

# Cosmological constraints from cosmic chronometer



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# Determination Cosmological parameter

$$H(t) = H_0 \sqrt{\Omega_M (1+z)^3 + \Omega_\Lambda (1+z)^{3(1+w)} + \Omega_K (1+z)^2}$$

Matter parameter  $\Omega_M = \frac{\rho_M}{\rho_c}$

Dark energy density parameter  $\Omega_\Lambda = \frac{\rho_\Lambda}{\rho_c}$

Curvature  $\Omega_K = 1 - \Omega_M - \Omega_\Lambda$

$$\rho_c \equiv \frac{3c^2 H^2}{8\pi G}$$

The current critical density

$w$  : The dark energy equation-of-state parameter

# Data used in this project

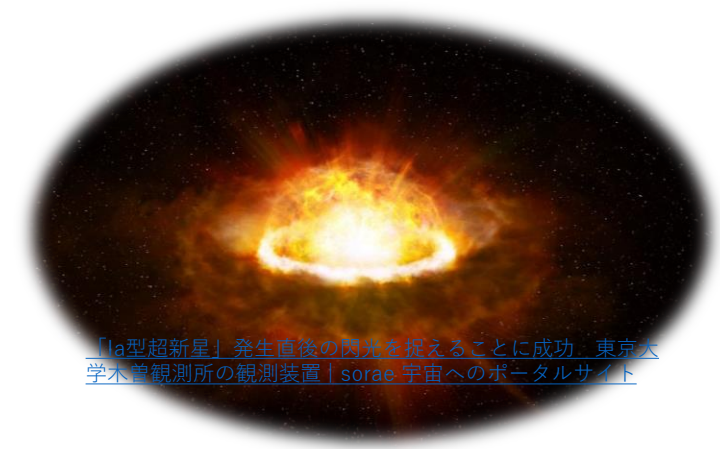
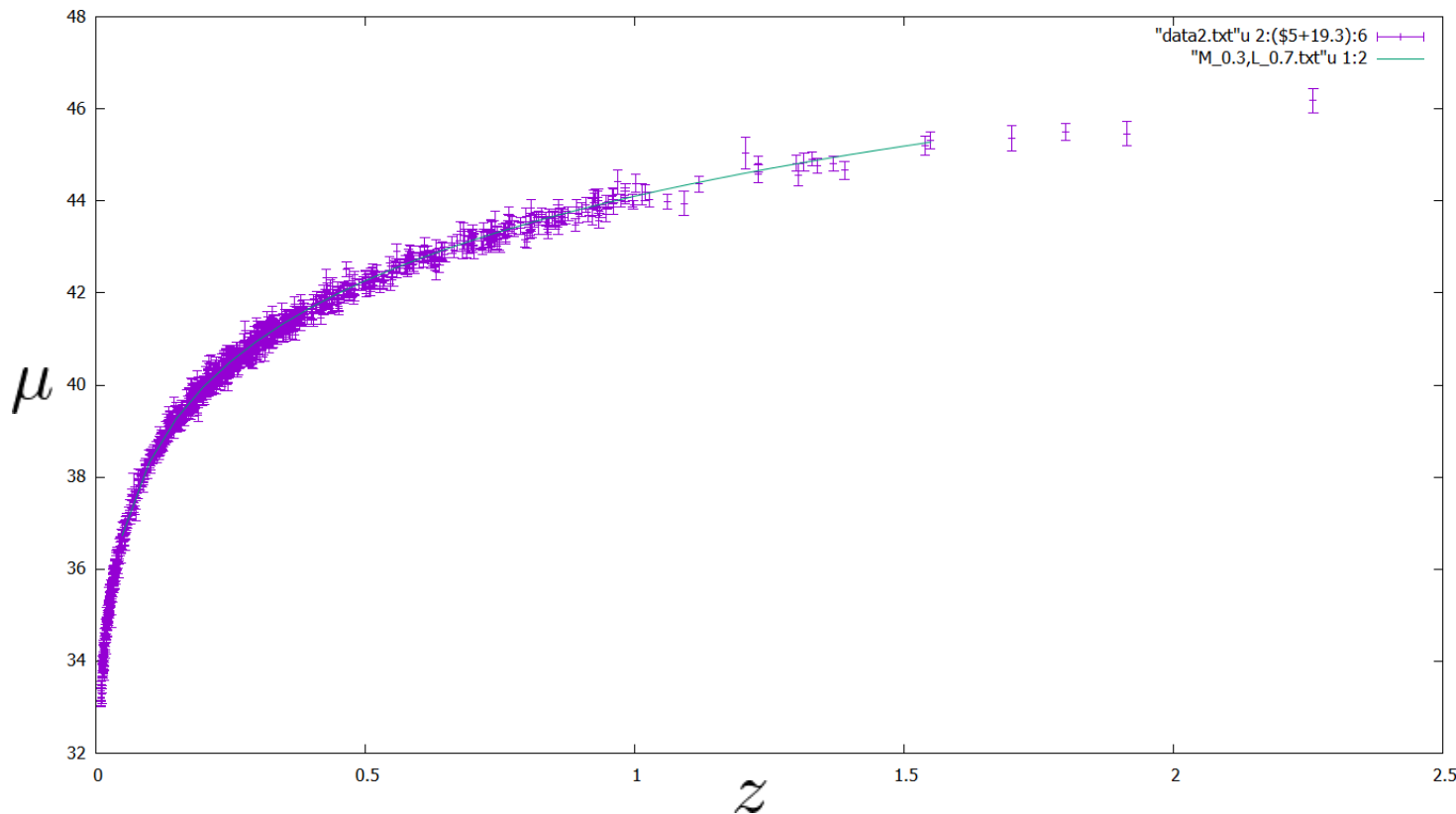
- Supernova and Cosmic chronometer



# Supernova

Based on the luminosity distance

$$d_L = (1 + z) \int_0^z \frac{dz'}{H(z')}$$



[「Ia型超新星」発生直後の閃光を捉えることに成功 - 東京大学宇宙観測所の観測装置 | sorae 宇宙へのポータルサイト](#)

- a wide range of redshifts ( $z=0.01 \sim 2.26$ )
- The number of the data is 1048.

$$\mu = m - M = 5 \log_{10} \frac{d_L}{1 \text{ Mpc}} + 25$$

$\mu$  : distance modulus  
 $m$  : apparent magnitude  
 $M$  : absolute magnitude

# Cosmic chronometer



Based on relative galaxy age

$$H(z) = -\frac{1}{(1+z)} \frac{dz}{dt} \approx -\frac{1}{1+z} \frac{\Delta z}{\Delta t}$$

## ☆ Conditions for selection

- Passive stellar populations
- evolve on a timescale much larger than their differential ages

ex) massive , early , passively-evolving galaxies

# How to use cosmic chronometer



$$H(z) = -\frac{1}{(1+z)} \frac{dz}{dt} \approx -\frac{1}{1+z} \frac{\Delta z}{\Delta t}$$

- Only measure differential age  $\frac{\Delta z}{\Delta t}$  .

☆ We used to constrain cosmological parameters.

- The standard  $\Lambda$ CDM model
- Scenarios with some dark energy characterized by its equation of state

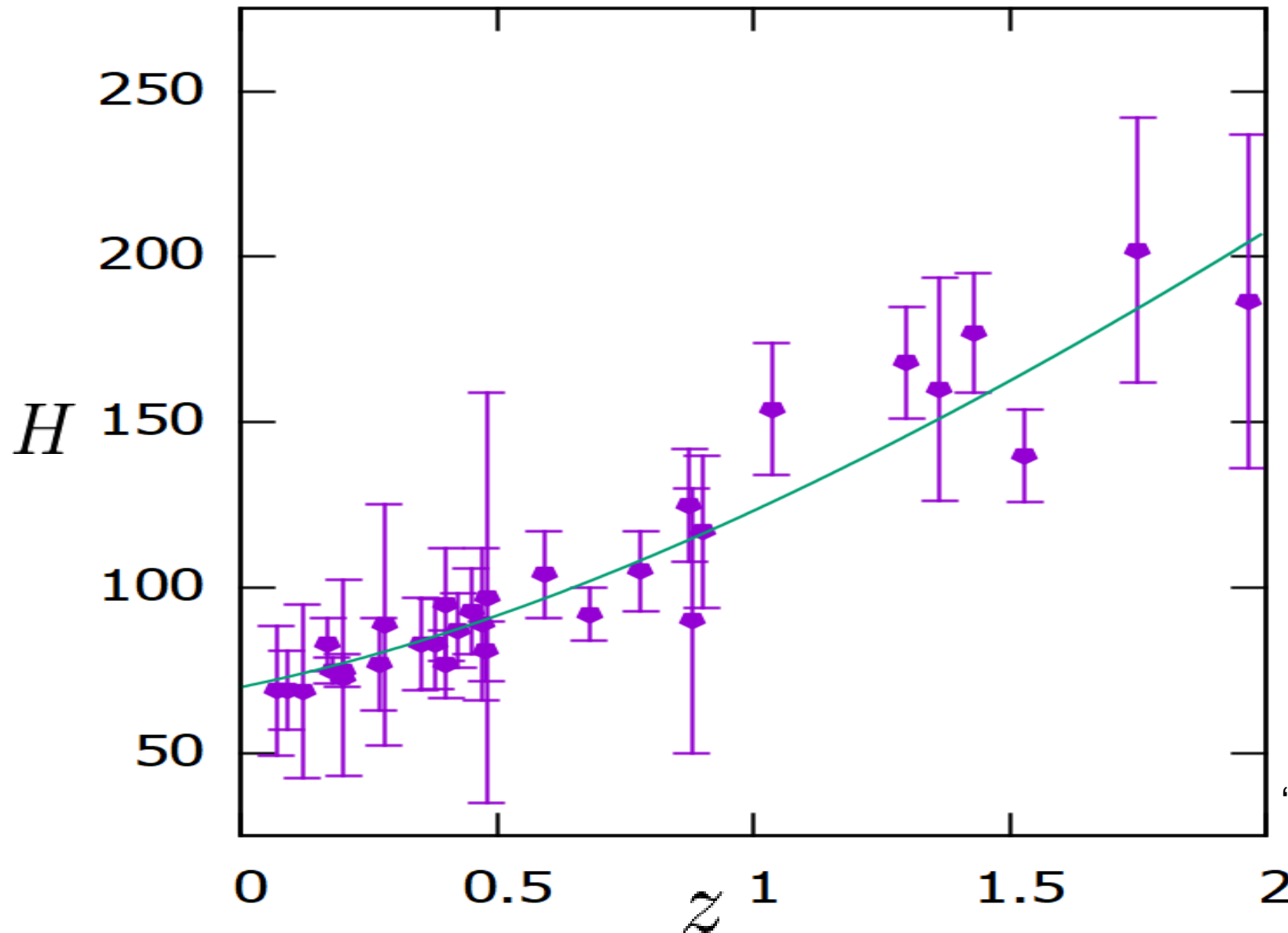
# Usefulness of Cosmic chronometer data



The effect of observational systematics on the CC dataset is relatively small, but the total error is larger than that of SN data.

CC determines  $H(z)$  with  $\sim 10\%$  uncertainties ( $z < 2$ )

# H as a function of z

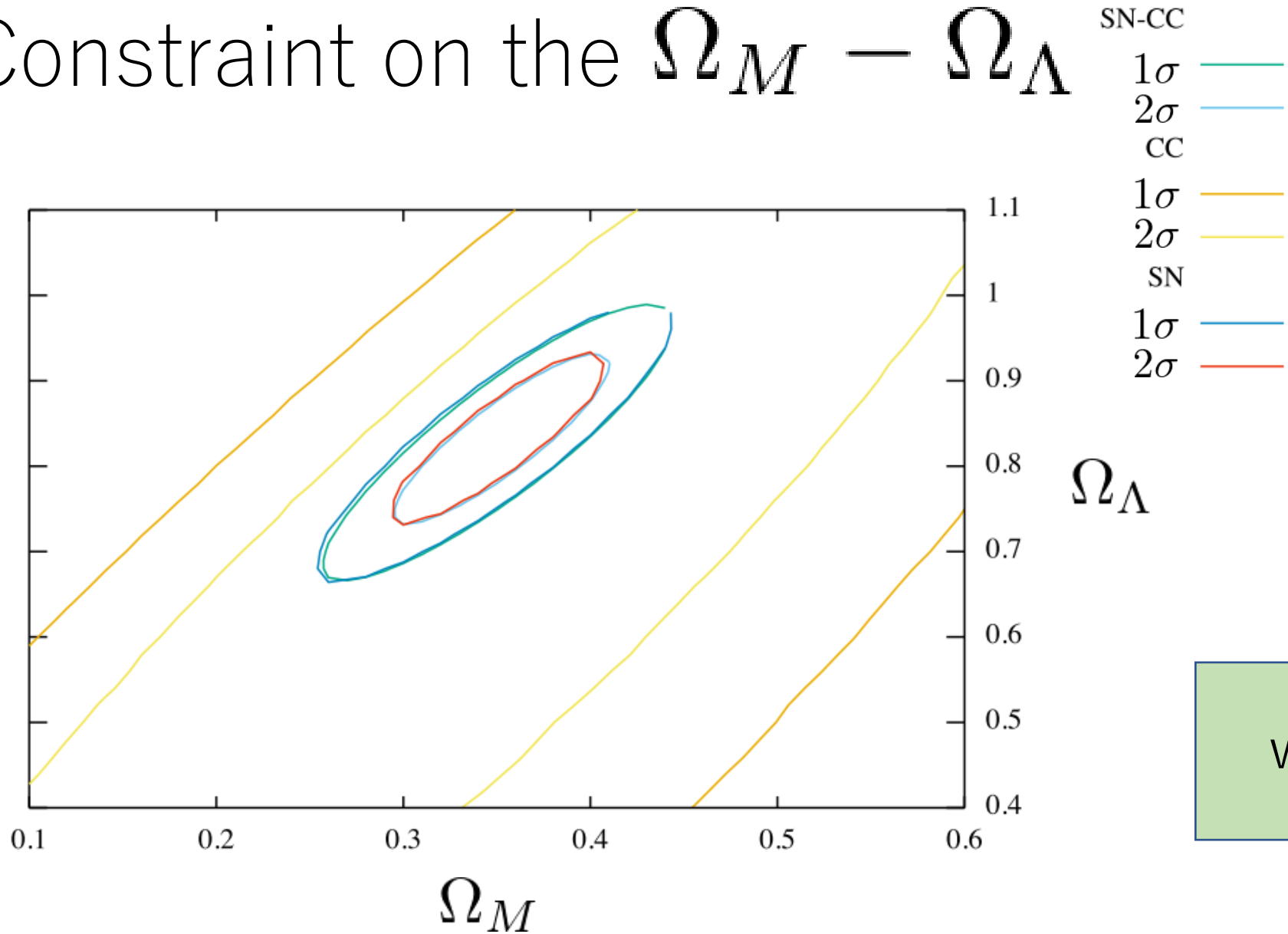


theoretical curve —  
Cosmic chronometer data ●

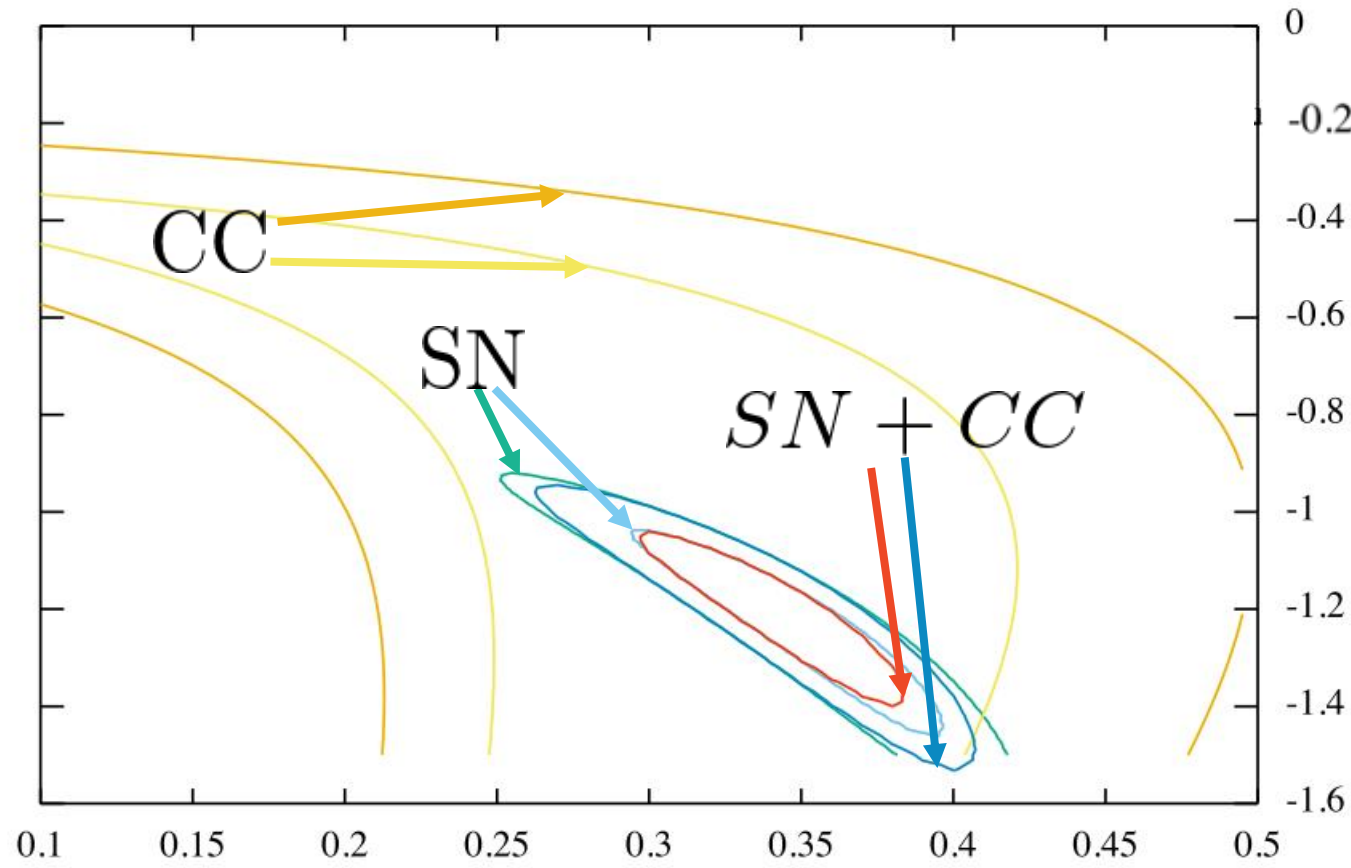
“Vagnozzi, Loeb, Moresco 2011.11645”



Constraint on the  $\Omega_M - \Omega_\Lambda$



# Constraint on the $\Omega_M - w$



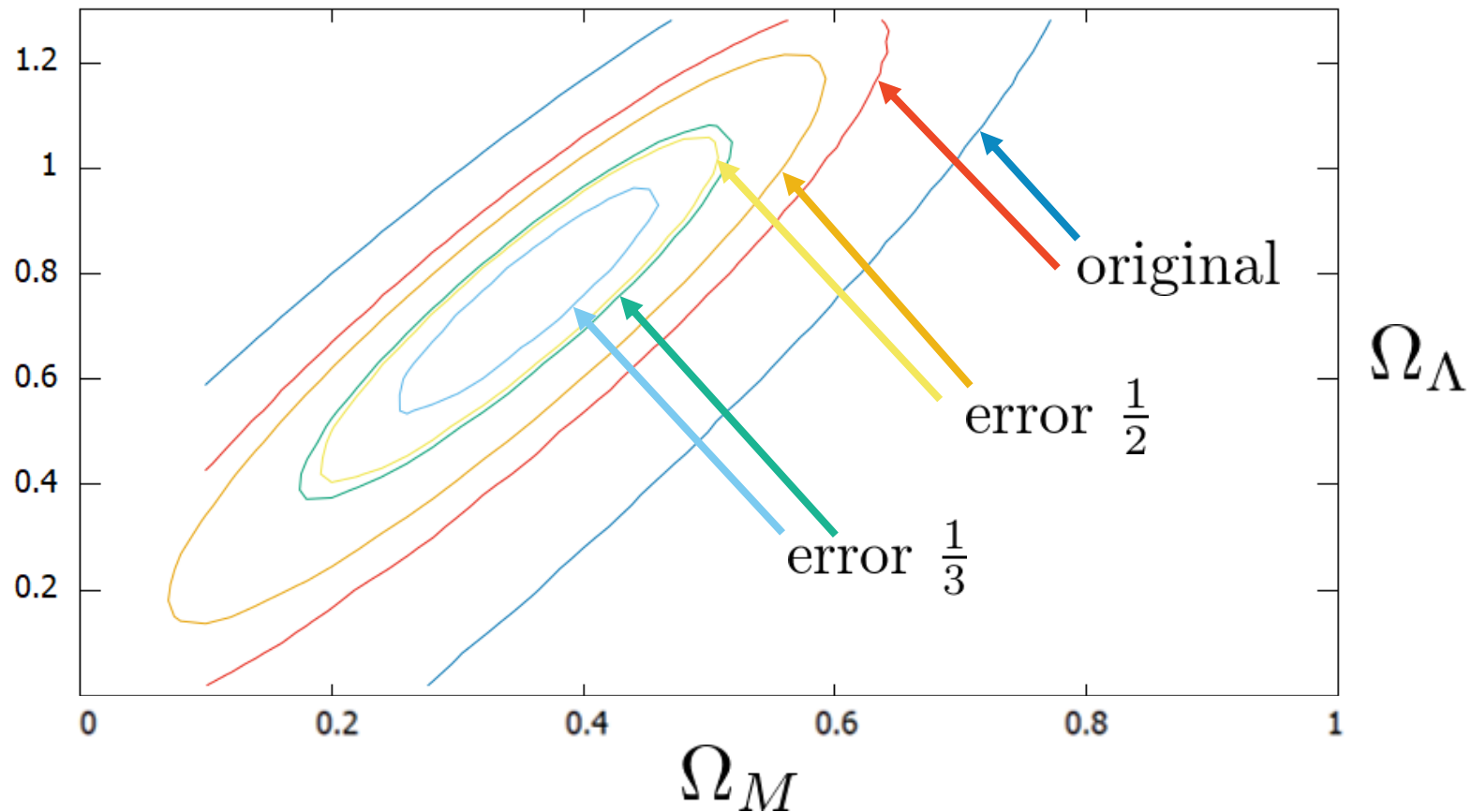
$$\Omega_\Lambda = 1 - \Omega_M$$

CC limit range  $\gg$  SN limit range

# Assumption of improved observation techniques

Cosmic chronometer

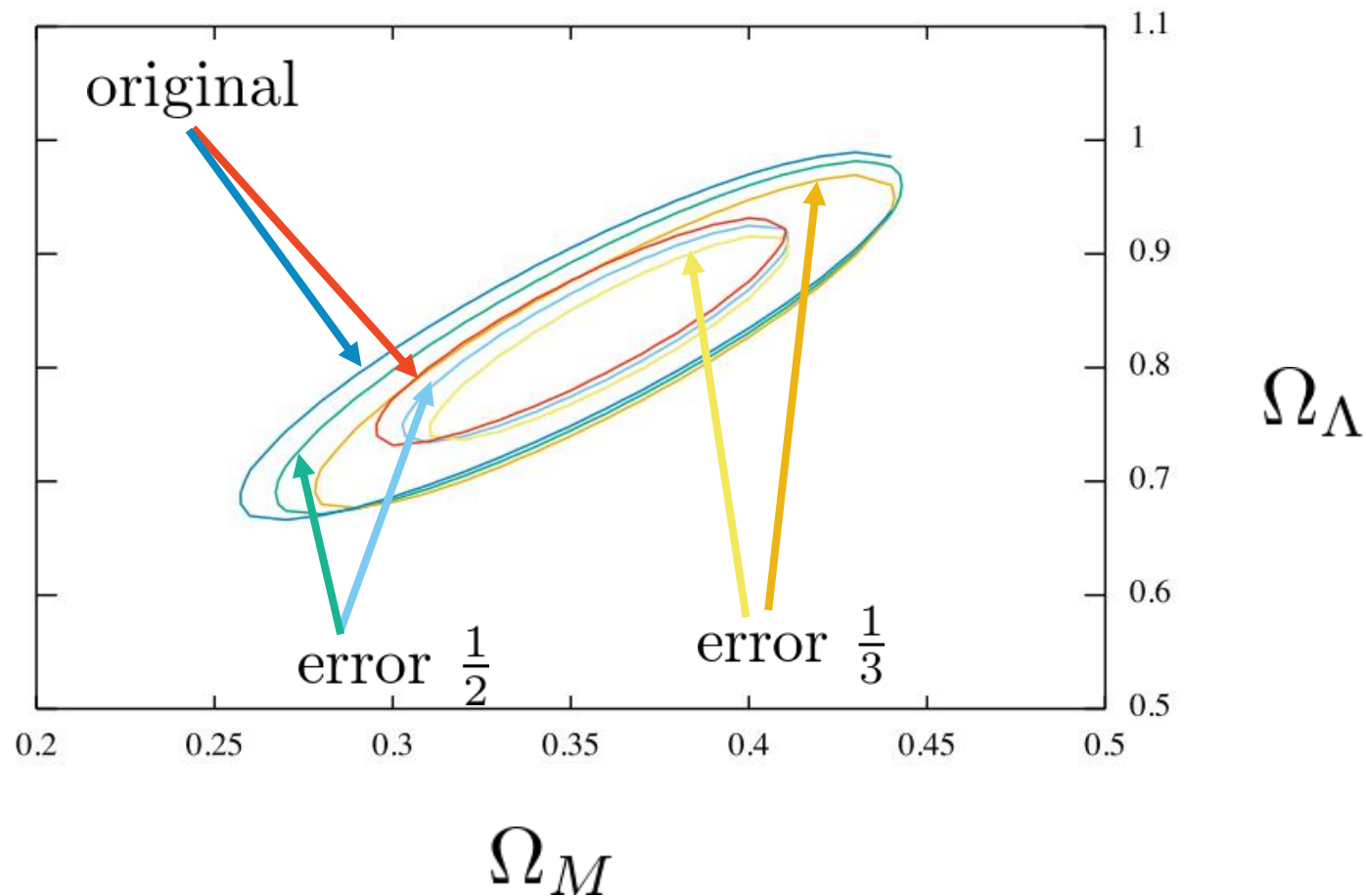
CC data error  
→ 1/2  
→ 1/3



# Assumption of improved observation techniques

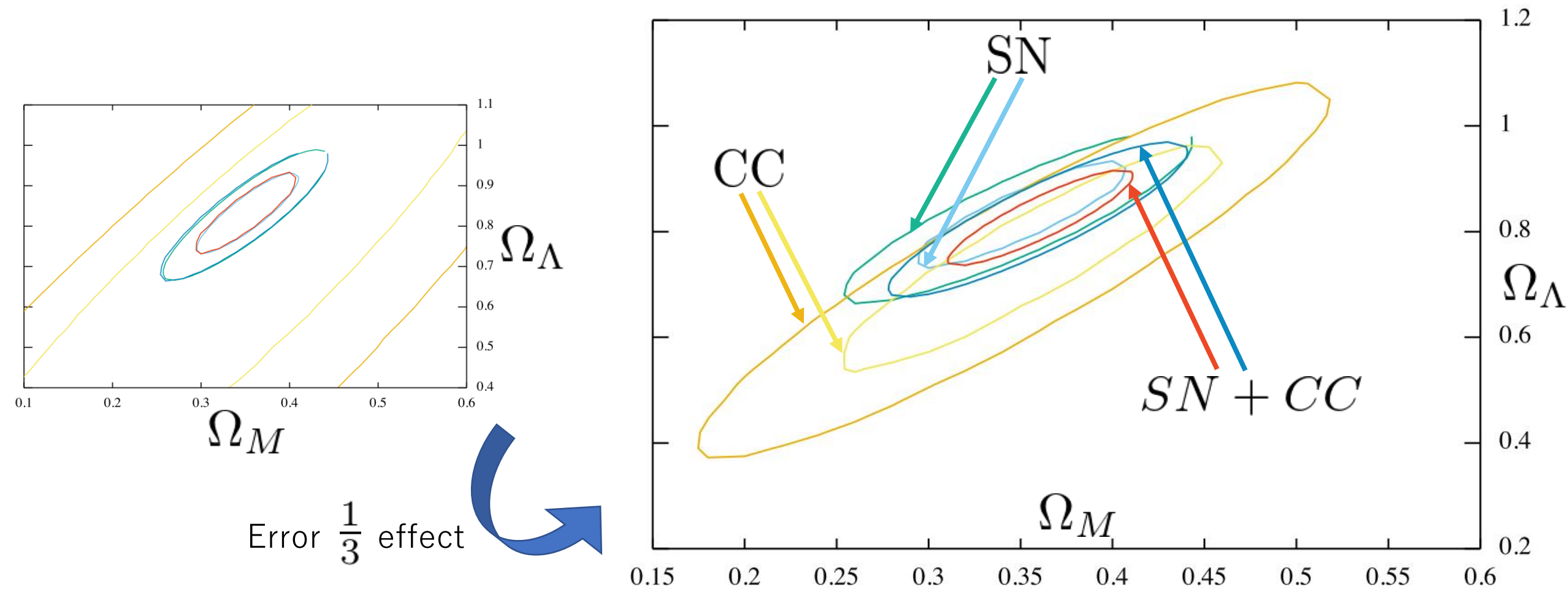
## Cosmic chronometer & supernova

CC data error  
→ 1/2  
→ 1/3



# Assumption of improved observation techniques

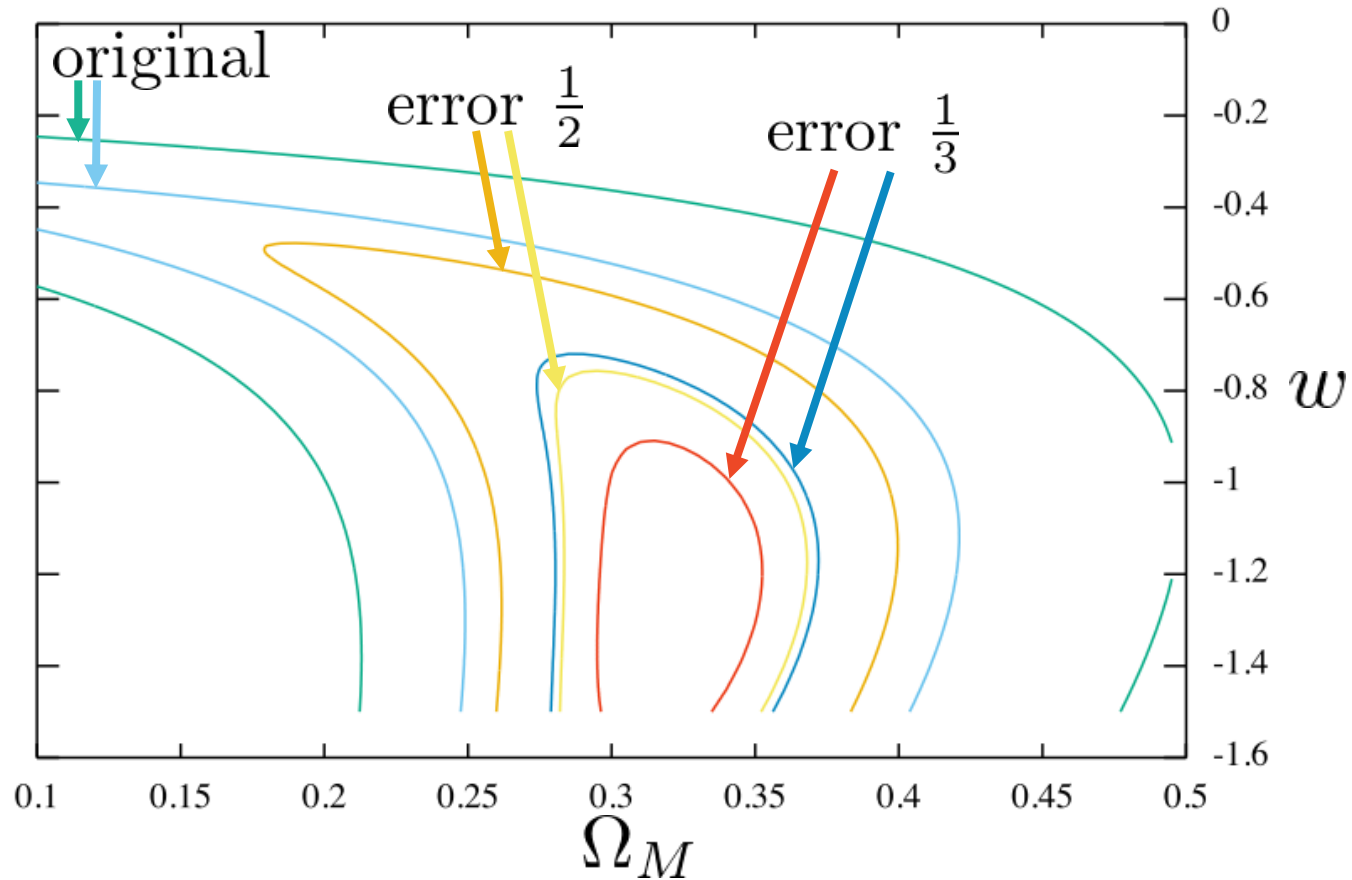
## Cosmic chronometer & supernova



# Assumption of improved observation techniques

Cosmic chronometer

$$\Omega_M - w$$



CC data error

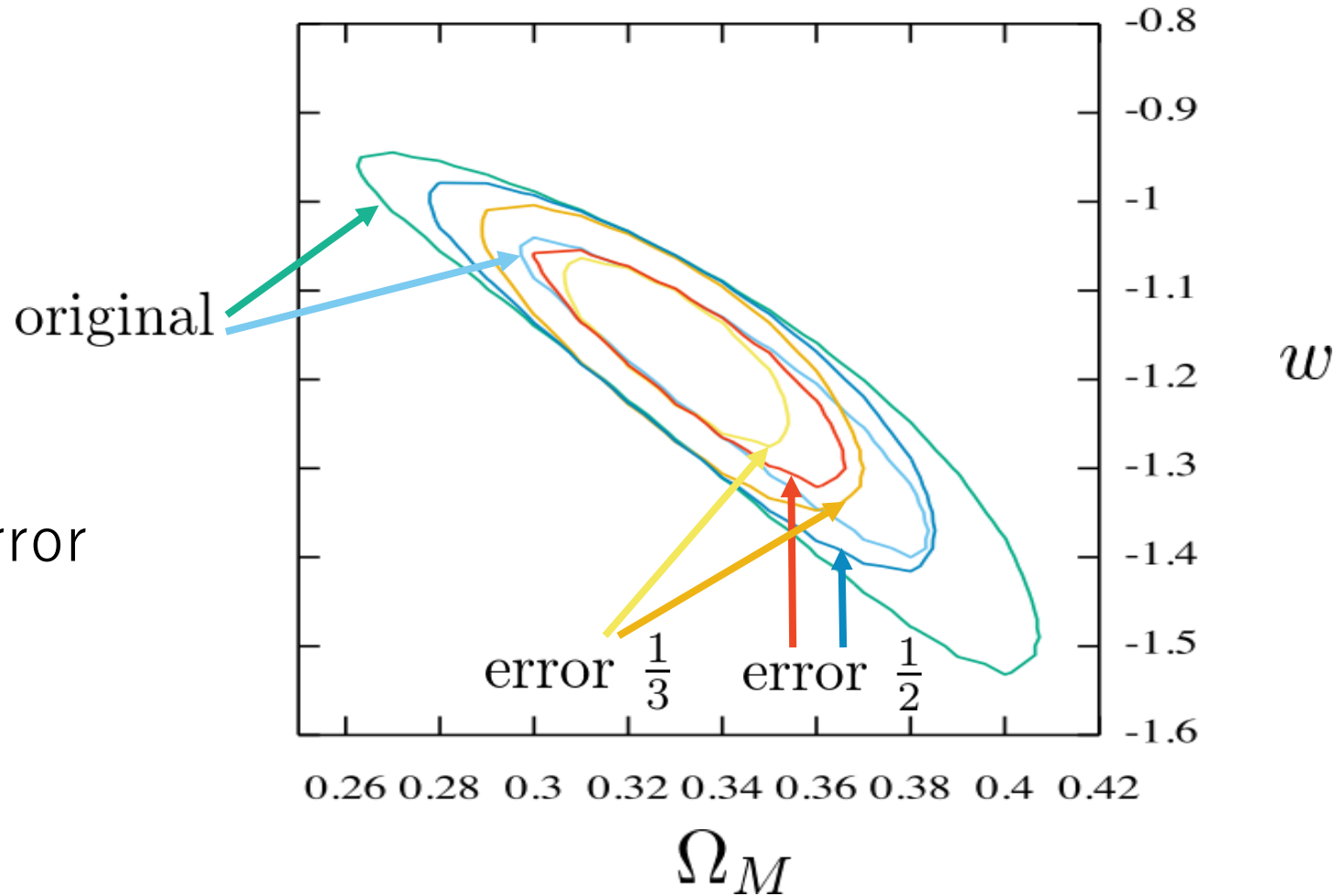
→ 1/2

→ 1/3

# Assumption of improved observation techniques

Cosmic chronometer & supernova

$$\Omega_M - w$$



CC data error

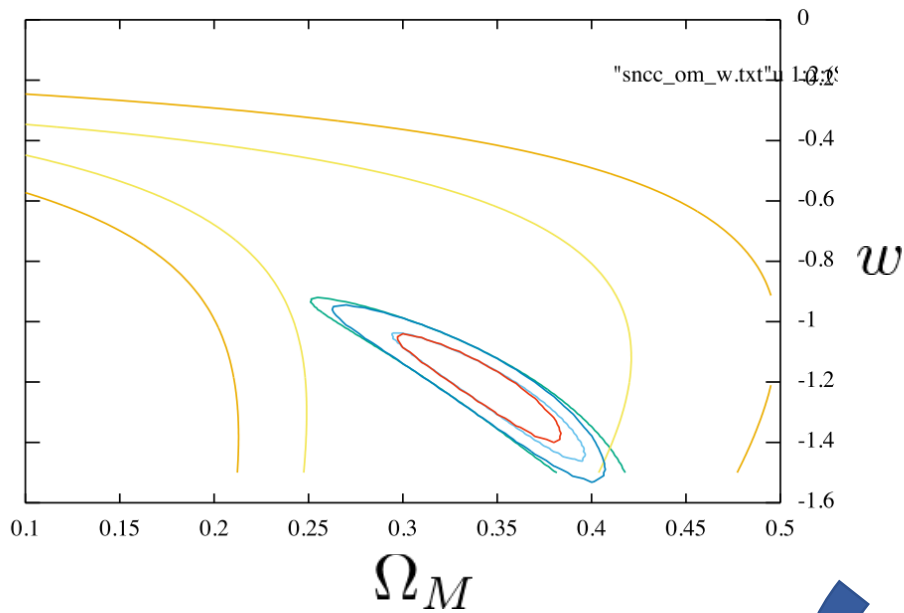
→ 1/2

→ 1/3

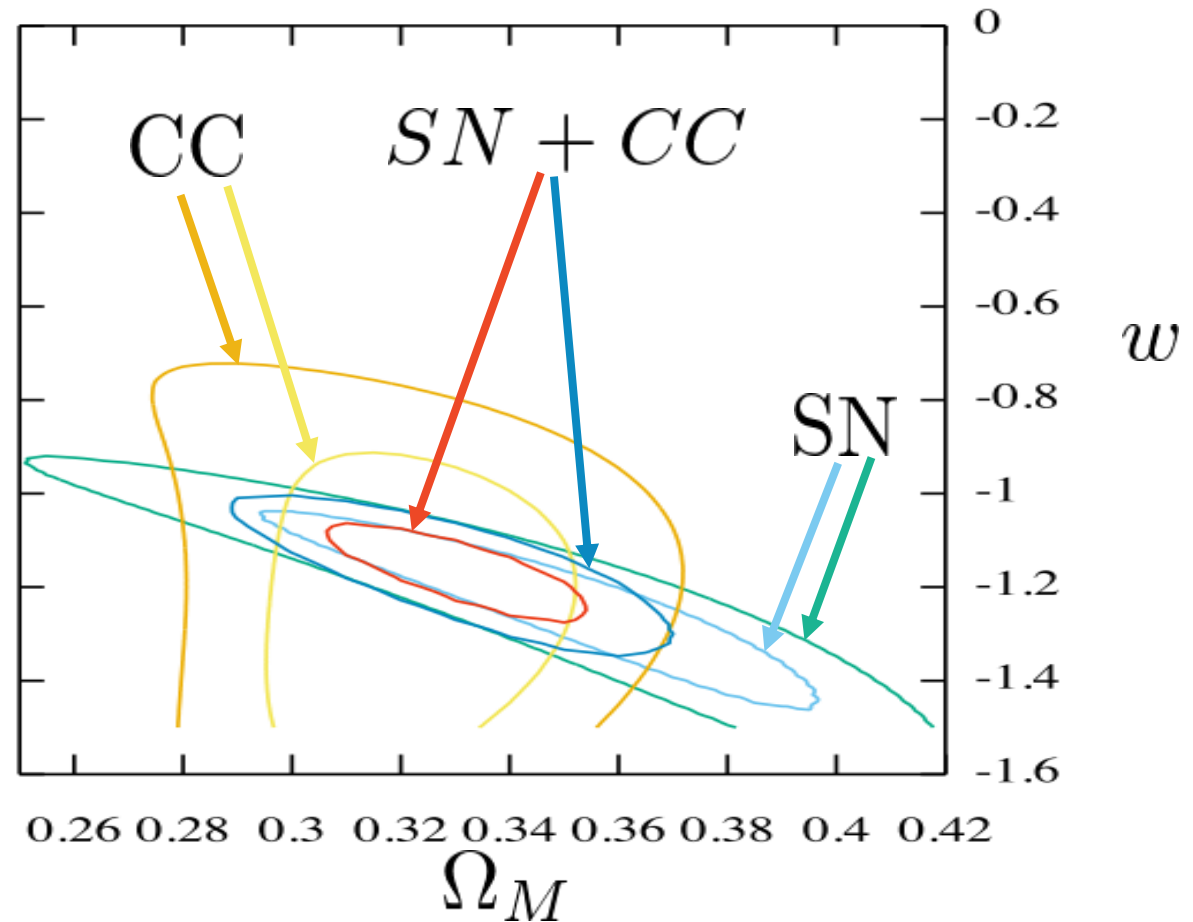
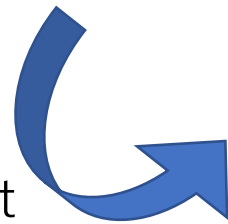
# Assumption of improved observation techniques

Cosmic chronometer & supernova

$$\Omega_M - w$$

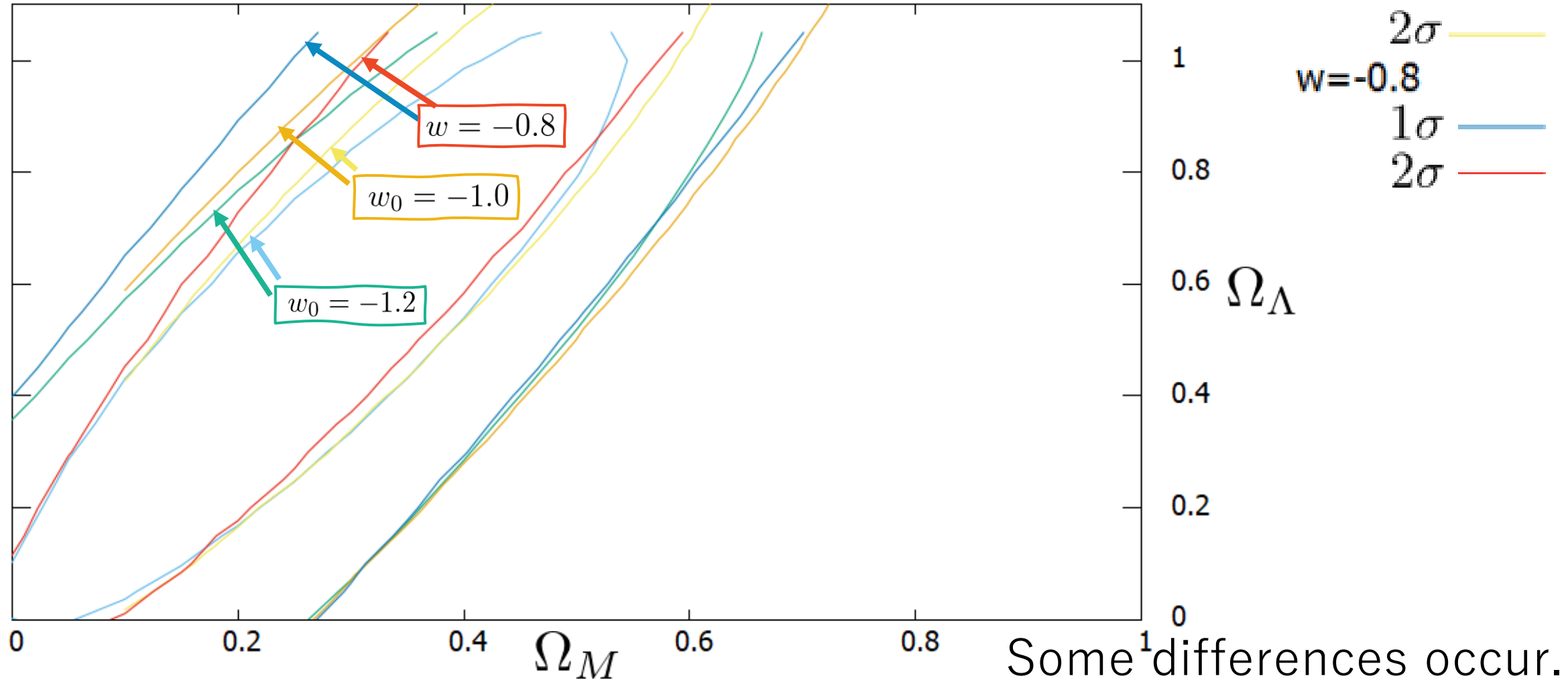


Error  $\frac{1}{3}$  effect





# Change $w$



# Time-dependent $w$

→ Chevallier–Polarski–Linder (CPL) Parametrization

The equation of state :  $w_X(z) = w_0 + (1 - a)w_1 = w_0 + \frac{z}{1+z}w_1$

The density  
of the dark energy :  $\rho_X(z) = \rho_{W_0} (1 + z)^{3(1+w_0+w_1)} \exp\left[-\frac{3w_1 z}{1+z}\right]$

$$H(z) = H_0 \sqrt{\Omega_M (1 + z)^3 + \Omega_\Lambda (1 + z)^{3(1+w_0+w_1)} \exp\left[-3w_1 \frac{z}{1+z}\right] + \Omega_K (1 + z)^2}$$

# CPL parametrization

present value :  
( $a = 1$ )( $z = 0$ )

$$w_X(0) = w_0$$

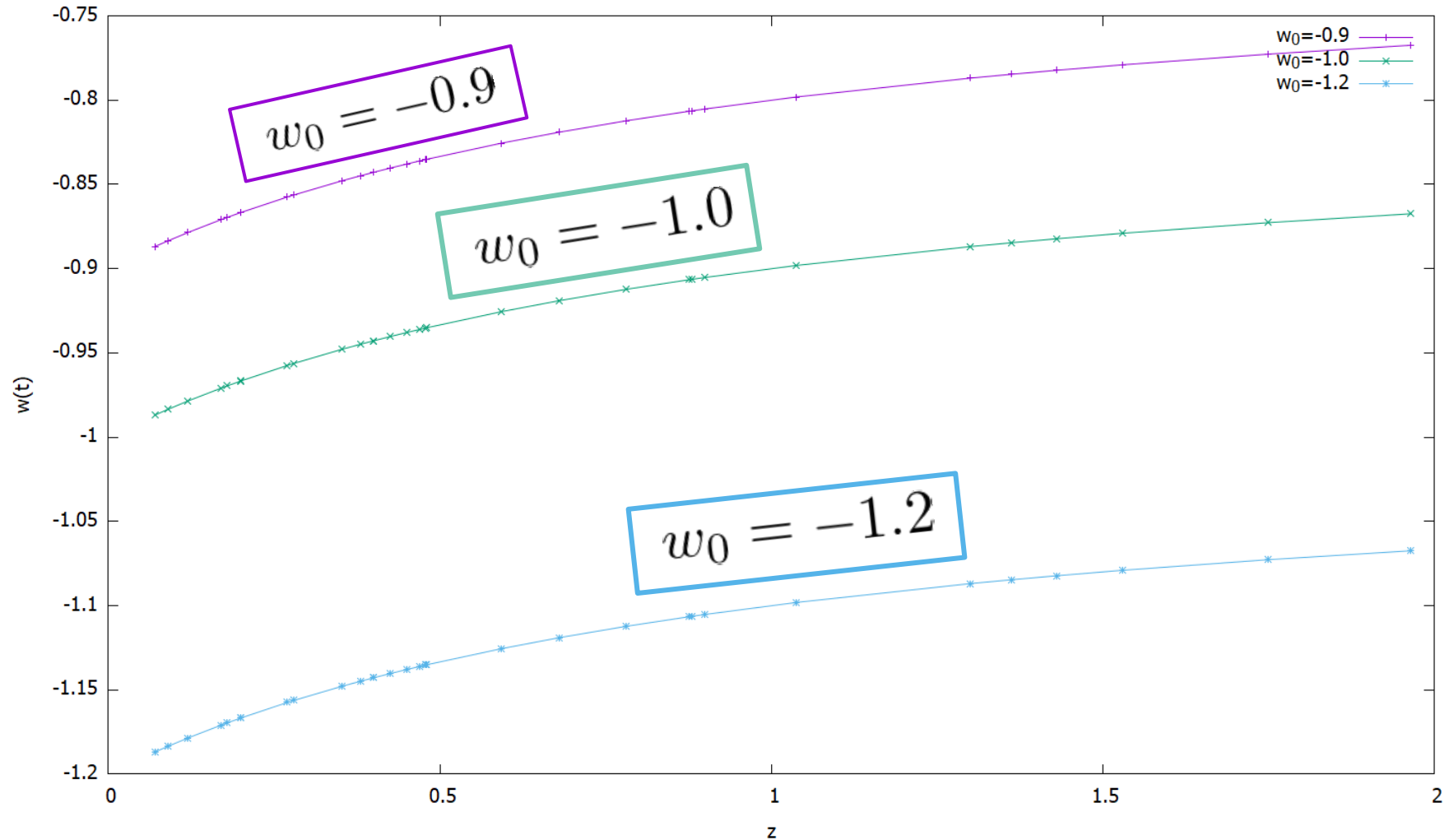
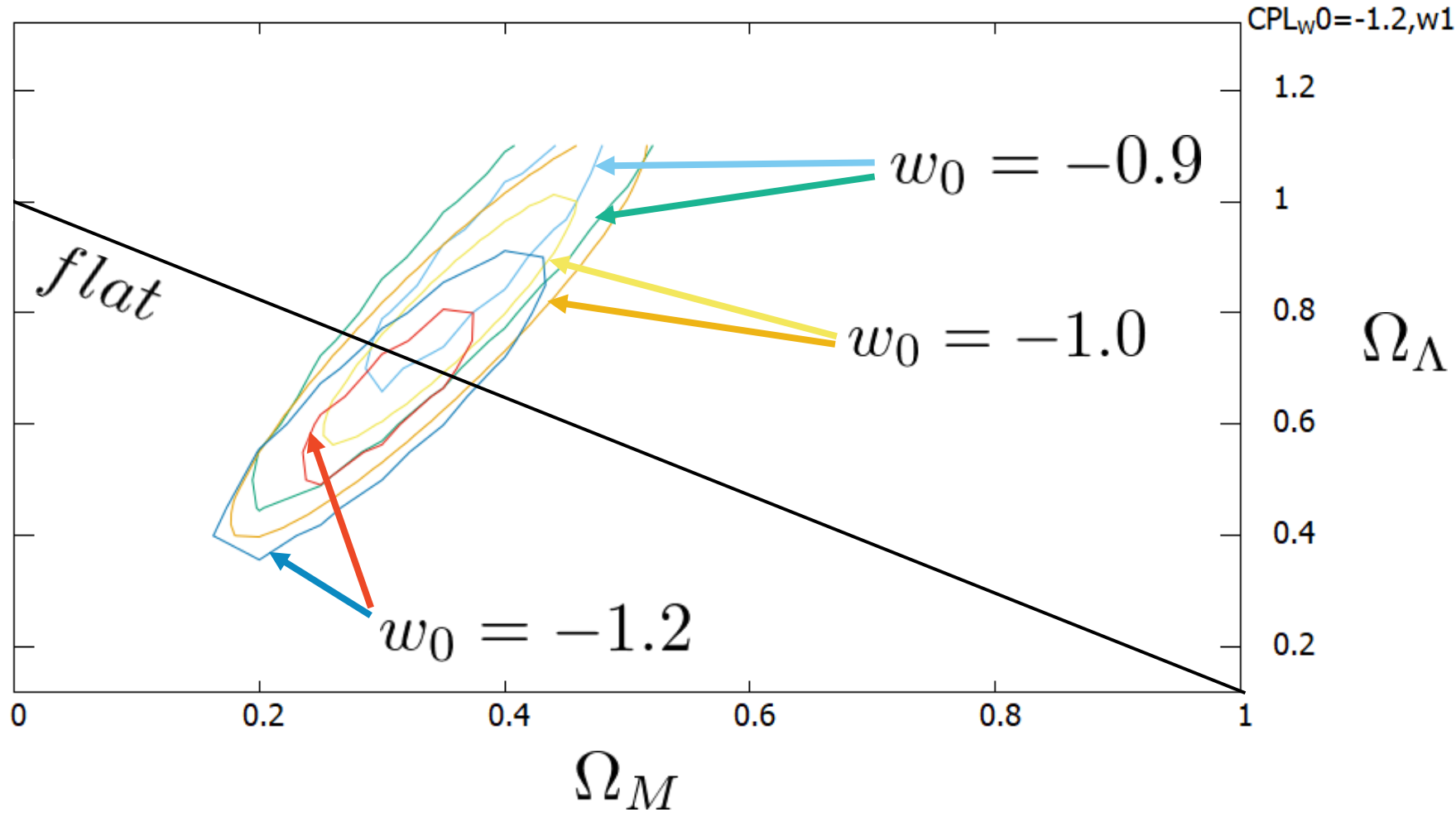
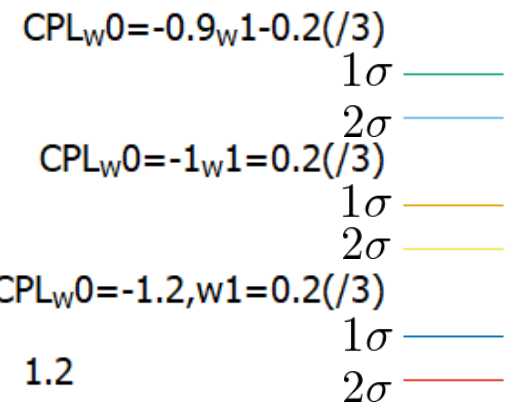


Figure z-w using cc data ( $w_1=0.2$ )

for CPL

Cosmic chronometer



CC data error  
→ 1/3

# Conclusion

- We have investigated constraints on the density parameters and the equation of state of dark energy from cosmic chronometer .
- Time-dependent  $w$  affects the constraint on the curvature of the Universe.
- If cosmic chronometer observational techniques improve, cosmological parameters can be more tightly constrained.

Thank you for listening.

$\mu$  : distance modulus  
 $m$  : apparent magnitude  
 $M$  : absolute magnitude

$$\mu = m - M = 5 \log_{10} \frac{d_L}{1 \text{ Mpc}} + 25$$

$$m \equiv -2.5 \log_{10} \frac{f}{f_0}$$

$$M \equiv -2.5 \log_{10} \frac{L}{L_0}$$

- Kazunori Kohri , Yoshihiko Oyama , Toyokazu Sekiguchi and Tomo Takahashi 1608.01601

**“Vagnozzi, Loeb, Moresco 2011.11645”**



theoretical curve

$$H(t) = H_0 \sqrt{\Omega_M (1+z)^3 + \Omega_\Lambda + \Omega_K (1+z)^2}$$

$$\Omega_M = 0.3$$

$$\Omega_\Lambda = 0.7$$

$$\Omega_K = 1 - \Omega_M - \Omega_\Lambda$$

$$H_0 = 70$$

# Plan

- SN and SN+CC for CPL
- Change  $w_1$