

# Signal MC Study

MC matching / isSignal / TopoAna



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Korea

- About this talk
- The **motivation** for the Signal MC study
  - What we reconstruct from the data
  - Possible cases of mis-reconstruction
  - Mathematical Expression of the reconstructed cases
  - Ratios and Distributions of the reconstructed cases
  - Reconstruction Efficiency and its Uncertainty
- **Design flags** for True / WC / SCF
  - Is it possible to design flags for True/Wrong-Comb./Self-Crossfeed with basf2 variable related to “isSignal”?
- **Design “isSignalEvent”**
  - with MC-matching info. / PDG-code
  - Machine learning **label**
- Further: Consider  $\gamma$

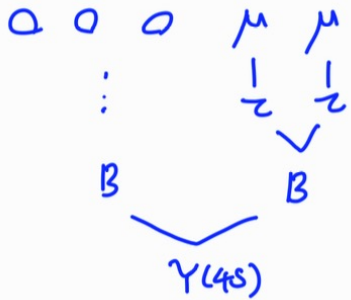
- Others
  - Advertising Code version control / Documentation Tools
  
- Backup
  - Tools for the MC study
    - MC matching
      - MC matching Algorithm
      - isSignal related variables (**Chanho Kim**)
    - TopoAna (**Jaeyoung Kim**)
  - References

# ***About this talk***

- Due to my incomplete understanding
  - Classifying my own questions
  - My own conclusions
    - this can be wrong
- **Conceptual**
- If you don't understand, that might be due to my misunderstanding...
  - **So, let's discuss**

***The motivation  
for the Signal MC study***

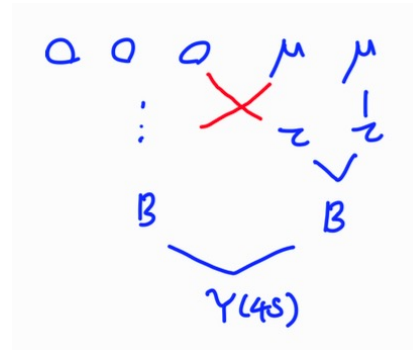
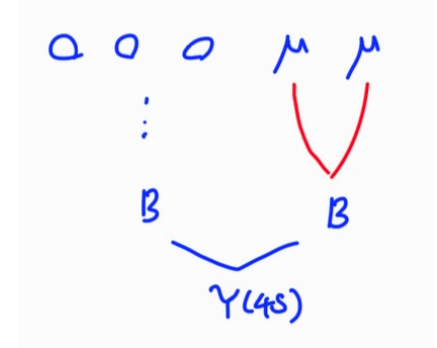
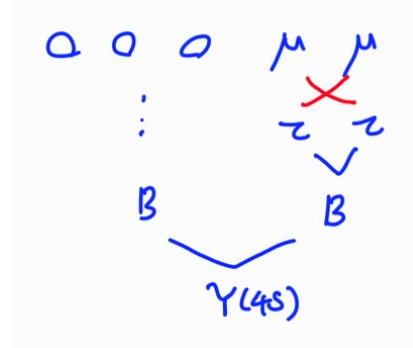
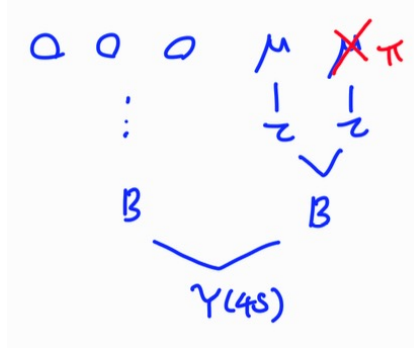
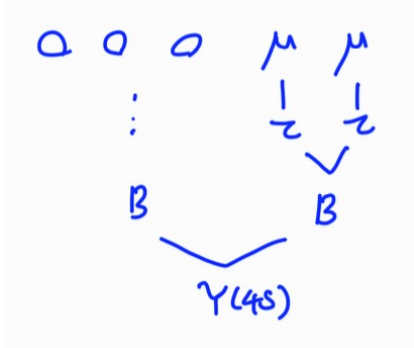
- Think about the final stage of the analysis first
  - Imagine there is no MC-matching study
    - Then,
      - we are not sure ...
      - we cannot distinguish ...
- Example
  - $\Upsilon(4S) \rightarrow \bar{B}^0 B^0$ 
    - $\bar{B}^0 \rightarrow \text{generic}$
    - $B^0 \rightarrow \tau^+ \tau^-$ 
      - $\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau, \tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$



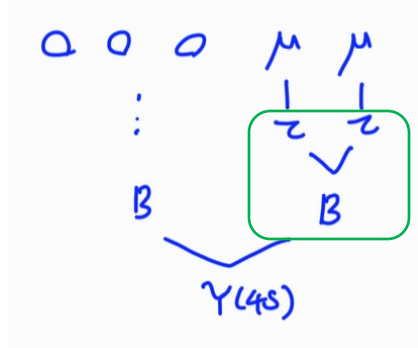
- Let us choose one of the final states, for example,  $\mu\mu$
- $R \equiv R_{\mu\mu}$ : Reconstruction of  $B \rightarrow \tau\tau$  from  $\mu\mu$  final state
- $P(R)$ : Reconstruction Probability of the  $B \rightarrow \tau\tau$  from  $\mu\mu$  final state
- For simplicity, let us assume
  - $P(R^C) = 0$ , no reconstruction failure
  - ( NaN case of isSignal )



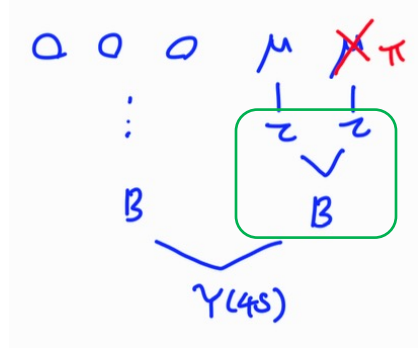
# Possible cases of mis-reconstruction



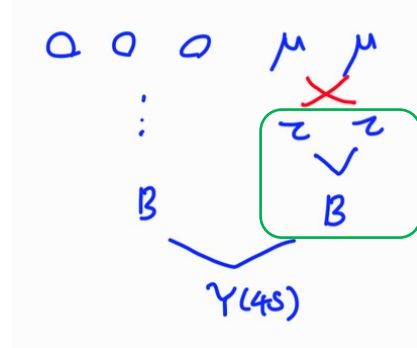
# Possible cases of mis-reconstruction



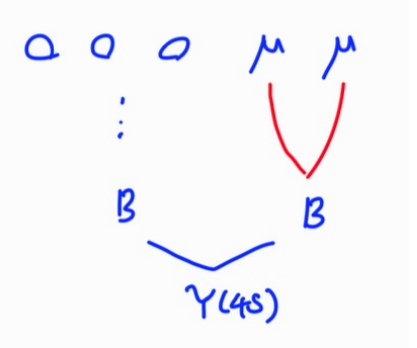
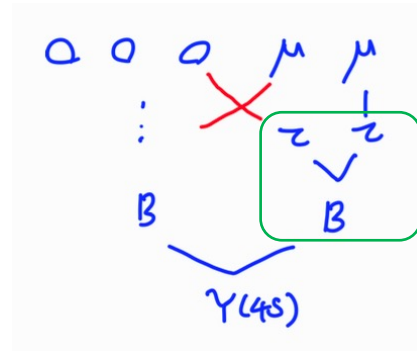
Signal O



Signal O

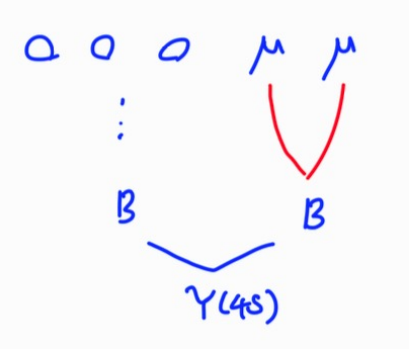
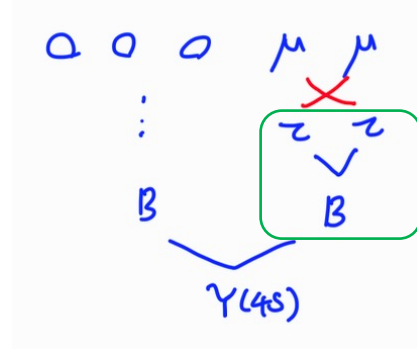
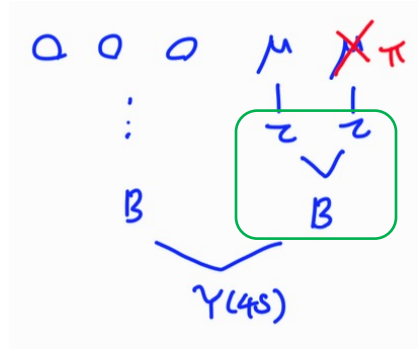
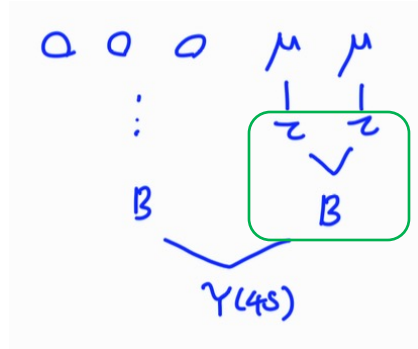


Signal O



Signal X

# Possible cases of mis-reconstruction



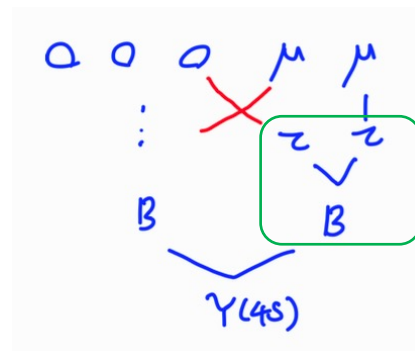
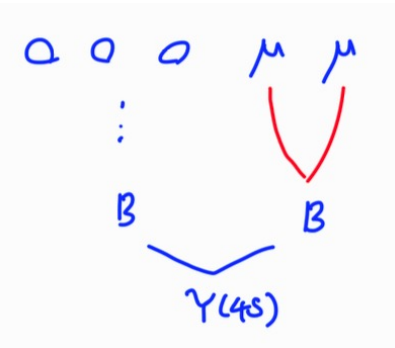
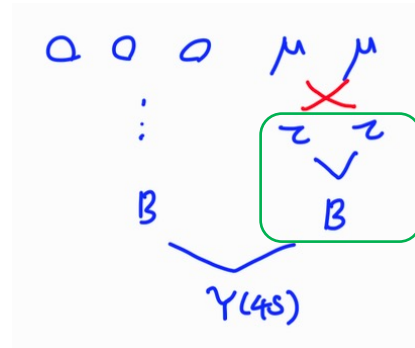
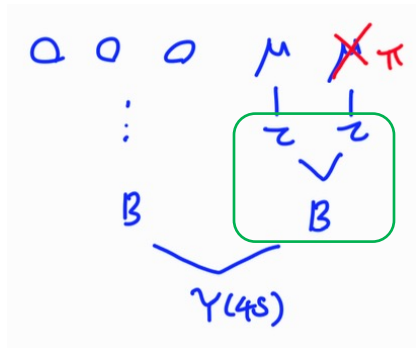
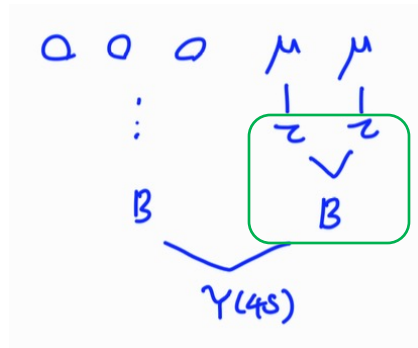
Signal O  
Recon O  
True

Signal O  
Recon X  
Wrong Comb.

Signal O  
Recon X  
Self-Crossfeed

Signal X  
Recon -  
Background

# Possible cases of mis-reconstruction



Signal O

Recon O

True

$P(T|R)$

Signal O

Recon X

Wrong Comb.

$P(WC|R)$

Signal O

Recon X

Self-Crossfeed

$P(SCF|R)$

Signal X

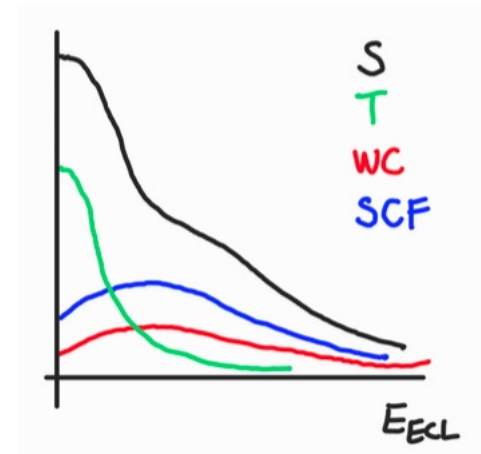
Recon -

Background

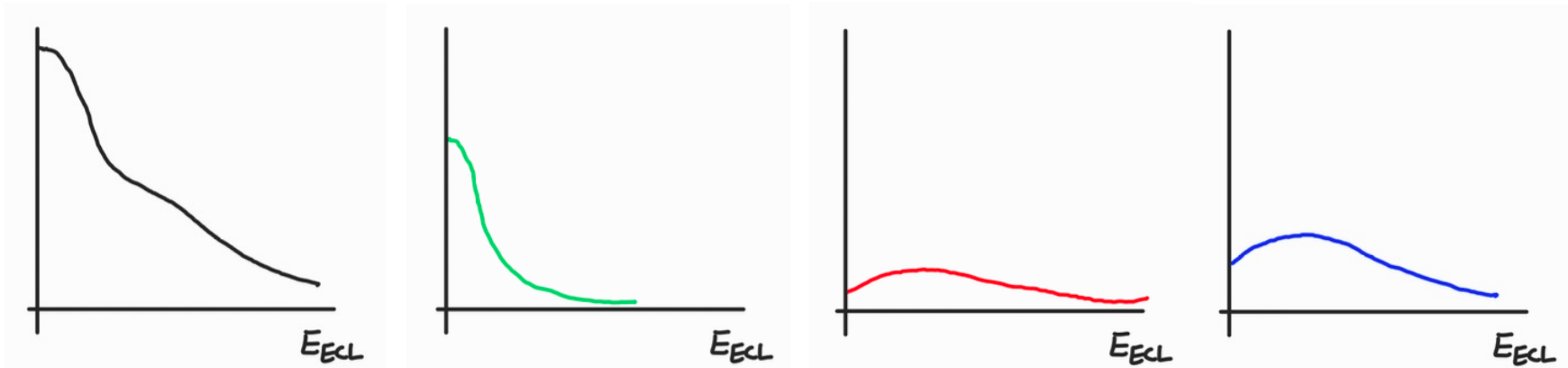
$P(B|R)$

- $P(S|R) = P(T|R) + P(WC|R) + P(SCF|R)$
- $P(S|R) + P(B|R) = P(S \cup B|R) = P(R|R) = 1$
- where,
  - $S$ : Signal
    - $T$ : True
    - $WC$ : Wrong-Combination
    - $SCF$ : Self-Crossfeed
  - $B$ : Background
  - $R \equiv R_{\mu\mu}$ : Reconstruction of  $B \rightarrow \tau\tau$  from  $\mu\mu$  final state
- Assumption: No reconstruction failure (This also should be considered, but for simplicity)
  - $P(R^C) = 0$

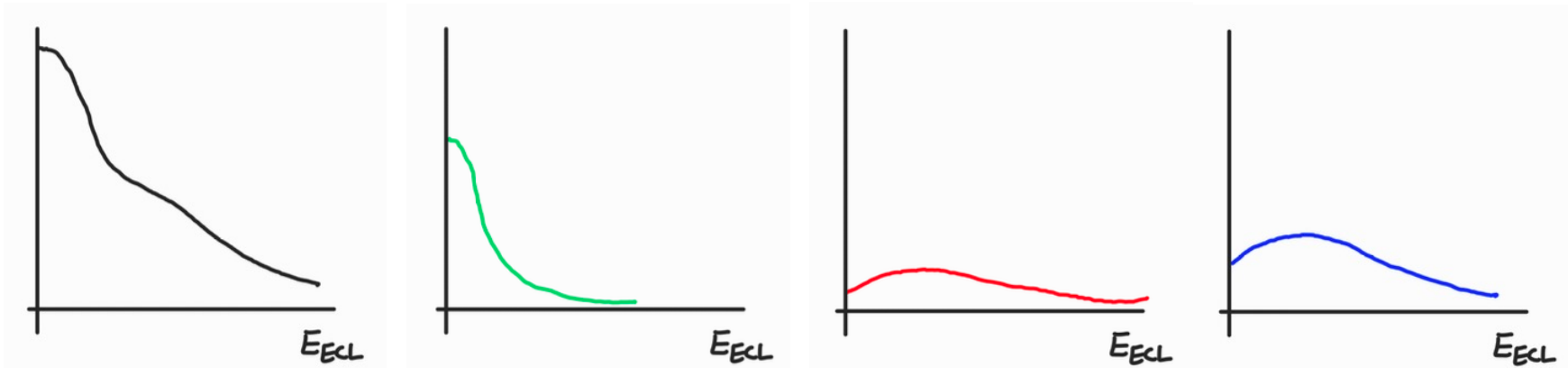
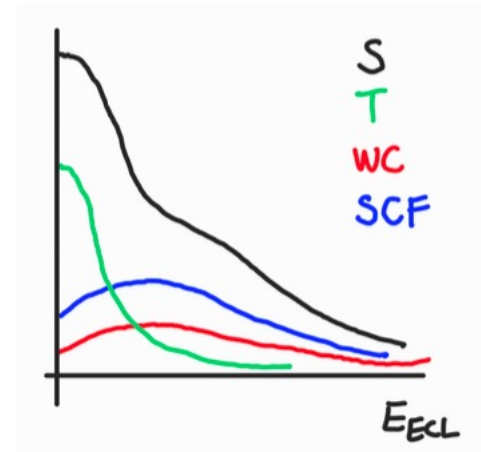
- $P(S|R) = P(T|R) + P(WC|R) + P(SCF|R)$
- Some Analysis  $P(S|R)$  can be approximated as,
  - $P(S|R) \approx P(T|R)$  with negligible  $WC$  and  $SC$
  - $P(S|R) \approx P(T|R) + P(SCF|R)$  with negligible  $WC$
- How can we know the ratios? ( $r_T:r_{WC}:r_{SC}$ )
  - $r_X = \frac{P(X|R)}{P(S|R)}$



- How can we know the distributions?



- $P(S|R) = P(T|R) + P(WC|R) + P(SCF|R)$
- Some Analysis  $P(S|R)$  can be approximated as,
  - $P(S|R) \approx P(T|R)$  with negligible  $WC$  and  $SC$
  - $P(S|R) \approx P(T|R) + P(SCF|R)$  with negligible  $WC$
- How can we know the ratios? ( $r_T:r_{WC}:r_{SC}$ )
  - $r_X = \frac{P(X|R)}{P(S|R)}$
- How can we know the distributions?



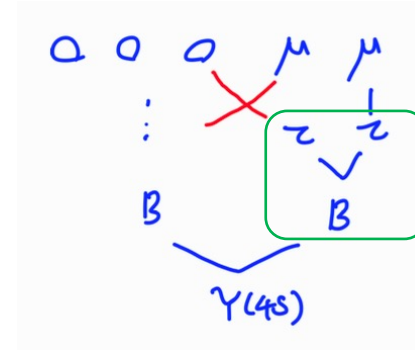
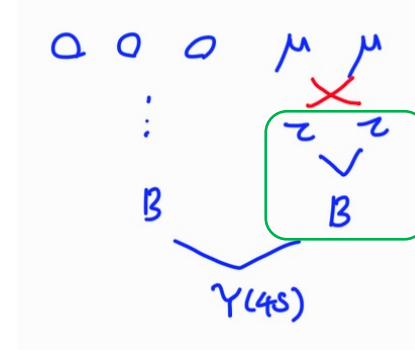
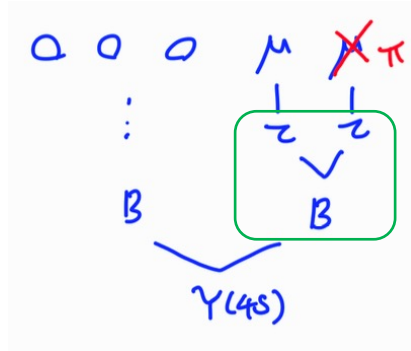
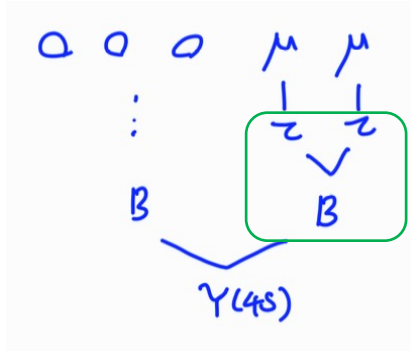
*There is a way to estimate these ratios and distributions!*

**Signal MC study**

- For **example**,
  - all numbers here are arbitrary
- Case 1) WC / SCF negligible
  - $\varepsilon(S = T) = 1 \pm 0.01 \%$
- Case 2) WC negligible, SCF significant
  - $\varepsilon(S = T + SCF) = 1 \pm 0.5 \%$ 
    - SCF worsen the systematic uncertainty (Fit)
  - Fraction is the important factor which affect the uncertainty
    - $f(SCF) = \frac{N_{SCF}}{N_{sig}} = \frac{N_{SCF}}{N_{True} + N_{SCF}} = 23 \%$
    - Thus, it is important to know the fraction and distribution.



***Design Flags  
for True / WC / SCF***

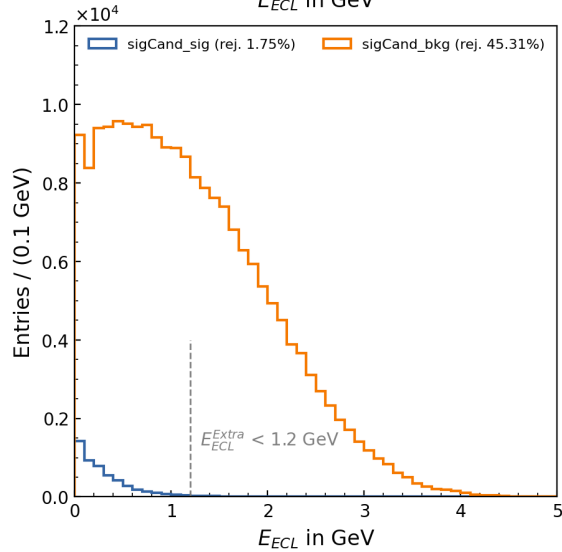
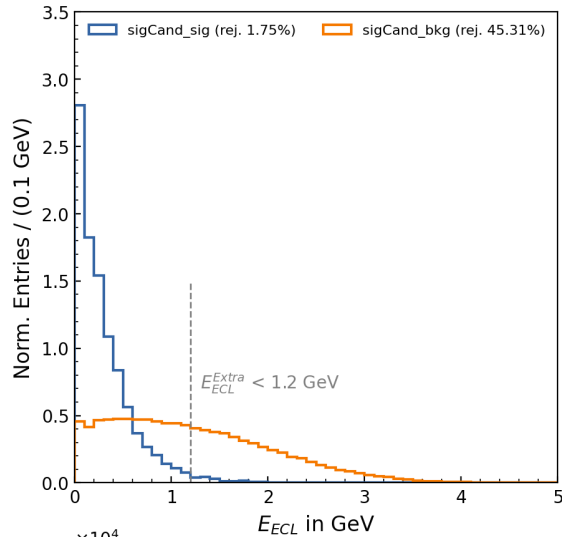


It might be possible as follows?

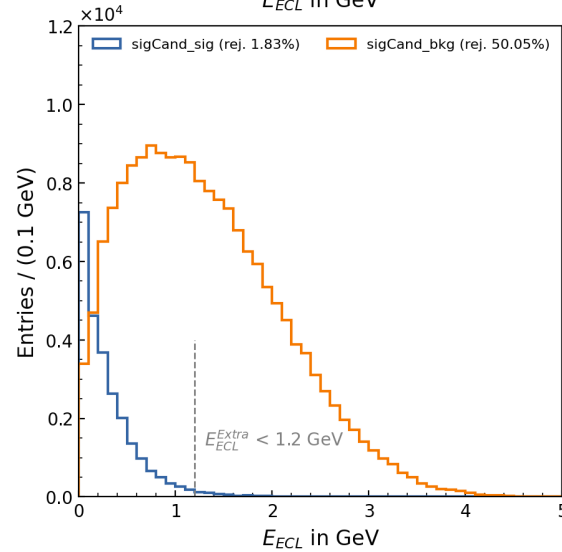
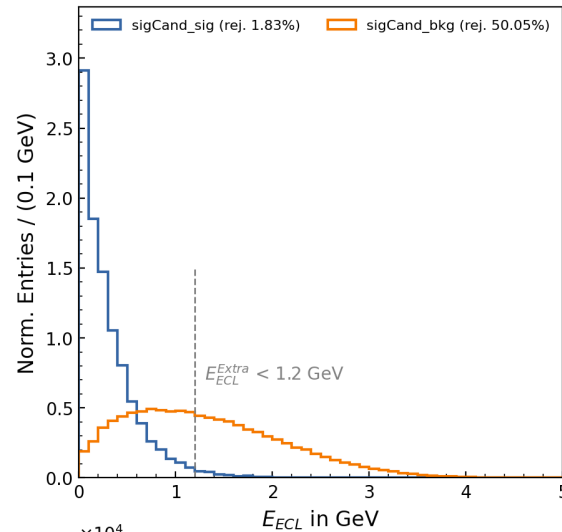
- WC and SCF with combinations of below flags?
  - misID
    - Particle Identification is not correct.
  - AddedWrongParticle
    - Check if the MC-matching is correct for each daughter. If not, the AddedWrongParticle flag is added.

※ [Monte Carlo matching in the Belle II software] <https://doi.org/10.1051/epjconf/202125103021>

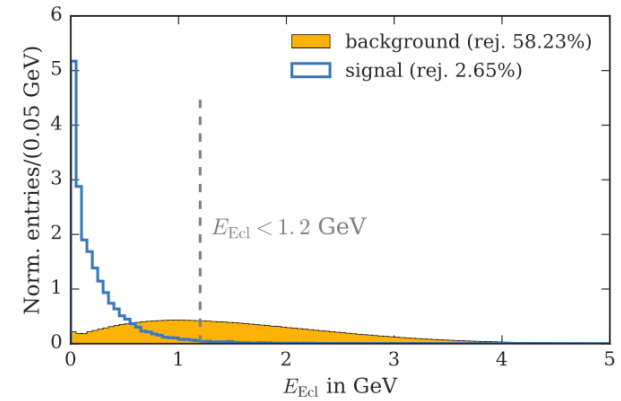
isSignalAccpetMissingNeutrino



isSignalAccpetMissingNeutrinoAndWrongFSPs



Belle



(a) Signal and background  $E_{ECL}$  distributions. Events with  $E_{ECL} < 1.2$  GeV are selected.

- Pre-defined isSignal
  - isSignalAccpetMissingNeutrino
    - “mcErrors == 0” or “mcErrors == 8”
- User-defined isSignal
  - isSignalAccpetMissingNeutrinoAndWrongFSPs
    - “mcErrors == 0” or “mcErrors == 8” or “mcErrors == 128” or “mcErrors == 256”

```
vu.create_isSignal_alias("isSignalAcceptMissingNeutrinoAndWrongFSPs", [8, 128, 256])
```

```
evt_variables = [  
  
    "isSignalAcceptMissingNeutrino",  
    "isSignalAcceptWrongFSPs",  
    "isSignalAcceptMissingNeutrinoAndWrongFSPs",  
    "isContinuumEvent",  
    "isNotContinuumEvent"  
  
]
```

## MC matching error codes

- ▶ calling `matchMCTruth(B+, path)` in one's steering file sets relations between `Particles` and `MCParticles`
  - ▶ recursively matches all daughter particles
  - ▶ bit-wise error flags indicate what went wrong in MC matching (variable `mcErrors`)

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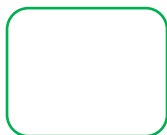
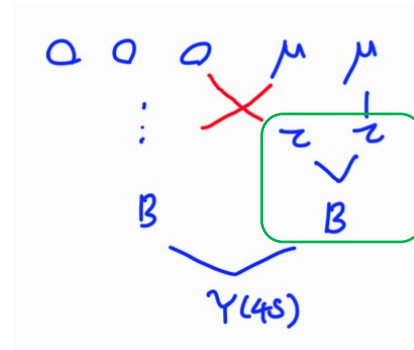
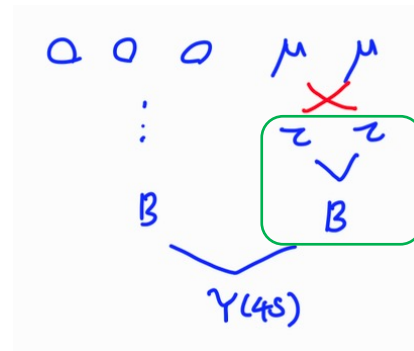
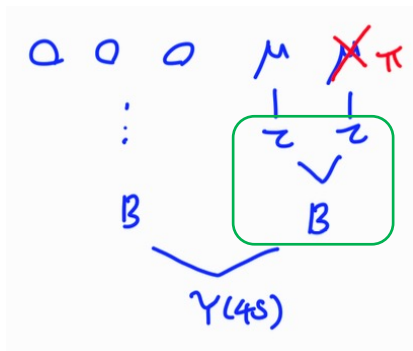
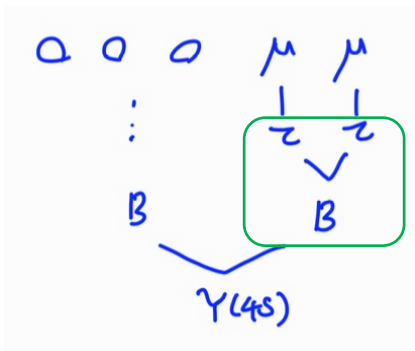
<code>c_Correct = 0</code>	This Particle and all its daughters are perfectly reconstructed.
<code>c_MissFSR = 1</code>	A Final State Radiation (FSR) photon is not reconstructed (based on <code>MCParticle::c_IsFSRPhoton</code> ).
<code>c_MissingResonance = 2</code>	The associated <code>MCParticle</code> decay contained additional non-final-state particles (e.g. a rho) that weren't reconstructed. This is probably O.K. in most cases.
<code>c_DecayInFlight = 4</code>	A Particle was reconstructed from the secondary decay product of the actual particle. This means that a wrong hypothesis was used to reconstruct it, which e.g. for tracks might mean a pion hypothesis was used for a secondary electron.
✓ <code>c_MissNeutrino = 8</code>	A neutrino is missing (not reconstructed).
<code>c_MissGamma = 16</code>	A photon (not FSR) is missing (not reconstructed).
<code>c_MissMassiveParticle = 32</code>	A generated massive FSP is missing (not reconstructed).
<code>c_MissKlong = 64</code>	A Klong is missing (not reconstructed).
✓ <code>c_MisID = 128</code>	One of the charged final state particles is mis-identified (wrong signed PDG code).
✓ <code>c_AddedWrongParticle = 256</code>	A non-FSP Particle has wrong PDG code, meaning one of the daughters (or their daughters) belongs to another Particle.
<code>c_InternalError = 512</code>	No valid match was found. For tracks, it indicates that there is not a true track related to the reconstructed one. Might indicate fake or background track or cluster.
<code>c_MissPHOTOS = 1024</code>	A photon created by PHOTOS was not reconstructed (based on <code>MCParticle::c_IsPHOTOSPhoton</code> ).
<code>c_AddedRecoBremsPhoton = 2048</code>	A photon added with the bremsstrahlung recovery tools ( <code>correctBrems</code> or <code>correctBremsBelle</code> ) has no MC particle assigned, or it doesn't belong to the decay chain of the corrected lepton mother.

---

## isSignal variables

- ▶ convenience aliases for `mcErrors` variable
- ▶ `isSignal`: `mcErrors == 0`
- ▶ `isSignalAcceptMissingNeutrino`: `mcErrors == 0 or mcErrors == 8`
- ▶ `isSignalAcceptMissingGamma`: `mcErrors == 0 or mcErrors == 16`
- ▶ `isSignalAcceptBremsPhotons`: `mcErrors == 0 or mcErrors == 2048`
- ▶ `isSignalAcceptMissingMassive`: `mcErrors ∈ [0, 32, 64, 96]`
- ▶ `isSignalAcceptWrongFSPs`: `mcErrors ∈ [0, 128, 256, 384]`
- ▶ `isSignalAcceptMissing`: `mcErrors ∈ [0, 8, 16, 24, 32, 40, 48, 56, 64, 72, 80, 88, 96, 104, 112, 120]`
- ▶ `create_isSignal_alias(aliasName, flags)`
  - ▶ `create_isSignal_alias("isSignalAcceptMissingNeutrinoAndMissingGamma", [8, 16]):`  
`mcErrors ∈ [0, 8, 16, 24]`
- ▶ three possible return values: 0, 1, and NaN
  - ▶ isSignal variables can not be used as booleans
  - ▶ NaN if no MC partner found (running on data or `matchMCTruth` not run or fake tracks / cluster)

***Design “isSignalEvent”***

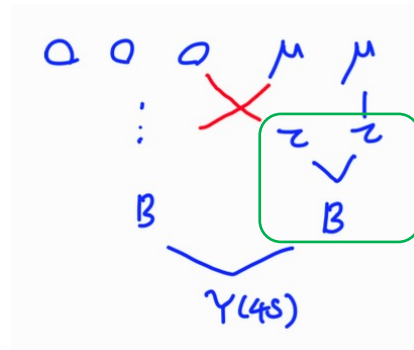
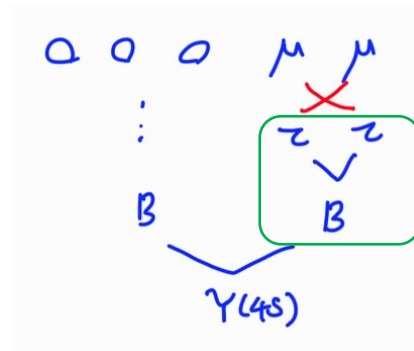
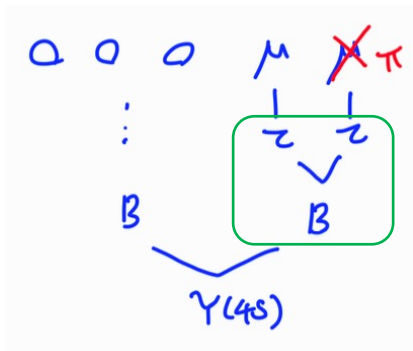
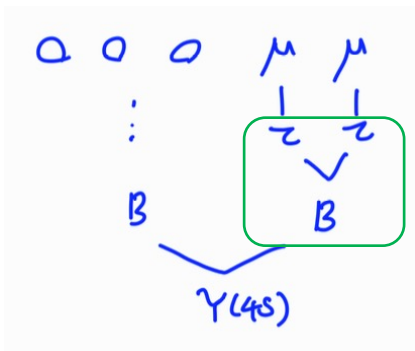


$P(S|R)$

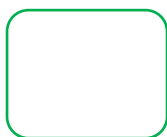
Make a flag as 1 (True), if this green box matches

- Condition 0. Check whether the right PDG code
- Condition 1. Only sister  $\tau$  (with the right PDG code)
- Condition 2. Mother  $B$  (with the right PDG code)





I think this flag can be the training flag.



$$P(S|R)$$

- Make a flag as 1 (True), if this green box matches
- Condition 0. Check whether the right PDG code
  - Condition 1. Only sister  $\tau$  (with the right PDG code)
  - Condition 2. Mother  $B$  (with the right PDG code)

- p15, line 210: “The signal is truth-matched [24].”
  - [24]: “*The truth-matching of the B+ candidate is as follows: the candidate should have a kaon daughter and 2 neutrinos.* Potential radiative photons are also accepted.”

## 6. INPUT VARIABLES

In this section, variables that are used in the training of the main classifier are defined and shown. A sample of  $8 \times 10^5$  events of each simulated category (signal,  $B^+B^-$ ,  $B^0\bar{B}^0$ ,  $u\bar{u}$ ,  $d\bar{d}$ ,  $s\bar{s}$ ,  $c\bar{c}$ ,  $\tau^+\tau^-$ ) is reconstructed with the event selection described in the previous section apart from the requirement on the KaonPID (unless specified differently).

The signal is truth-matched [24]. Furthermore, additional weights are applied on the signal events to correct the phase space of the decay products as the MC was generated assuming on a three-body decay of the signal B. This procedure is described in detail in Appendix F The background samples are stacked with weights taking into account the cross-section of the process and the reconstruction efficiency. Both the signal and the stacked background histograms are normalized to unity and the signal-background separation power is estimated with the Jensen-Shannon distance [7], that gives 0 (1) for perfectly matching (diverging) histograms. Moreover, data taken during the Run 3123 from Experiment 8 is overlaid (randomly chosen from the list of ‘good’ runs).

All histograms are framed by colored boxes as some of the considered input variables are excluded from the training of the BDT:

※ [“Studies of  $B^\pm \rightarrow K^\pm \nu \bar{\nu}$  decay using inclusive tagging method” by Filippo Dattola]  
<https://docs.belle2.org/record/2003>

```
47 class IsSignalEvent(b2.Module):
48     """
49     define extraInfo isSignalEvent, that is set to true if, checking MC info:
50     one of the B mesons has a son with the right PDG-ID, its mother is a B+ or B0 (depending of its charge)
51     and its only sisters are a nu and an anti-nu)
52     """
```

```
45 class IsSignalEvent(b2.Module):
46     """
47     define extraInfo isSignalEvent, that is set to true if, checking MC info:
48     one of the B mesons has a son with the right PDG-ID, its mother is a B+ or B0 (depending of its charge)
49     and its only sisters are a tau+ and a tau-)
50     """
```

※ [ $B \rightarrow K\nu\nu$  Analysis Code by Giulio Dujany]

[https://gitlab.desy.de/giulio.dujany/b2knn/-/blob/main/ntupliser/ntuple\\_variables.py](https://gitlab.desy.de/giulio.dujany/b2knn/-/blob/main/ntupliser/ntuple_variables.py)

※ [ $B \rightarrow K\tau\tau$  Analysis Code by Stefano Moneta]

[https://gitlab.desy.de/stefano.moneta/btokst\\_tau\\_tau/-/blob/main/ntupliser/ntuple\\_variables.py](https://gitlab.desy.de/stefano.moneta/btokst_tau_tau/-/blob/main/ntupliser/ntuple_variables.py)

# "isSignalEvent" Example ( $B^+ \rightarrow K^+ \nu \bar{\nu}$ )

```
47 class IsSignalEvent(b2.Module):
48     """
49     define extraInfo isSignalEvent, that is set to true if, checking MC info:
50     one of the B mesons has a son with the right PDG-ID, its mother is a B+ or B0 (depending of its charge)
51     and its only sisters are a nu and an anti-nu
52     """
53
54     def __init__(self, listname, varname="isSignalEvent"):
55         super().__init__()
56         self.particleList = r.Belle2.PyStoreObj(listname)
57         self.varname = varname
58
59     def event(self):
60         mcParticles = r.Belle2.PyStoreArray("MCParticles")
61         KaonsPDGids = [
62             321,
63             310,
64             323,
65             313,
66             130,
67             311,
68             10311,
69             10321,
70             100311,
71             100321,
72             10313,
73             10323,
74             20313,
75             20323,
76             100313,
77             100323,
78             30313,
79             30323,
80             315,
81             325,
82             10315,
83             10325,
84             20315,
85             20325,
86             317,
87             327,
88             319,
89             329,
90         ]
91         Knunu_generic = []
92         KJpsi_generic = []
93         for a in KaonsPDGids:
94             for b in [12, 14, 16]: # here are the neutrinos!!!
95                 Knunu_generic.append(sorted([a, b, -b]))
96                 KJpsi_generic.append(sorted([-a, b, -b]))
```

```
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```

```
if sorted(
    list(
        filter(
            lambda x: x != 22,
            [abs(h.getPDG()) for h in j.getDaughters()],
        )
    ) == [211, 310]:
    for k in j.getDaughters():
        if k.getPDG() == 310:
            if sorted(
                list(
                    filter(
                        lambda x: x != 22,
                        [
                            m.getPDG()
                            for m in k.getDaughters()
                        ],
                    )
                ) == [-211, 211]:
                particle.setExtraInfo(self.varname, 4)
if sorted(
    list(
        filter(
            lambda x: x != 22,
            [abs(h.getPDG()) for h in j.getDaughters()],
        )
    ) == [211, 311]:
    for k in j.getDaughters():
        if (
            k.getPDG() == 311
            and k.getDaughter(0).getPDG() == 310
        ):
            if sorted(
                list(
                    filter(
                        lambda x: x != 22,
                        [
                            m.getPDG()
                            for m in k.getDaughter(
                                0
                            ).getDaughters()
                        ],
                    )
                ) == [-211, 211]:
                particle.setExtraInfo(self.varname, 4)
elif abs(j.getPDG()) == 313:
    if sorted(
        list(
            filter(
                lambda x: x != 22,
                [abs(h.getPDG()) for h in j.getDaughters()],
            )
        ) == [211, 321]:
        particle.setExtraInfo(self.varname, 5)
```

※ [  $B \rightarrow K \nu \nu$  Analysis Code by Giulio Dujany ]

[https://gitlab.desy.de/giulio.dujany/b2knn/-/blob/main/ntupliser/ntuple\\_variables.py](https://gitlab.desy.de/giulio.dujany/b2knn/-/blob/main/ntupliser/ntuple_variables.py)

```
class IsSignalEvent(b2.Module):
    """
    define extraInfo isSignalEvent, that is set to true if, checking MC info:
    one of the B mesons has a son with the right PDG-ID, its mother is a B+ or B0 (depending of its charge)
    and its only sisters are a tau+ and a tau-
    """

    def __init__(self, listname, varname="isSignalEvent"):
        super().__init__()
        self.particleList = ROOT.Belle2.PyStoreObj(listname)
        self.varname = varname

    def event(self):
        mcParticles = ROOT.Belle2.PyStoreArray("MCParticles")
        KaonsPDGids = [323, 313]
        Ktautau_generic = []
        for KaonPDGid in KaonsPDGids:
            Ktautau_generic.append(sorted([[KaonPDGid,15,-15]]))
            Ktautau_generic.append(sorted([-KaonPDGid,15,-15]))
        for particle in self.particleList:
            if particle.hasExtraInfo(self.varname):
                continue
            particle.addExtraInfo(self.varname, 0)
            mcParticle = False
            for Upscand in mcParticles:
                if Upscand.getPDG() == 300553:
                    mcParticle = Upscand
                    break
            if not mcParticle:
                continue
            B_sons_PDGids = []
            for i in mcParticle.getDaughters():
                if abs(i.getPDG()) != 521 and abs(i.getPDG()) != 511 :
                    continue
                B_sons_PDGids.append(sorted(list(filter(lambda x: x!= 22,[j.getPDG() for j in i.getDaughters()])))
            for B_son_PDGids in B_sons_PDGids :
                if B_son_PDGids in Ktautau_generic :
                    particle.setExtraInfo(self.varname, -1)
                else:
                    continue
            for i in mcParticle.getDaughters(): #loop on Bs
                sons_PDGids = sorted(list(filter(lambda x: x!= 22,[j.getPDG() for j in i.getDaughters()])))
                if sons_PDGids in Ktautau_generic: # then we know its K tau tau
                    for j in i.getDaughters():
                        if abs(j.getPDG()) == 313: # K*0 -> K- pi+
                            if sorted(list(filter(lambda x: x!= 22,[abs(h.getPDG()) for h in j.getDaughters()]))) == [211,321]:
                                particle.setExtraInfo(self.varname, 1)
```

※ [B → Kττ Analysis Code by Stefano Moneta]

[https://gitlab.desy.de/stefano.moneta/btokst\\_tau\\_tau/-/blob/main/ntupliser/ntuple\\_variables.py](https://gitlab.desy.de/stefano.moneta/btokst_tau_tau/-/blob/main/ntupliser/ntuple_variables.py)

```

12 class IsB2Xnnu(b2.Module):
13     """
14     define extraInfo isB2Xnnu, that is set to true if, checking MC info:
15     X has the right PDG-ID, its mother is a B+ or B0 (depending of its charge)
16     and its only sisters are a nu_e and an anti-nu_e
17     """
18
19     def __init__(self, listname, varname="isB2Xnnu"):
20         super().__init__()
21         self.particleList = r.Belle2.PyStoreObj(listname)
22         self.varname = varname
23
24     def event(self):
25         mcParticles = r.Belle2.PyStoreArray("MCParticles")
26         for particle in self.particleList:
27             if particle.hasExtraInfo(self.varname):
28                 continue
29             particle.addExtraInfo(self.varname, 0)
30             mcParticle = particle.getRelatedTo("MCParticles")
31             if not mcParticle:
32                 continue
33             mcMother = mcParticle.getMother()
34             if not mcMother:
35                 continue
36             B_PDG = 511 if particle.getCharge() == 0 else 521
37             if abs(mcMother.getPDG()) != B_PDG:
38                 continue
39             if mcMother.getCharge() != particle.getCharge():
40                 continue
41             daughters_PDGs = sorted([i.getPDG() for i in mcMother.getDaughters()])
42             if daughters_PDGs != sorted([particle.getPDGCode(), -12, 12]):
43                 continue
44             particle.setExtraInfo(self.varname, 1)

```

※ [ $B \rightarrow K \nu \nu$  Analysis Code by Giulio Dujany]

[https://gitlab.desy.de/giulio.dujany/b2knn/-/blob/main/ntupliser/ntuple\\_variables.py](https://gitlab.desy.de/giulio.dujany/b2knn/-/blob/main/ntupliser/ntuple_variables.py)

```
class IsB2Xtautau(b2.Module):
    """
    define extraInfo isB2Xtautau, that is set to true if, checking MC info:
    X has the right PDG-ID, its mother is a B+ or B0 (depending of its charge)
    and its only sisters are a tau+ and a tau-
    """

    def __init__(self, listname, varname="isB2Xtautau"):
        super().__init__()
        self.particleList = ROOT.Belle2.PyStoreObj(listname)
        self.varname = varname

    def event(self):
        mcParticles = ROOT.Belle2.PyStoreArray("MCParticles")
        for particle in self.particleList:
            if particle.hasExtraInfo(self.varname):
                continue
            particle.addExtraInfo(self.varname, 0)
            mcParticle = particle.getRelatedTo("MCParticles")
            if not mcParticle:
                continue
            mcMother = mcParticle.getMother()
            if not mcMother:
                continue
            B_PDG = 511 if particle.getCharge() == 0 else 521
            if abs(mcMother.getPDG()) != B_PDG:
                continue
            if mcMother.getCharge() != particle.getCharge():
                continue
            daughters_PDGs = sorted([i.getPDG() for i in mcMother.getDaughters()])
            if daughters_PDGs != sorted([particle.getPDGCode(), -15, 15]):
                continue
            particle.setExtraInfo(self.varname, 1)
```

※ [ $B \rightarrow K\tau\tau$  Analysis Code by Stefano Moneta]

[https://gitlab.desy.de/stefano.moneta/btokst\\_tau\\_tau/-/blob/main/ntupliser/ntuple\\_variables.py](https://gitlab.desy.de/stefano.moneta/btokst_tau_tau/-/blob/main/ntupliser/ntuple_variables.py)

***Further: Consider  $\gamma$***



- p15, line 210: “The signal is truth-matched [24].”
  - [24]: “The truth-matching of the B<sup>+</sup> candidate is as follows: the candidate should have a kaon daughter and 2 neutrinos. **Potential radiative photons are also accepted.**”

## 6. INPUT VARIABLES

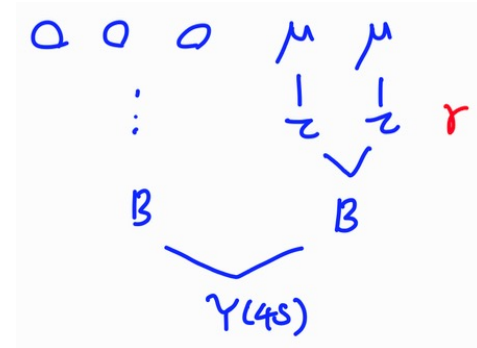
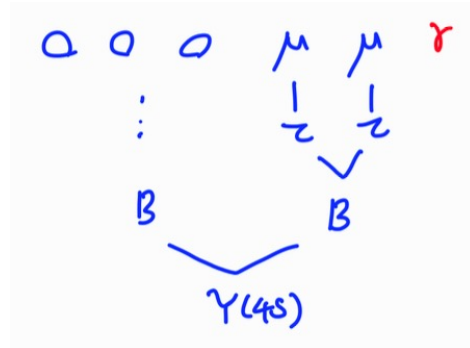
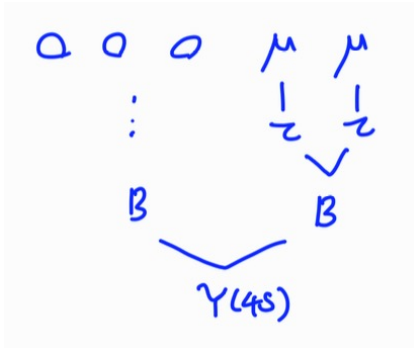
In this section, variables that are used in the training of the main classifier are defined and shown. A sample of  $8 \times 10^5$  events of each simulated category (signal,  $B^+B^-$ ,  $B^0\bar{B}^0$ ,  $u\bar{u}$ ,  $d\bar{d}$ ,  $s\bar{s}$ ,  $c\bar{c}$ ,  $\tau^+\tau^-$ ) is reconstructed with the event selection described in the previous section apart from the requirement on the KaonPID (unless specified differently).

The signal is truth-matched [24]. Furthermore, additional weights are applied on the signal events to correct the phase space of the decay products as the MC was generated assuming on a three-body decay of the signal B. This procedure is described in detail in Appendix F The background samples are stacked with weights taking into account the cross-section of the process and the reconstruction efficiency. Both the signal and the stacked background histograms are normalized to unity and the signal-background separation power is estimated with the Jensen-Shannon distance [7], that gives 0 (1) for perfectly matching (diverging) histograms. Moreover, data taken during the Run 3123 from Experiment 8 is overlaid (randomly chosen from the list of ‘good’ runs).

All histograms are framed by colored boxes as some of the considered input variables are excluded from the training of the BDT:

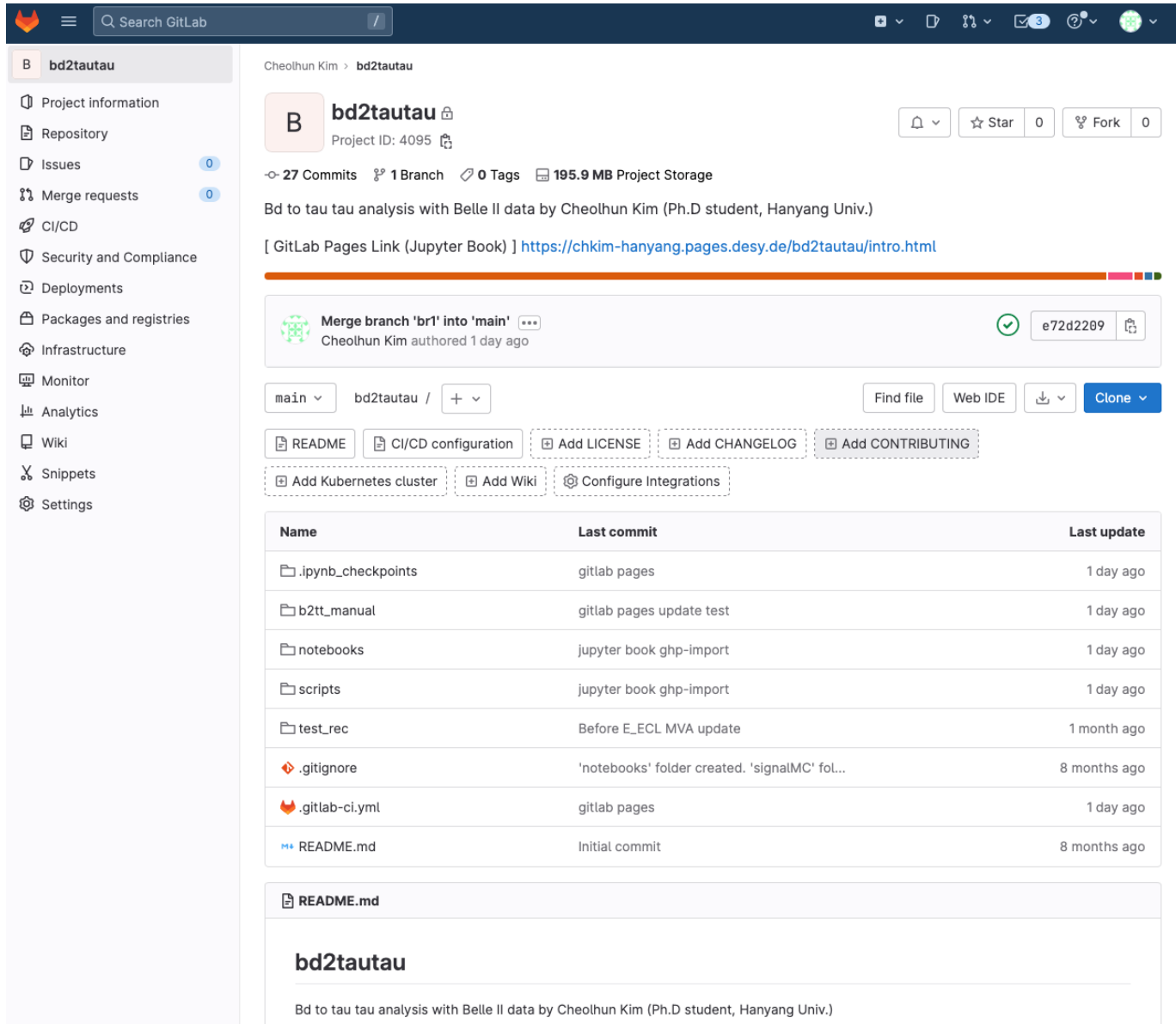
※ [“Studies of  $B^\pm \rightarrow K^\pm \nu \bar{\nu}$  decay using inclusive tagging method” by Filippo Dattola]  
<https://docs.belle2.org/record/2003>

# Consider $\gamma$



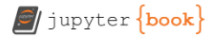
***Others:***  
***Code Version Control***  
***and Documentation***

- Gitlab
  - Belle II uses “Gitlab” as git repository
  - My repository
    - <https://gitlab.desy.de/chkim-hanyang/bd2tautau>
- Jupyter book
  - Python-based documentation package
    - Markdown format
    - Comparability with Sphinx
    - HTML output
  - My documentation online page with “Gitlab Pages”
    - <https://chkim-hanyang.pages.desy.de/bd2tautau/intro.html>
  - This will be a supplementary of my Belle II note



The screenshot shows the GitLab interface for a repository named 'bd2tautau'. The left sidebar contains navigation options like 'Project information', 'Repository', 'Issues', 'Merge requests', 'CI/CD', 'Security and Compliance', 'Deployments', 'Packages and registries', 'Infrastructure', 'Monitor', 'Analytics', 'Wiki', 'Snippets', and 'Settings'. The main content area displays the repository name, project ID (4095), and statistics (27 Commits, 1 Branch, 0 Tags, 195.9 MB Project Storage). A description reads: 'Bd to tau tau analysis with Belle II data by Cheolhun Kim (Ph.D student, Hanyang Univ.)'. A link to the GitLab Pages (Jupyter Book) is provided: <https://chkim-hanyang.pages.desy.de/bd2tautau/intro.html>. A recent merge commit is shown: 'Merge branch 'br1' into 'main'' by Cheolhun Kim, authored 1 day ago, with commit hash e72d2209. Below this, there are buttons for 'Find file', 'Web IDE', 'Clone', and a list of repository files with their last commit details.

Name	Last commit	Last update
.ipynb_checkpoints	gitlab pages	1 day ago
b2tt_manual	gitlab pages update test	1 day ago
notebooks	jupyter book ghp-import	1 day ago
scripts	jupyter book ghp-import	1 day ago
test_rec	Before E_ECL MVA update	1 month ago
.gitignore	'notebooks' folder created. 'signalMC' fol...	8 months ago
.gitlab-ci.yml	gitlab pages	1 day ago
README.md	Initial commit	8 months ago



[Bd to tau tau Analysis](#)

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## Sample Information

Sample Information

## Reconstruction

FEI Tagging

Pre-selection

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Commands

Version Control

Jupyter Book



Contents

Title  
Author  
Abstract  
keywords

# Bd to tau tau Analysis

## Title

Search for the rare decay  $B^0 \rightarrow \tau^+ \tau^-$  at Belle II experiment

## Author

Cheolhun Kim, Hanyang University [hun4341@hanyang.ac.kr](mailto:hun4341@hanyang.ac.kr)

## Abstract

A search for the rare decay  $B^0 \rightarrow \tau^+ \tau^-$  is performed at the Belle II experiment at the superKEKB asymmetric electron-positron collider. The standard model predicts that the branching fraction of the decay mode is suppressed, but several extensions of the standard model expect enhancements. The results will be obtained with data samples corresponding to an integrated luminosity of  $427.79 \text{ fb}^{-1}$  collected at the  $\Upsilon(4S)$  resonance. We use a hadronic tagging method that reconstructs fully accompanying B meson and try to find signals from the remaining part of the event. The result of this study will be the measurement or upper limit setting of the branching fraction of the decay. We present the results based on Monte Carlo simulation samples.

## keywords

Rare Decay, Hadronic Tagging, Leptonic, Belle II Experiment

Next  
[Theory](#) >

By Cheolhun Kim  
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***Backup***



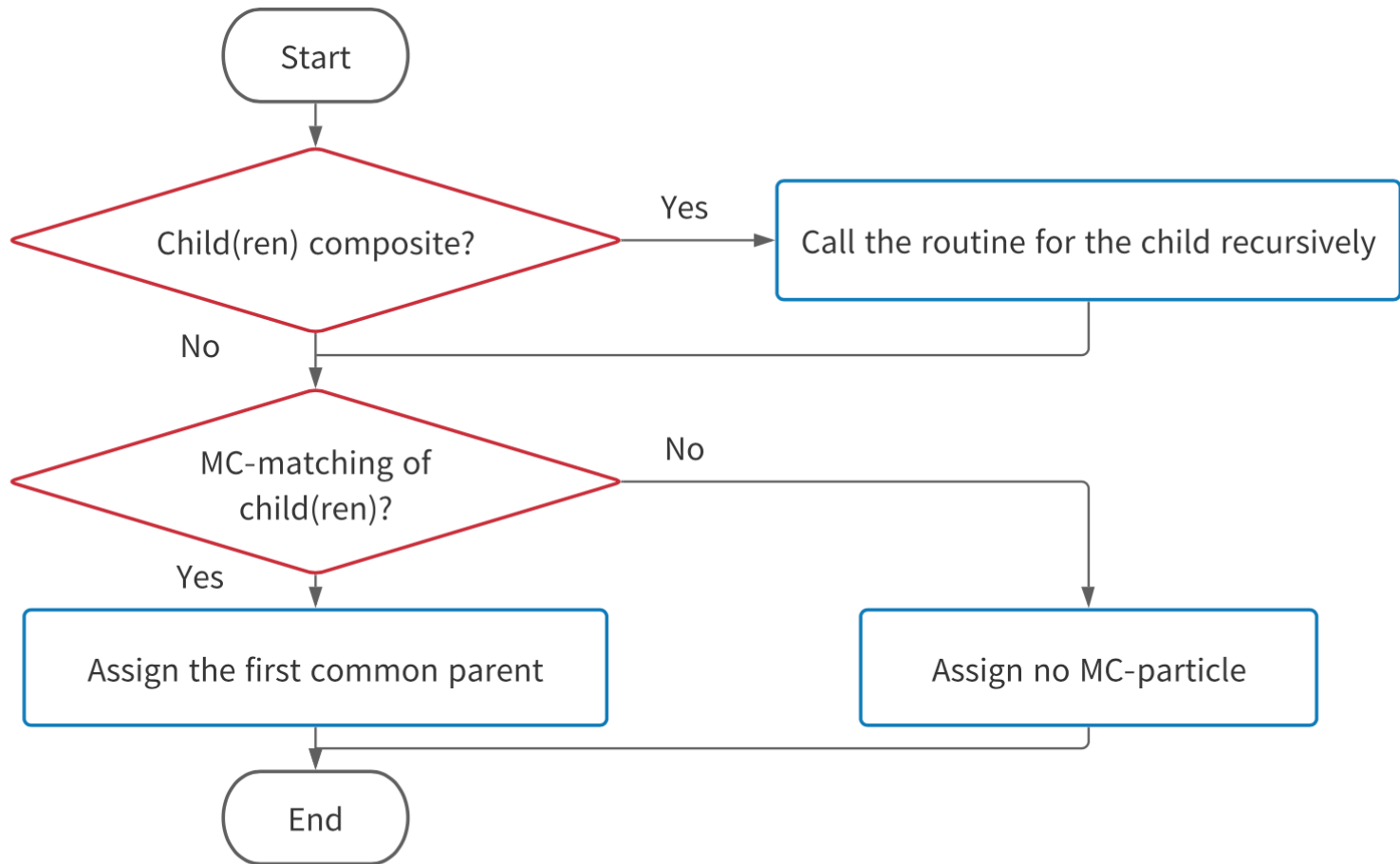


- Tools for the MC study
- References

# *Tools for the MC study*

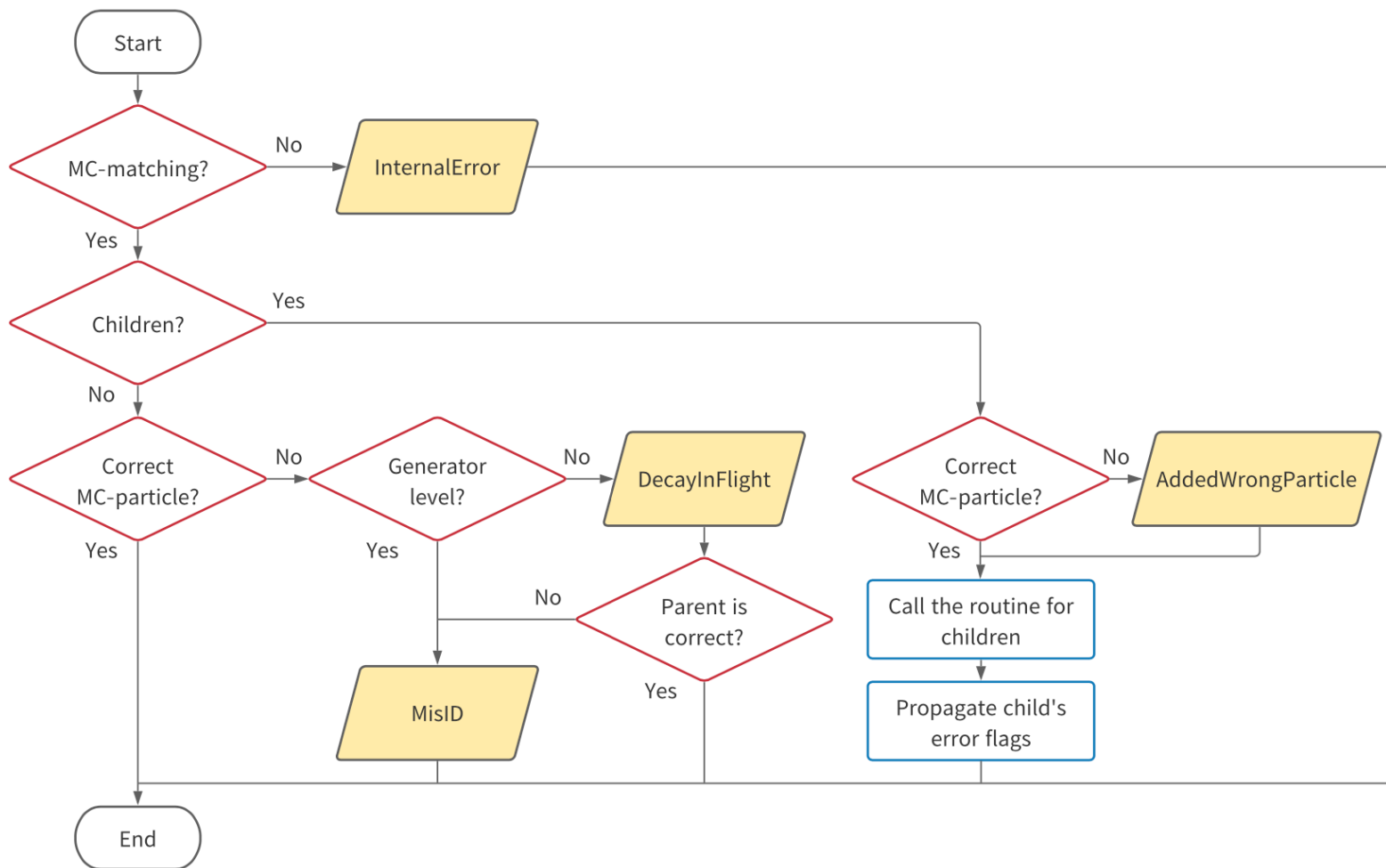
- MC matching?
  - Particle Candidates: Combinations of **reconstructed** objects
  - **Simulated** Particles: From the **event generators**
- Purpose of MC matching?
  - To study **Detector effects, analysis backgrounds, and efficiencies**
  - To consider the **reconstruction effect and backgrounds**
- MC matching of tracks / MC matching of clusters
  - Track-based and Cluster-based particles (final-state particles) candidates
- “MC matching algorithm for Composite particles”
  - Goal: To establish the relation between the **reconstructed composite particle** and the **corresponding MC-particle**
- Evaluation algorithm for the “MC matching algorithm for Composite particles”
  - Categorizing failure cases: Several Error flags
  - **“Each analyst can CHOOSE to accept or not for his or her own analysis use case”**
  - Two major parts of the algorithm
    - Processes with **existing particles**
    - Processes with **missing particles**

※ [Monte Carlo matching in the Belle II software] <https://doi.org/10.1051/epjconf/202125103021>



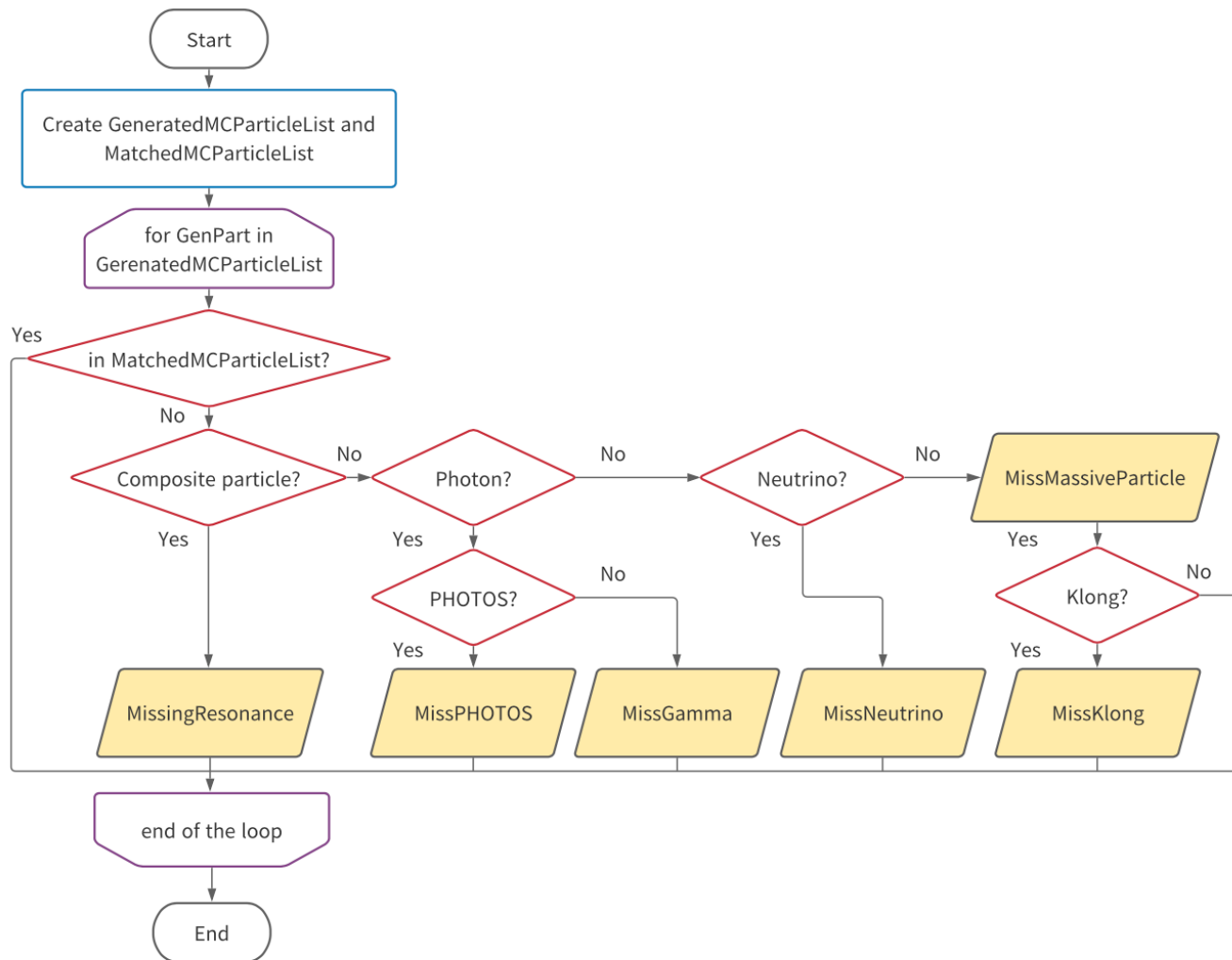
**Figure 1.** The algorithm flowchart of the MC-matching for a composite particle.

※ [Monte Carlo matching in the Belle II software] <https://doi.org/10.1051/epiconf/202125103021>



**Figure 2.** The algorithm flowchart of the evaluation for existing particles

※ [Monte Carlo matching in the Belle II software] <https://doi.org/10.1051/epjconf/202125103021>



**Figure 3.** The algorithm flowchart of the evaluation for missing particles

※ [Monte Carlo matching in the Belle II software] <https://doi.org/10.1051/epjconf/202125103021>

※ *Chanho Kim will cover this part in detail.*

## MC matching

- ▶ MC matching useful to
  - ▶ optimize selection requirements, *e.g.* label training data for MVAs
  - ▶ calculate signal efficiencies
  - ▶ study background sources
- ▶ two steps
  1. relate mdst dataobjects (**Track**, **ECLCluster**, **KLMCluster**) with **MCParticle** (with weights)
  2. relate reconstructed particles with MC particles
- ▶ interpretation of MC matches necessary

※ [All you wanted to know about brems correction and MC matching and never dared asking, Belle II Physics Meeting]

<https://indico.belle2.org/event/8674/#42-all-you-wanted-to-know-about>

## MC matching error codes

- ▶ calling `matchMCTruth(B+, path)` in one's steering file sets relations between `Particles` and `MCParticles`
  - ▶ recursively matches all daughter particles
  - ▶ bit-wise error flags indicate what went wrong in MC matching (variable `mcErrors`)

---

<code>c_Correct = 0</code>	This Particle and all its daughters are perfectly reconstructed.
<code>c_MissFSR = 1</code>	A Final State Radiation (FSR) photon is not reconstructed (based on <code>MCParticle::c_IsFSRPhoton</code> ).
<code>c_MissingResonance = 2</code>	The associated <code>MCParticle</code> decay contained additional non-final-state particles (e.g. a rho) that weren't reconstructed. This is probably O.K. in most cases.
<code>c_DecayInFlight = 4</code>	A Particle was reconstructed from the secondary decay product of the actual particle. This means that a wrong hypothesis was used to reconstruct it, which e.g. for tracks might mean a pion hypothesis was used for a secondary electron.
<code>c_MissNeutrino = 8</code>	A neutrino is missing (not reconstructed).
<code>c_MissGamma = 16</code>	A photon (not FSR) is missing (not reconstructed).
<code>c_MissMassiveParticle = 32</code>	A generated massive FSP is missing (not reconstructed).
<code>c_MissKlong = 64</code>	A Klong is missing (not reconstructed).
<code>c_MisID = 128</code>	One of the charged final state particles is mis-identified (wrong signed PDG code).
<code>c_AddedWrongParticle = 256</code>	A non-FSP Particle has wrong PDG code, meaning one of the daughters (or their daughters) belongs to another Particle.
<code>c_InternalError = 512</code>	No valid match was found. For tracks, it indicates that there is not a true track related to the reconstructed one. Might indicate fake or background track or cluster.
<code>c_MissPHOTOS = 1024</code>	A photon created by PHOTOS was not reconstructed (based on <code>MCParticle::c_IsPHOTOSPhoton</code> ).
<code>c_AddedRecoBremsPhoton = 2048</code>	A photon added with the bremsstrahlung recovery tools ( <code>correctBrems</code> or <code>correctBremsBelle</code> ) has no MC particle assigned, or it doesn't belong to the decay chain of the corrected lepton mother.

---



## isSignal variables

- ▶ convenience aliases for `mcErrors` variable
- ▶ `isSignal`: `mcErrors == 0`
- ▶ `isSignalAcceptMissingNeutrino`: `mcErrors == 0 or mcErrors == 8`
- ▶ `isSignalAcceptMissingGamma`: `mcErrors == 0 or mcErrors == 16`
- ▶ `isSignalAcceptBremsPhotons`: `mcErrors == 0 or mcErrors == 2048`
- ▶ `isSignalAcceptMissingMassive`: `mcErrors ∈ [0, 32, 64, 96]`
- ▶ `isSignalAcceptWrongFSPs`: `mcErrors ∈ [0, 128, 256, 384]`
- ▶ `isSignalAcceptMissing`: `mcErrors ∈ [0, 8, 16, 24, 32, 40, 48, 56, 64, 72, 80, 88, 96, 104, 112, 120]`
- ▶ `create_isSignal_alias(aliasName, flags)`
  - ▶ `create_isSignal_alias("isSignalAcceptMissingNeutrinoAndMissingGamma", [8, 16]):`  
`mcErrors ∈ [0, 8, 16, 24]`
- ▶ three possible return values: 0, 1, and NaN
  - ▶ isSignal variables can not be used as booleans
  - ▶ NaN if no MC partner found (running on data or `matchMCTruth` not run or fake tracks / cluster)

## Decay strings

- ▶ MC matching interpretation configured via decay arrow, markers, and keywords
- ▶ four different allowed arrow types
  - ▶ `->` decays via intermediate resonances and / or with radiative photons are counted as signal
  - ▶ `=norad=>` if in actual decay photon was radiated it is **not** counted as signal; intermediate resonances do not have to be specified
  - ▶ `=direct=>` if actual decay proceeds via intermediate resonance it is **not** counted as signal; decays with radiative photons are counted as signal
  - ▶ `=exact=>` intermediate resonances and radiative photons have to be specified explicitly, otherwise decay is not counted as signal
- ▶ different arrows allowed in same decay string `D*+ -> [D0 =direct=> K- pi+ pi0] pi+`
- ▶ example:
  - ▶ generated decay:  $B^+ \rightarrow J/\psi K^+$  with  $J/\psi \rightarrow e^+e^-$  and final state photon
  - ▶ `B+:default -> K+ e+ e-`  $\Rightarrow$  `isSignal == 1`
  - ▶ `B+:noFSR =norad=> K+ e+ e-`  $\Rightarrow$  `isSignal == 0` and `mcErrors == 1`
  - ▶ `B+:nores =direct=> K+ e+ e-`  $\Rightarrow$  `isSignal == 0` and `mcErrors == 2`
  - ▶ `B+:exact =exact=> K+ e+ e-`  $\Rightarrow$  `isSignal == 0` and `mcErrors == 3`

## Decay string marker and keywords

- ▶ `@` marked (composite) particle can be any particle and decay is still counted as signal
- ▶ `(misID)` marked (final state) particle can be other particle type and decay is still counted as signal
- ▶ `(decay)` decay in flight of marked particle counted as signal, *e.g.*  $\pi \rightarrow \mu\nu_\mu$
- ▶ `@`, `(misID)`, and `(decay)` have to be placed in front of particle
- ▶ `...` even if there are more massive final state particles than specified, decay is counted as signal (`isSignal` behaves like `isSignalAcceptMissingMassive`)
  - ▶ missing  $\pi^0$  are not counted as signal
- ▶ `?nu` neutrinos are ignored in MC matching (`isSignal` works like `isSignalAcceptMissingNeutrino`)
- ▶ `?adbbrems` Bremsstrahlung correction photons are ignored in MC matching (`isSignal` works like `isSignalAcceptBremsPhotons`)
- ▶ `?gamma` missing photon(s) are ignored in MC matching (`isSignal` works like `isSignalAcceptMissingGamma`)
- ▶ `...`, `?nu`, `?adbbrems`, and `?gamma` have to be placed at the end of the decay string

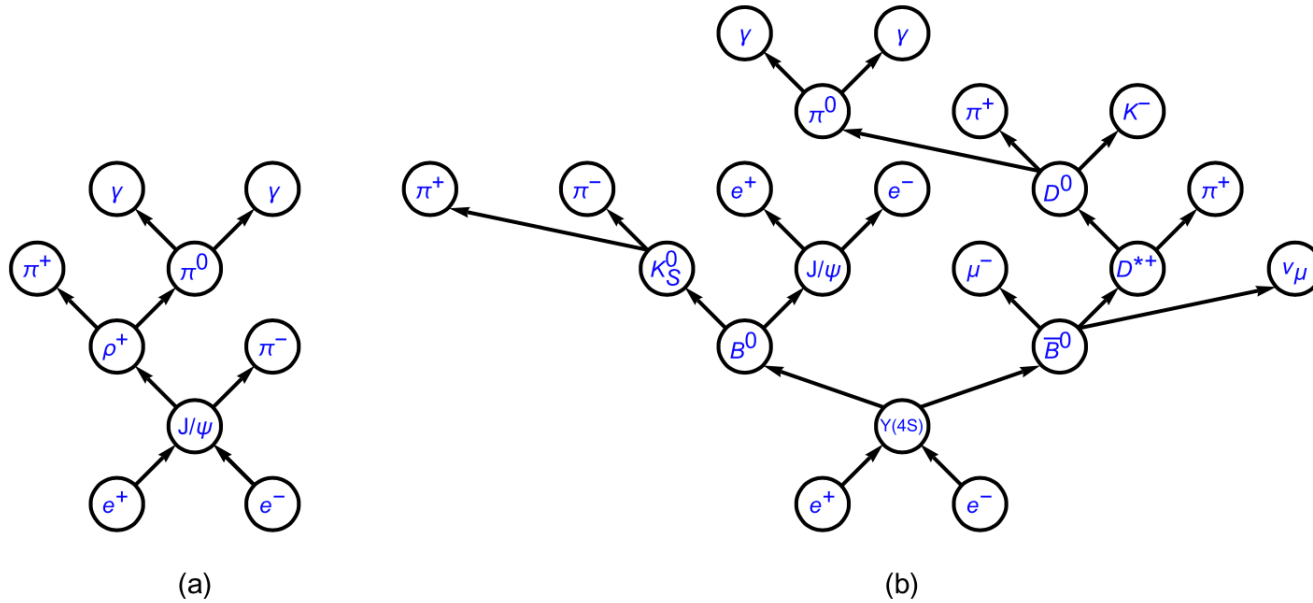
※ *Special thanks to Jaeyoung Kim. He teaches me how to use the TopoAna package.*

※ *He will cover “TopoAna”.*

- Before TopoAna package (ex: Belle)
  - Analysts usually wrote some **private codes** to match a **few** signals and/or backgrounds for their own studies.
  - The limited functions of these codes do not satisfy the increasing demands for topology analysis.
- Motivation
  - A generic, powerful, and easy-to-use program is required for the topology analysis
- History
  - TopoAna is developed for **BESIII** ( $\tau$ -Charm energy region)
  - Extended to Belle II (already applied to some analysis in Belle)
- Main usage
  - One can figure out the main backgrounds (especially peaking ones)
  - Optimize the selection criteria

※ [TopoAna: A generic tool for the event type analysis of inclusive Monte-Carlo samples in high energy physics experiments]

<https://www.sciencedirect.com/science/article/pii/S0010465520302575?via%3Dihub>



**Fig. 1.** Topology diagrams of (a)  $e^+e^- \rightarrow J/\psi, J/\psi \rightarrow \rho^+\pi^-, \rho^+ \rightarrow \pi^+\pi^0, \pi^0 \rightarrow \gamma\gamma$  and (b)  $e^+e^- \rightarrow \Upsilon(4S), \Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow K_S^0 J/\psi, \bar{B}^0 \rightarrow \mu^- D^{*+} \nu_\mu, K_S^0 \rightarrow \pi^+\pi^-, J/\psi \rightarrow e^+e^-, D^{*+} \rightarrow D^0\pi^+, D^0 \rightarrow \pi^0\pi^+K^-, \pi^0 \rightarrow \gamma\gamma$ . As if trees grow, the diagrams are plotted from bottom to top.

※ [TopoAna: A generic tool for the event type analysis of inclusive Monte-Carlo samples in high energy physics experiments]

<https://www.sciencedirect.com/science/article/pii/S0010465520302575?via%3Dihub>

```
1 % Names of input root files
2 {
3   /gpfs/group/belle/users/chkim/b2ana/output/bd2tautau/signal/local/bd2tautau_local_sig_MC15_BGx1_230321_par_TopoAna_000.root
4 }
5
6 % TTree name
7 {
8   tree
9 }
10
11 # Here, AOI, VOI, MSI, and MSD are short for array of integers, vector of integers, multiple scalar integers, and multiple scalar doubles.
12 % Storage type of input raw topology truth information (Six options: AOI, VOI, MSI, MSF, MSD, and MSID. Default: AOI)
13 {
14   MSID
15 }
16
17 % Component analysis --- decay trees
18 {
19   Y      100
20 }
21
22 % Component analysis --- cascade decay branches of particles
23 {
24   Upsilon(4S)  Y_4S  150
25   B0           B0    150
26   tau+         taup  100
27   tau-         taum  100
28 }
29
30 % Component analysis --- inclusive decay branches
31 {
32   B0 --> tau+ tau-          & B0Xtt   & 100
33 }
34
35 % Common name of output files (Default: Name of the card file)
36 {
37   topoana
38 }
```

※ [Topology Analysis: Sphinx Manual]

[https://b2-master.belle2.org/software/sphinx/light-2212-foldex/online\\_book/analysis/topoana.html](https://b2-master.belle2.org/software/sphinx/light-2212-foldex/online_book/analysis/topoana.html)

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※ [Topology Analysis: Sphinx Manual]

[https://b2-master.belle2.org/software/sphinx/light-2212-foldex/online\\_book/analysis/topoana.html](https://b2-master.belle2.org/software/sphinx/light-2212-foldex/online_book/analysis/topoana.html)

Table 1: Decay trees and their respective initial-final states.

rowNo	decay tree (decay initial-final states)	iDcyTr	nEtr	nCEtr
1	$\Upsilon(4S) \rightarrow B^0 \bar{B}^0, B^0 \rightarrow \tau^+ \tau^-, \bar{B}^0 \rightarrow \rho^- D^+, \tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau, \tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau, \rho^- \rightarrow \pi^0 \pi^-,$ $D^+ \rightarrow \pi^+ \pi^+ K^-$ $(\Upsilon(4S) \rightarrow \mu^+ \mu^- \nu_\mu \bar{\nu}_\mu \nu_\tau \bar{\nu}_\tau \pi^0 \pi^+ \pi^+ \pi^- K^-)$	491	4	4
2	$\Upsilon(4S) \rightarrow B^0 \bar{B}^0, B^0 \rightarrow \rho^+ D^-, \bar{B}^0 \rightarrow \tau^+ \tau^-, \rho^+ \rightarrow \pi^0 \pi^+, D^- \rightarrow \pi^- \pi^- K^+, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^+,$ $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$ $(\Upsilon(4S) \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau \bar{\nu}_\tau \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^+)$	493	4	8
3	$\Upsilon(4S) \rightarrow B^0 \bar{B}^0, B^0 \rightarrow \pi^+ \pi^+ \pi^- D^-, \bar{B}^0 \rightarrow \tau^+ \tau^-, D^- \rightarrow \pi^- \pi^- K^+, \tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau, \tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$ $(\Upsilon(4S) \rightarrow \mu^+ \mu^- \nu_\mu \bar{\nu}_\mu \nu_\tau \bar{\nu}_\tau \pi^+ \pi^+ \pi^- \pi^- K^+)$	893	4	12
4	$\Upsilon(4S) \rightarrow B^0 \bar{B}^0, B^0 \rightarrow \tau^+ \tau^-, \bar{B}^0 \rightarrow \pi^+ \pi^- \pi^- D^+, \tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau \gamma^F \gamma^F, \tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau, D^+ \rightarrow \pi^+ \pi^+ K^-$ $(\Upsilon(4S) \rightarrow e^+ e^- \nu_e \bar{\nu}_e \nu_\tau \bar{\nu}_\tau \pi^+ \pi^+ \pi^- \pi^- K^- \gamma^F \gamma^F)$	16	3	15
5	$\Upsilon(4S) \rightarrow B^0 \bar{B}^0, B^0 \rightarrow \tau^+ \tau^-, \bar{B}^0 \rightarrow D^{*+} a_1^-, \tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau \gamma^F, \tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau, D^{*+} \rightarrow \pi^+ D^0,$ $a_1^- \rightarrow \pi^- f_0(600), D^0 \rightarrow \pi^0 \pi^+ K^-, f_0(600) \rightarrow \pi^+ \pi^-$ $(\Upsilon(4S) \rightarrow \mu^+ \mu^- \nu_\mu \bar{\nu}_\mu \nu_\tau \bar{\nu}_\tau \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^- \gamma^F)$	23	3	18
⋮				
rowNo	decay tree (decay initial-final states)	iDcyTr	nEtr	nCEtr
97	$\Upsilon(4S) \rightarrow B^0 \bar{B}^0, B^0 \rightarrow \tau^+ \tau^-, \bar{B}^0 \rightarrow \pi^+ \pi^- \rho^- D^{*+}, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^0 \pi^+, \tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau \gamma^F, \rho^- \rightarrow \pi^0 \pi^-,$ $D^{*+} \rightarrow \pi^+ D^0, D^0 \rightarrow \pi^0 \pi^+ K^-$ $(\Upsilon(4S) \rightarrow e^- \bar{\nu}_e \nu_\tau \bar{\nu}_\tau \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- K^- \gamma^F)$	71	2	279
98	$\Upsilon(4S) \rightarrow B^0 \bar{B}^0, B^0 \rightarrow \pi^+ \pi^+ \rho^- D^{*-} \gamma^F, \bar{B}^0 \rightarrow \tau^+ \tau^-, \rho^- \rightarrow \pi^0 \pi^-, D^{*-} \rightarrow \pi^0 D^-, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^+,$ $\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau \gamma^F, D^- \rightarrow \pi^- K^+ K^-$ $(\Upsilon(4S) \rightarrow e^- \bar{\nu}_e \nu_\tau \bar{\nu}_\tau \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^+ K^- \gamma^F \gamma^F)$	74	2	281
99	$\Upsilon(4S) \rightarrow B^0 \bar{B}^0, B^0 \rightarrow \tau^+ \tau^-, \bar{B}^0 \rightarrow \pi^0 \rho^- D^{*+}, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^+, \tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau, \rho^- \rightarrow \pi^0 \pi^-,$ $D^{*+} \rightarrow \pi^+ D^0, D^0 \rightarrow K^- a_1^+, a_1^+ \rightarrow \pi^+ \pi^+ \pi^- \gamma^F$ $(\Upsilon(4S) \rightarrow e^- \bar{\nu}_e \nu_\tau \bar{\nu}_\tau \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^- \pi^- K^- \gamma^F)$	76	2	283
100	$\Upsilon(4S) \rightarrow B^0 \bar{B}^0, B^0 \rightarrow D^{*-} a_1^+, \bar{B}^0 \rightarrow \tau^+ \tau^-, D^{*-} \rightarrow \pi^0 D^-, a_1^+ \rightarrow \pi^+ \pi^+ \pi^- \gamma^F, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^+,$ $\tau^- \rightarrow \nu_\tau \pi^0 \pi^+ \pi^- \pi^-, D^- \rightarrow \pi^0 \pi^- K_S^0, K_S^0 \rightarrow \pi^+ \pi^-$ $(\Upsilon(4S) \rightarrow \nu_\tau \bar{\nu}_\tau \pi^0 \pi^0 \pi^0 \pi^+ \pi^+ \pi^+ \pi^- \pi^- \pi^- \pi^- \gamma^F)$	82	2	285
rest	$\Upsilon(4S) \rightarrow \text{others (1696 in total)}$ $(\Upsilon(4S) \rightarrow \text{corresponding to others})$	—	2030	2315



Table 3: Cascade decay branches of  $B^0$ .

rowNo	cascade decay branch of $B^0$	iCascDcyBrP	nCase	nCCase
1	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^+, \tau^- \rightarrow \nu_\tau \pi^0 \pi^-$	6	73	73
2	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau, \tau^- \rightarrow \nu_\tau \pi^0 \pi^-$	39	46	119
3	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau, \tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$	30	43	162
4	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^+, \tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$	124	40	202
5	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^+, \tau^- \rightarrow \nu_\tau \pi^-$	102	35	237
6	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau, \tau^- \rightarrow \nu_\tau \pi^0 \pi^0 \pi^-$	139	30	267
7	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow \bar{\nu}_\tau \pi^+, \tau^- \rightarrow \nu_\tau \pi^0 \pi^-$	109	29	296
8	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^+, \tau^- \rightarrow \nu_\tau \pi^0 \pi^0 \pi^-$	99	24	320
9	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau, \tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$	122	24	344
10	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau, \tau^- \rightarrow \nu_\tau \pi^0 \pi^-$	180	24	368
	⋮			
145	$B^0 \rightarrow \tau^+ \tau^-, \tau^+ \rightarrow \bar{\nu}_\tau \pi^0 \pi^+, \tau^- \rightarrow \nu_\tau \pi^- \gamma^F$	732	3	1173
146	$B^0 \rightarrow \pi^+ \pi^- p \bar{\Lambda}_c^-, \bar{\Lambda}_c^- \rightarrow \pi^- K^+ \bar{p}$	741	3	1176
147	$B^0 \rightarrow \pi^0 \pi^+ \eta D^{*-}, \eta \rightarrow \gamma \gamma, D^{*-} \rightarrow \pi^- \bar{D}^0, \bar{D}^0 \rightarrow \pi^0 \pi^- K^+$	755	3	1179
148	$B^0 \rightarrow D^- D_s^+, D^- \rightarrow \pi^- \rho^- K^+, D_s^+ \rightarrow \pi^+ \pi^- K^+, \rho^- \rightarrow \pi^0 \pi^- \gamma^F$	764	3	1182
149	$B^0 \rightarrow \pi^0 \pi^0 \rho^+ D^{*-}, \rho^+ \rightarrow \pi^0 \pi^+, D^{*-} \rightarrow \pi^- \bar{D}^0, \bar{D}^0 \rightarrow K^+ K^-$	765	3	1185
150	$B^0 \rightarrow \pi^0 K^{*+} D^-, K^{*+} \rightarrow \pi^0 K^+, D^- \rightarrow \pi^- K^+ K^-$	840	3	1188
rest	$B^0 \rightarrow \text{others (898 in total)}$	—	1127	2315

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