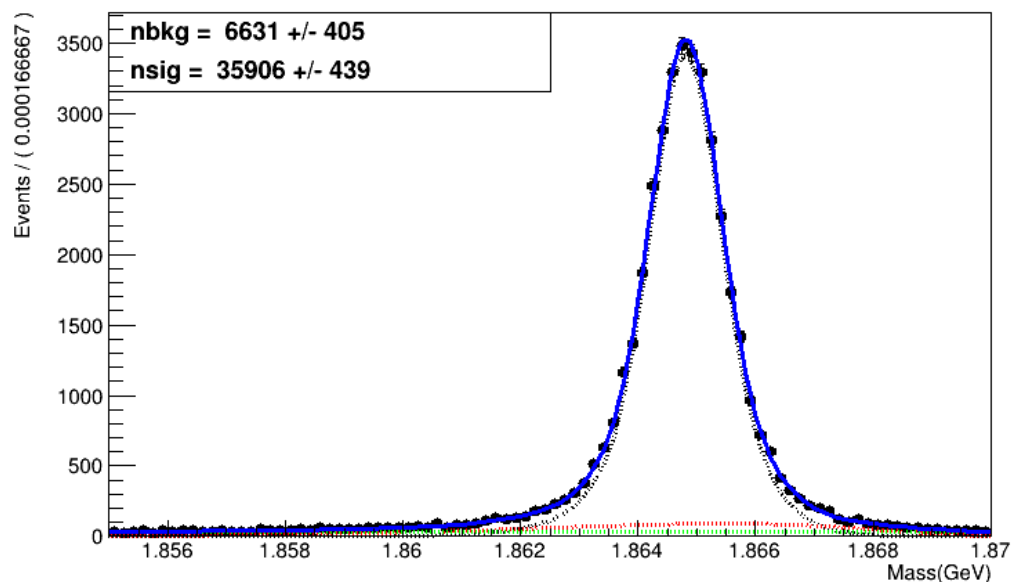
# Exclusive D requirement for signal MC & control sample (signal extraction)

- Exclusive :  $D^0$  with selection on signal side  
 $1.84 \text{ GeV} < M_{D^0} < 1.875 \text{ GeV}$  &  $E_{ECL} < 2.1 \text{ GeV}$ 
  - Signal MC ( $D^0 \rightarrow \nu\bar{\nu}$ ) selection for exclusive  $D^0$ 
    - no remaining tracks,  $\pi^0, K_L^0, K_S^0, \Lambda^0$
  - Control sample ( $D^0 \rightarrow K^-\pi^+$ ) selection for exclusive  $D^0$   
(studying about this selection is on-going ...)
    - 2 remaining tracks and 1 reconstructed  $D^0(K^-\pi^+)$
    - no  $\pi^0, K_L^0, K_S^0, \Lambda^0$
    - $|\Delta E| < 1.0 \text{ GeV}$  ( $\Delta E \equiv E(\text{recoil } D^0) - E_{K\pi}$ )

# Inclusive D fitting on signal MC / control sample

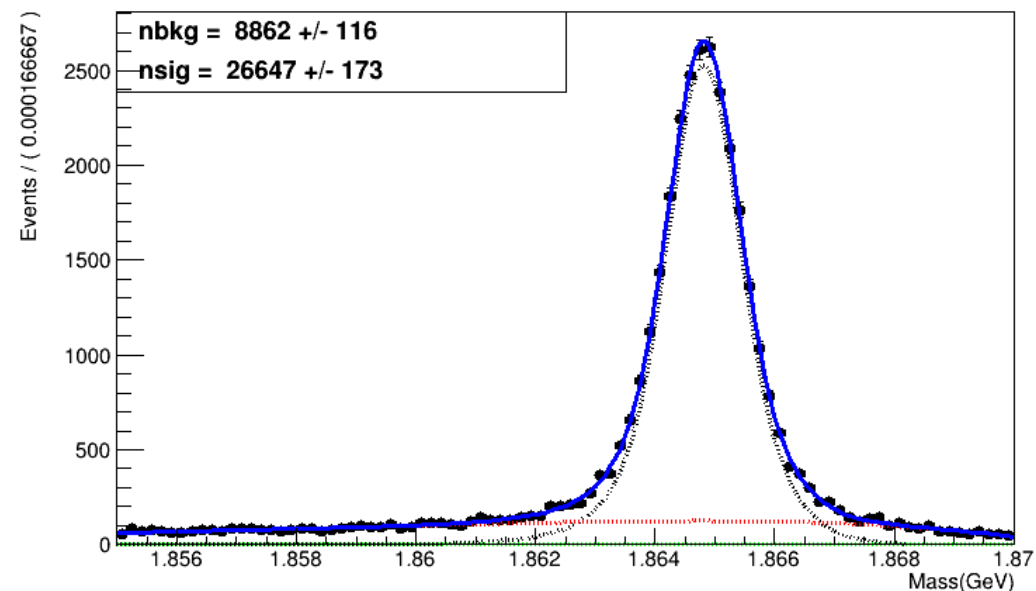
## Signal MC

Inclusive recoil  $D^0$  Mass

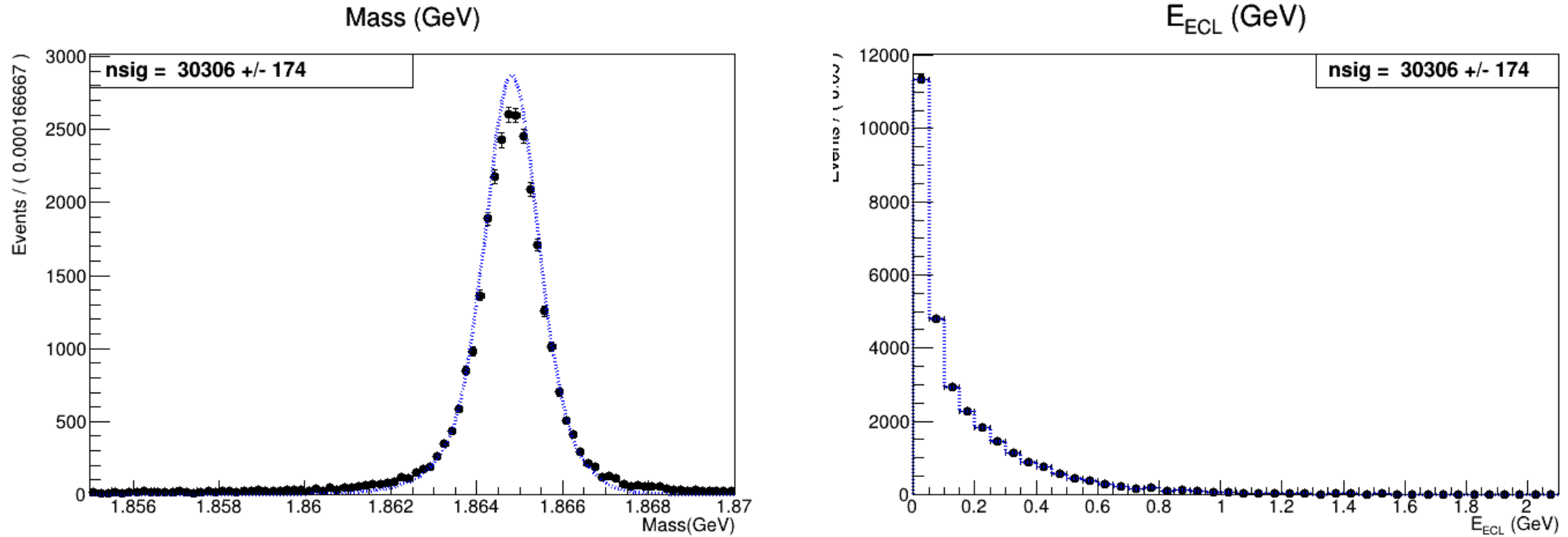


## Control sample

inclusive recoil  $D^0$  Mass



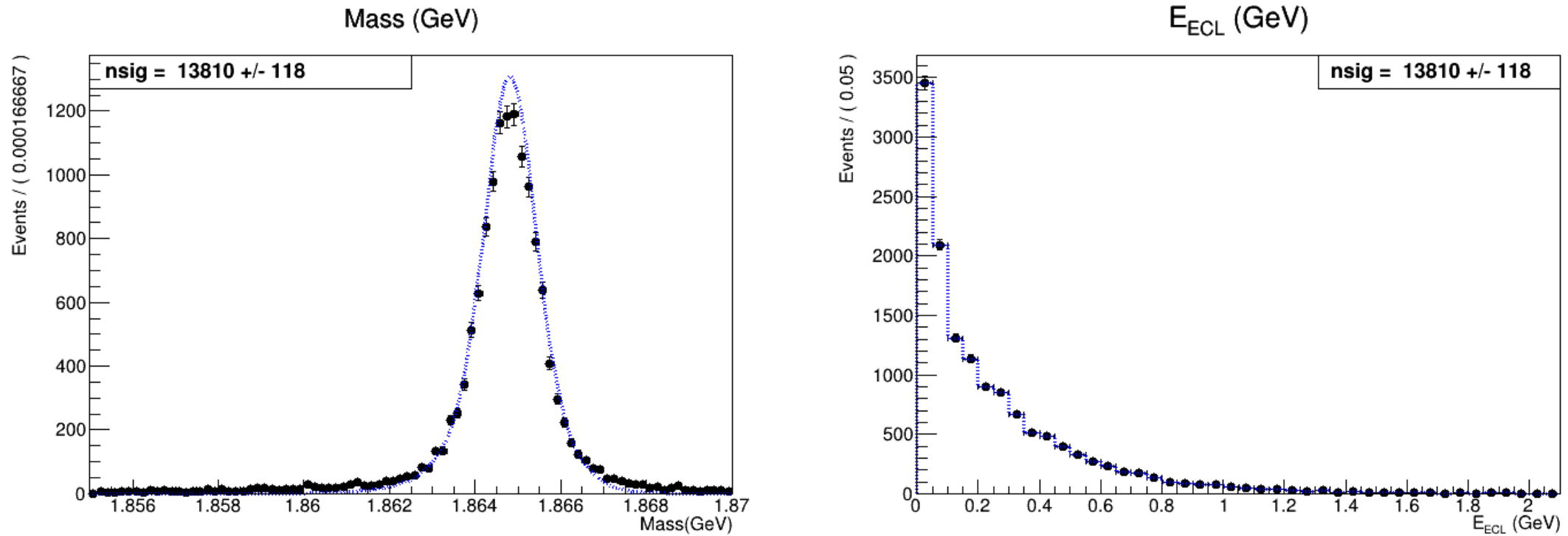
# Extraction of exclusive D on signal MC



Signal efficiency = 0.84404 +/- 0.01140

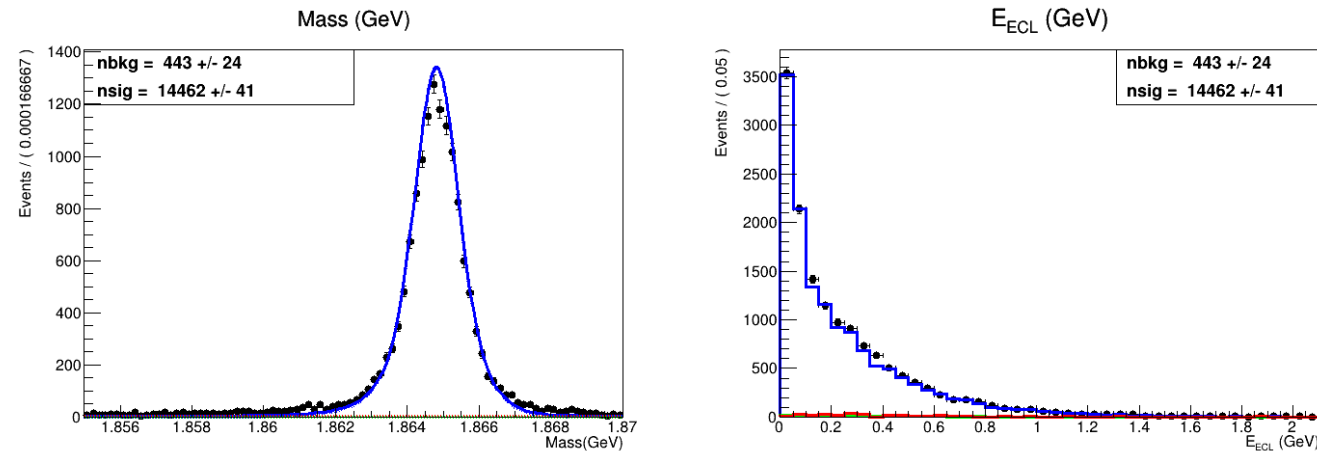


# Extraction of exclusive D on control sample



Signal efficiency = 0.51826 +/- 0.00556

# Measurement of $Br(D^0 \rightarrow K^- \pi^+)$ on generic MC

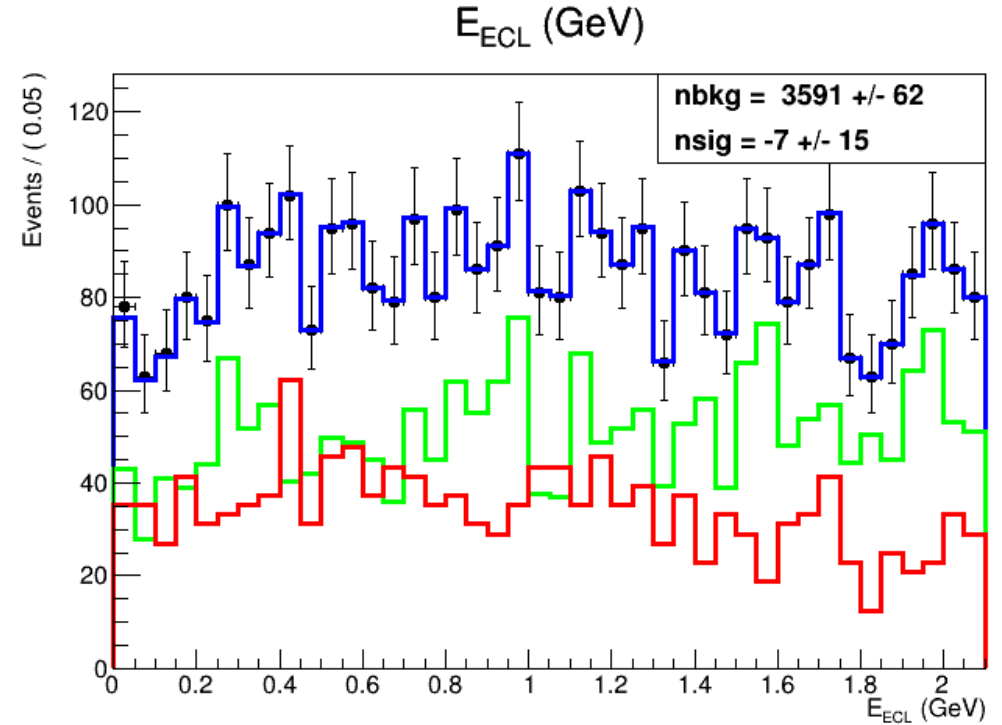
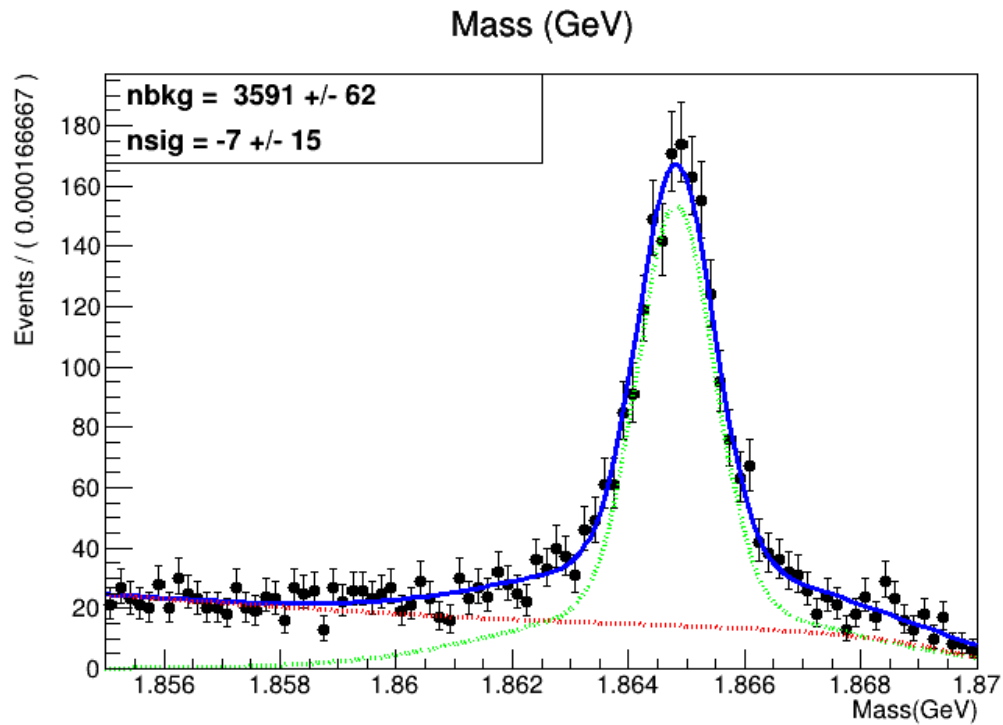


- BF formula :  $Br(D^0 \rightarrow K^- \pi^+) = \frac{N_{exclusive}}{N_{inclusive} * \epsilon_{sig}}$  (pdg value : 0.0395)

- Measurement of BF :

$$Br(D^0 \rightarrow K^- \pi^+) = \frac{14462 \pm 41}{(704597 \pm 1169) * (0.51826 \pm 0.00556)} = 0.039604 \pm 0.000444$$

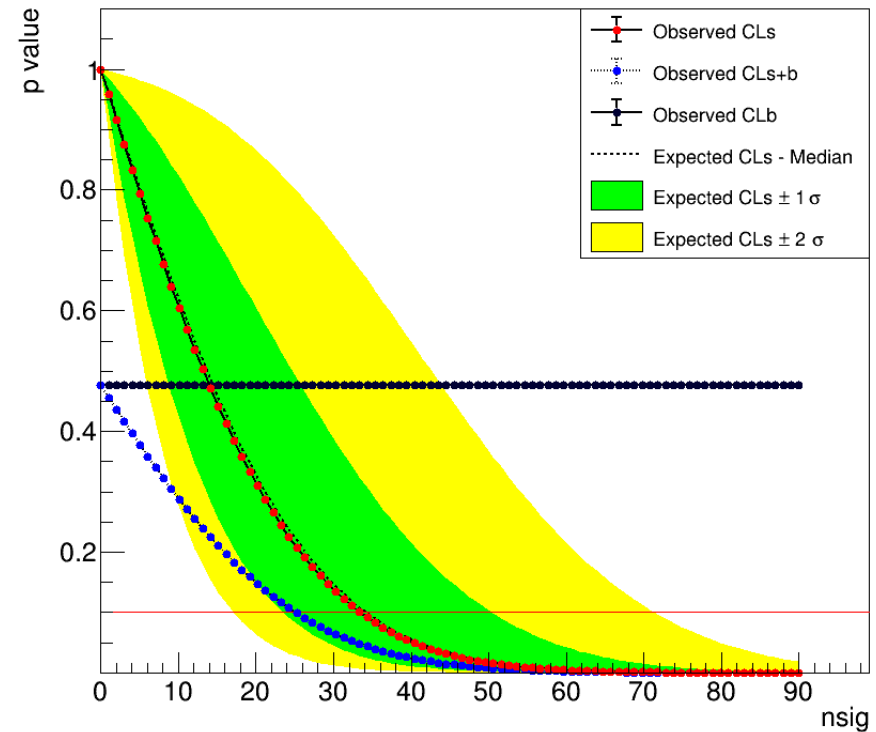
# Extraction of $D^0$ decays to invisible on generic $c\bar{c}$ MC



# Trial to calculate Upper Limit of $D^0$ to invisible on $1 \text{ ab}^{-1}$ generic MC with CLs method

- Systematics are not considered yet...
- $N_{UL} = 34.4444$
- $BR_{UL} = \frac{34.4444}{(704597 * 0.84404)} = 5.62 \times 10^{-5}$

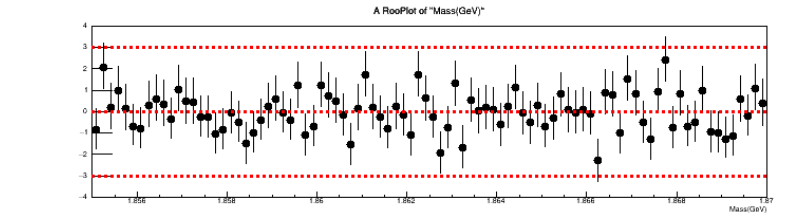
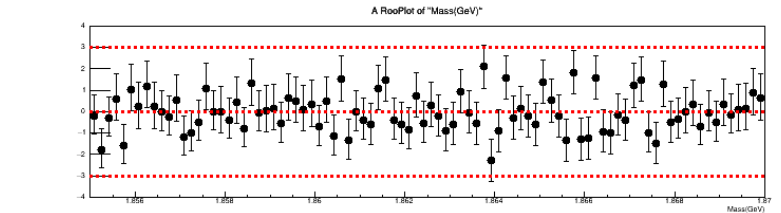
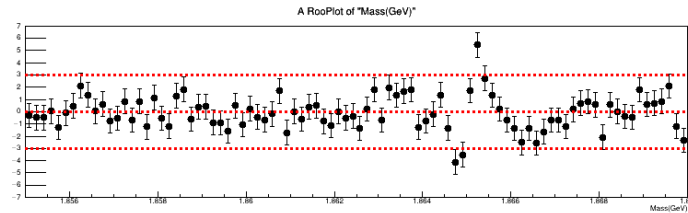
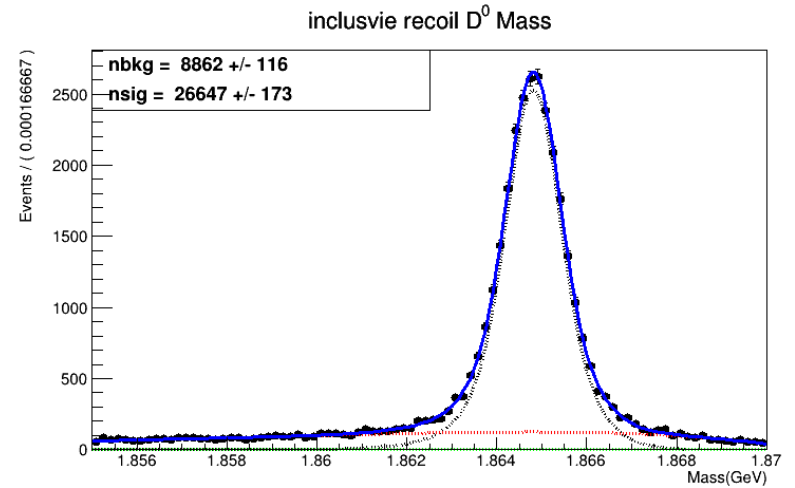
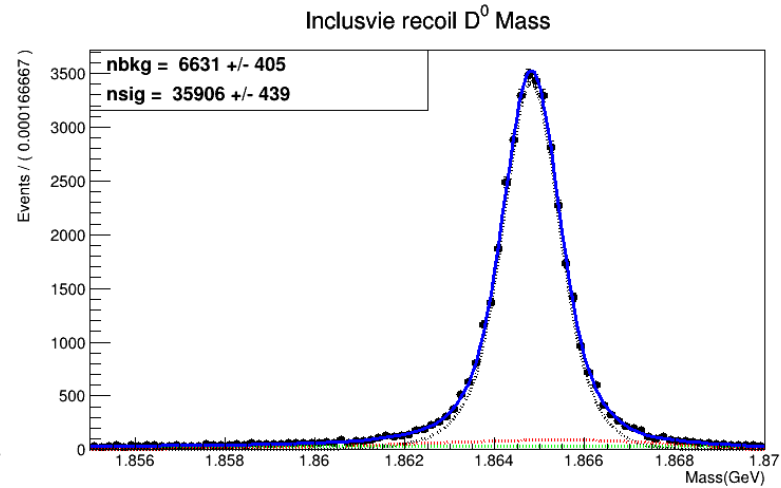
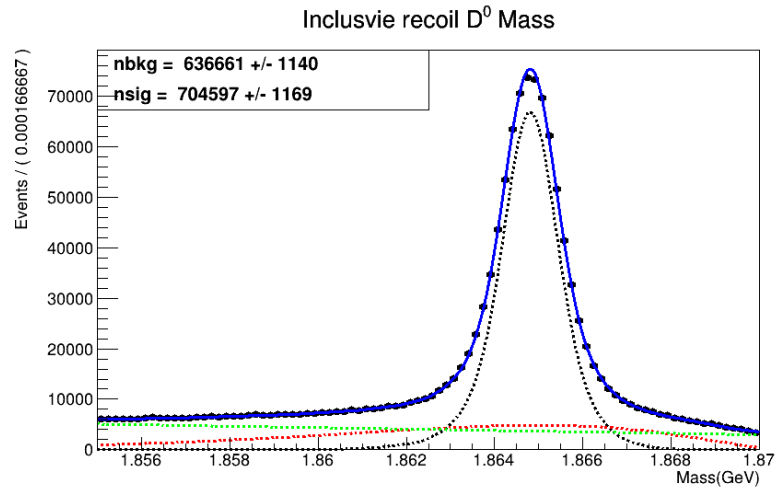
HypoTest Scan Result



# Fitting strategy & check with pull distribution

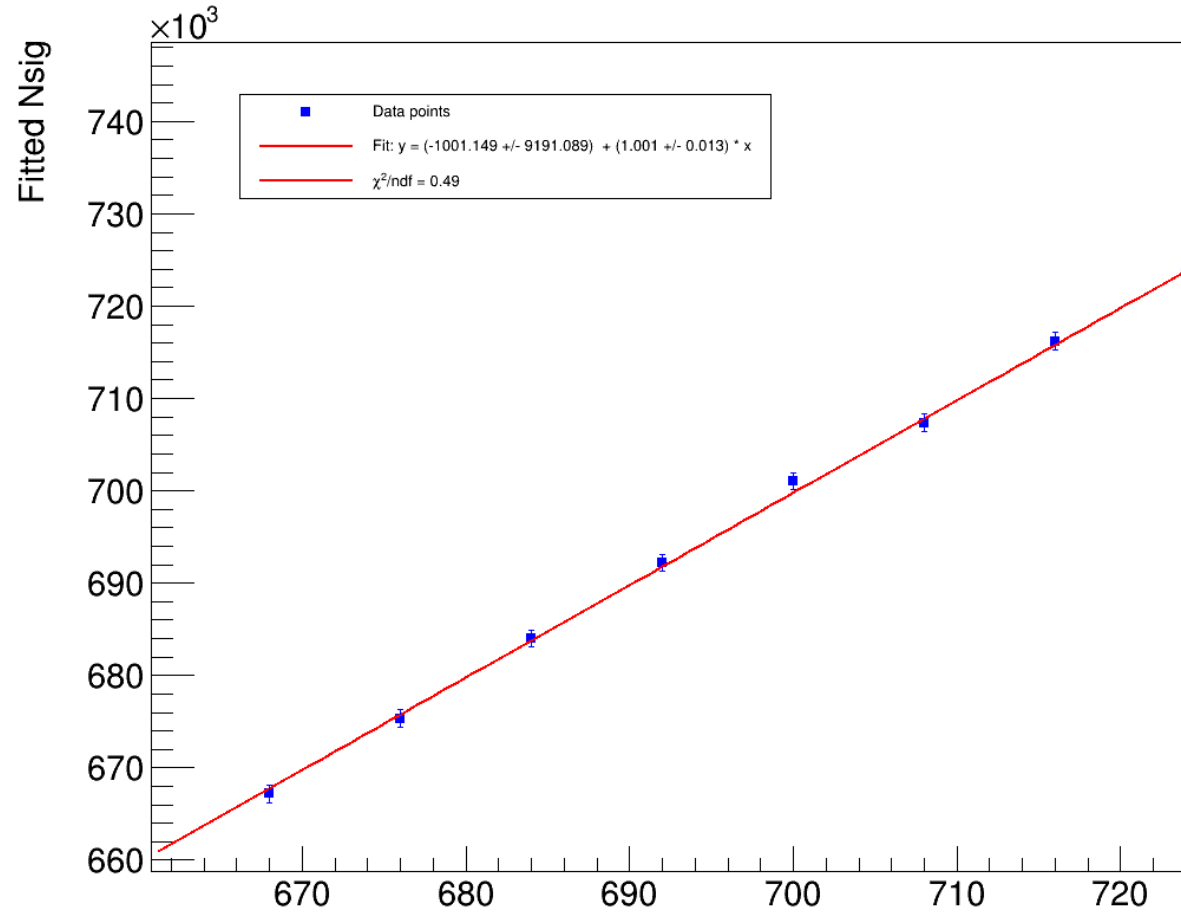
- Inclusive D fitting
  - 1D fitting :  $M_{D^0}$
  - Signal pdf : 2 gaussians + 1 bifurcated gaussian
  - Background pdf : argus + linear
- Exclusive D fitting
  - 2D fitting :  $(M_{D^0}, E_{ECL})$
  - Signal pdf : signal pdf from inclusive D fitting & histogram pdf
  - Background pdf :
    - Flat: Argus + linear & histogram PDF from MC study
    - Peak: 3 gaussians & histogram PDF from MC study

# Fit result with Pull distribution for inclusive D

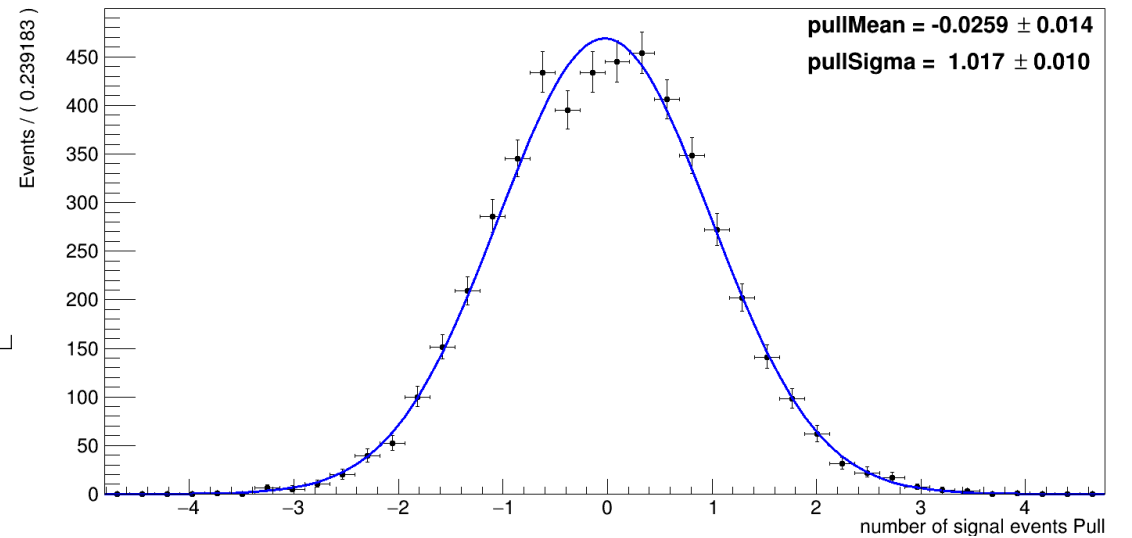


# Inclusive D fit result check with ToyMC on generic MC

## Linearity Test



A RooPlot of "number of signal events Pull"



## Backup : variable a

- The value of a can be roughly estimated
- a is floating number with small range around the estimated value

