

Dark Matter and New Physics from Belle-II Experiment

Hyun Min Lee

Chung-Ang University, Korea



2021 KPS Spring Meeting Focus Session
Status report on Belle-II Heavy Flavor Experiment
KPS, Korea, April 21-23, 2021

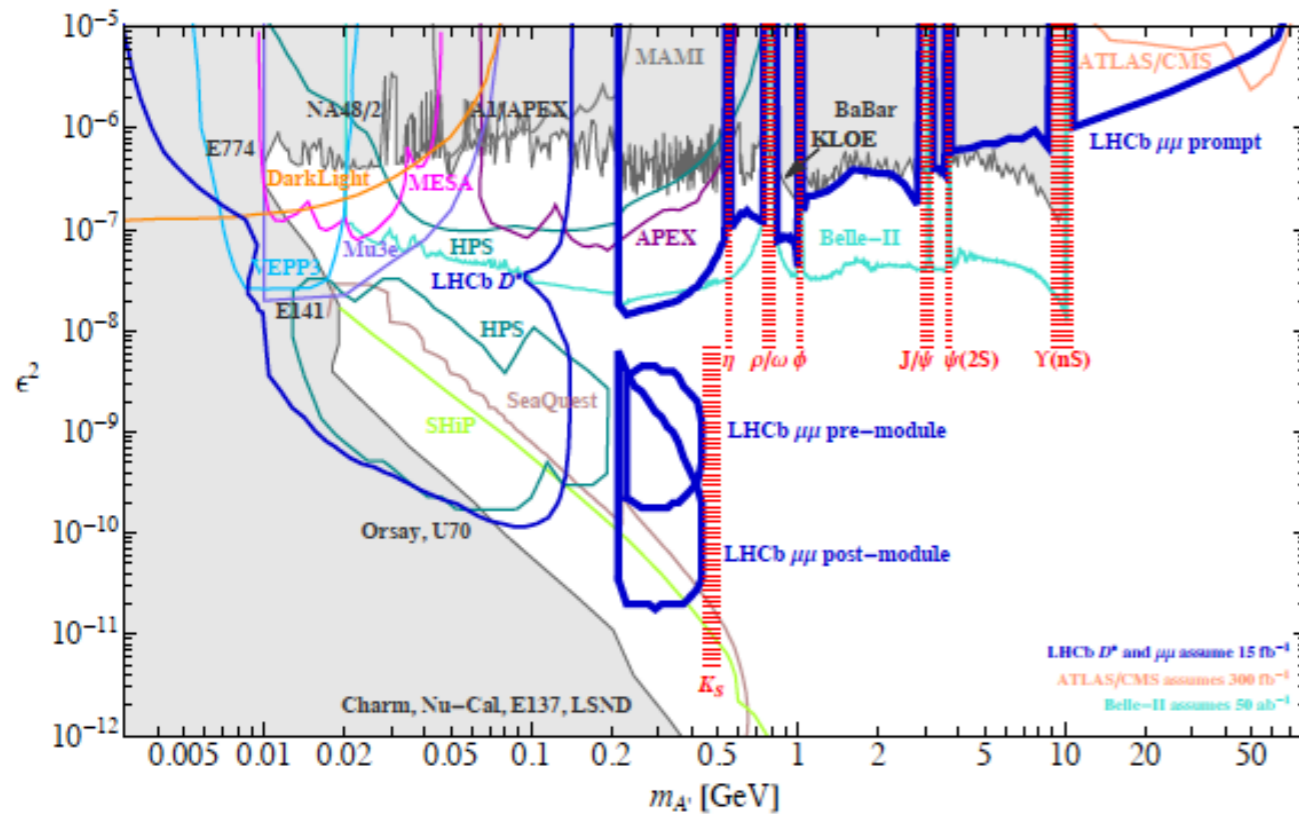
Outline

- Introduction
- Light dark matter and mediators
- B-meson anomalies and new physics
- Conclusions

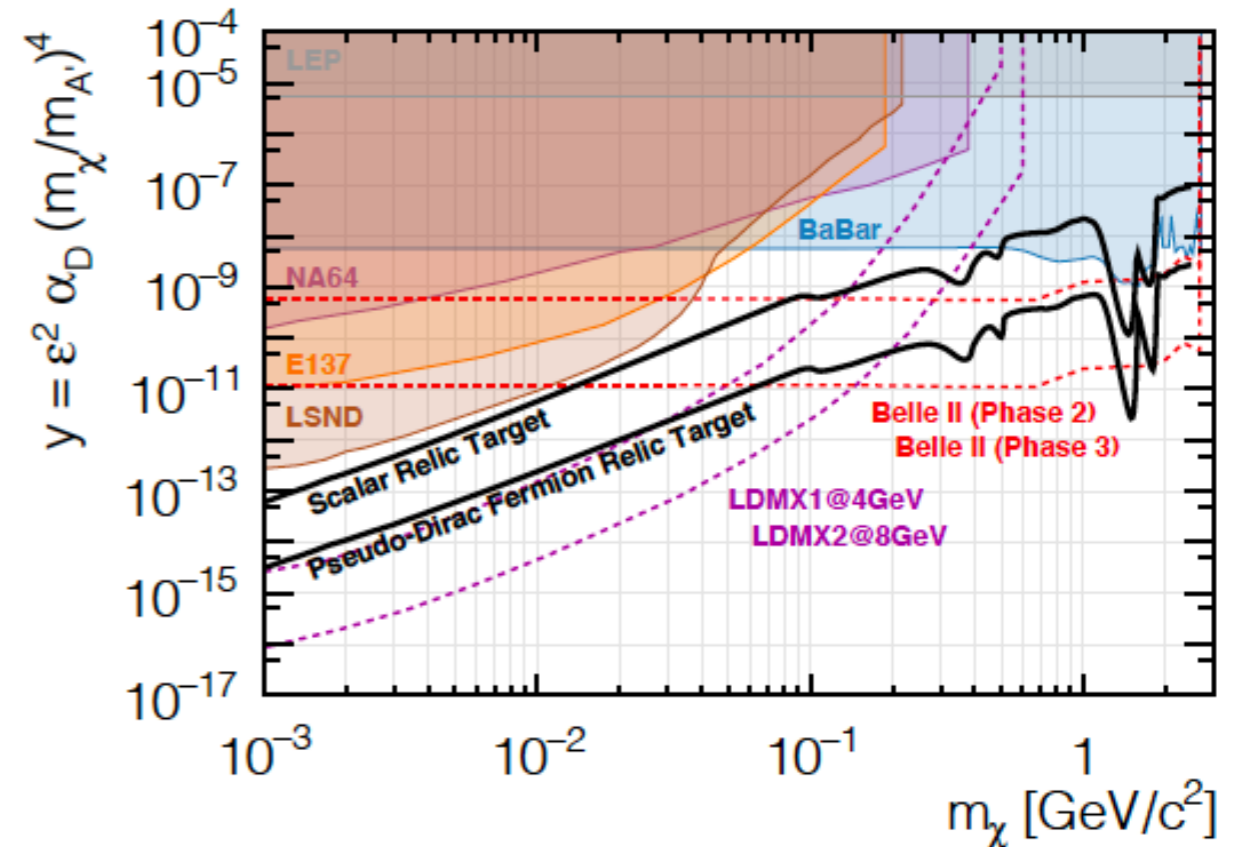
Light dark matter and mediators

Energy/Intensity interplay

-1-



[Ilten et al, 2016]

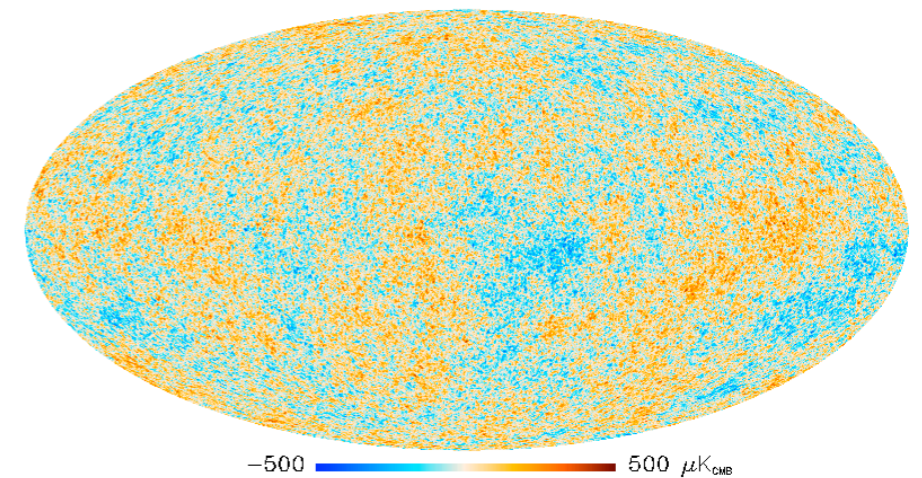
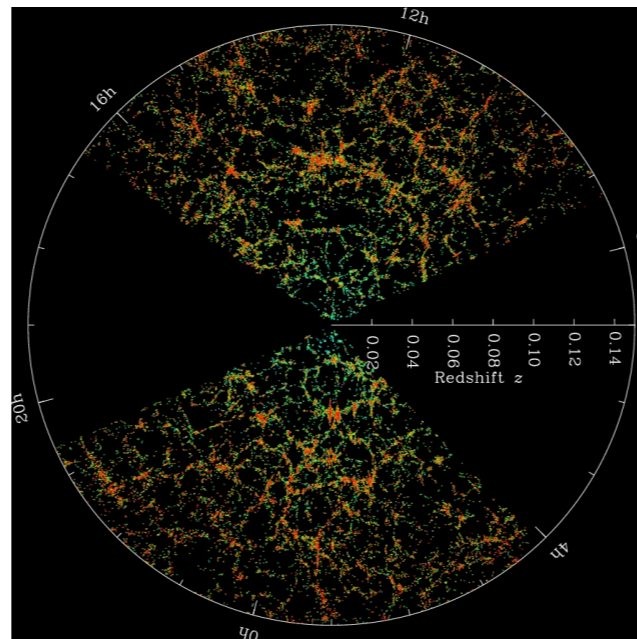
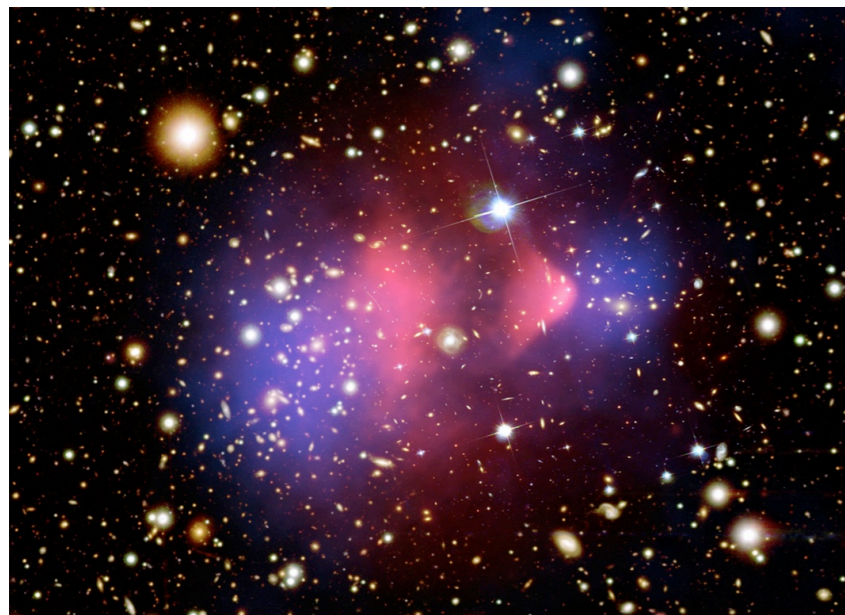
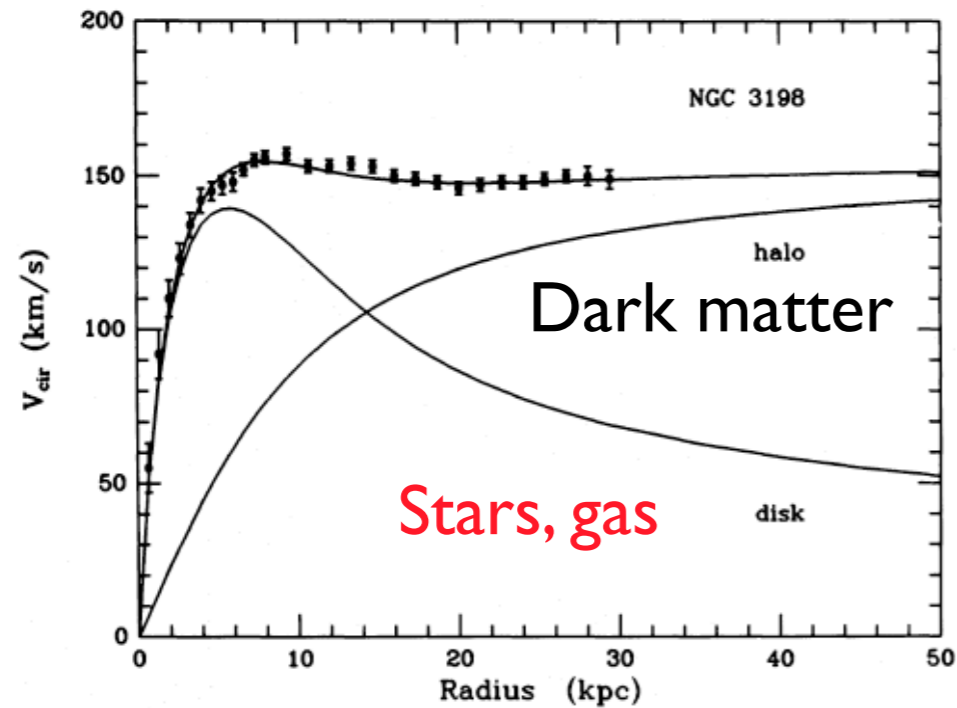


[Belle-II, 1808.10567]

- No direct evidence for new physics at LHC.
 - ➔ Little hierarchy between weak scale and new physics?
- New particles are very weakly coupled and/or light.
 - ➔ Testable with precision and intensity experiments?

Evidences for dark matter

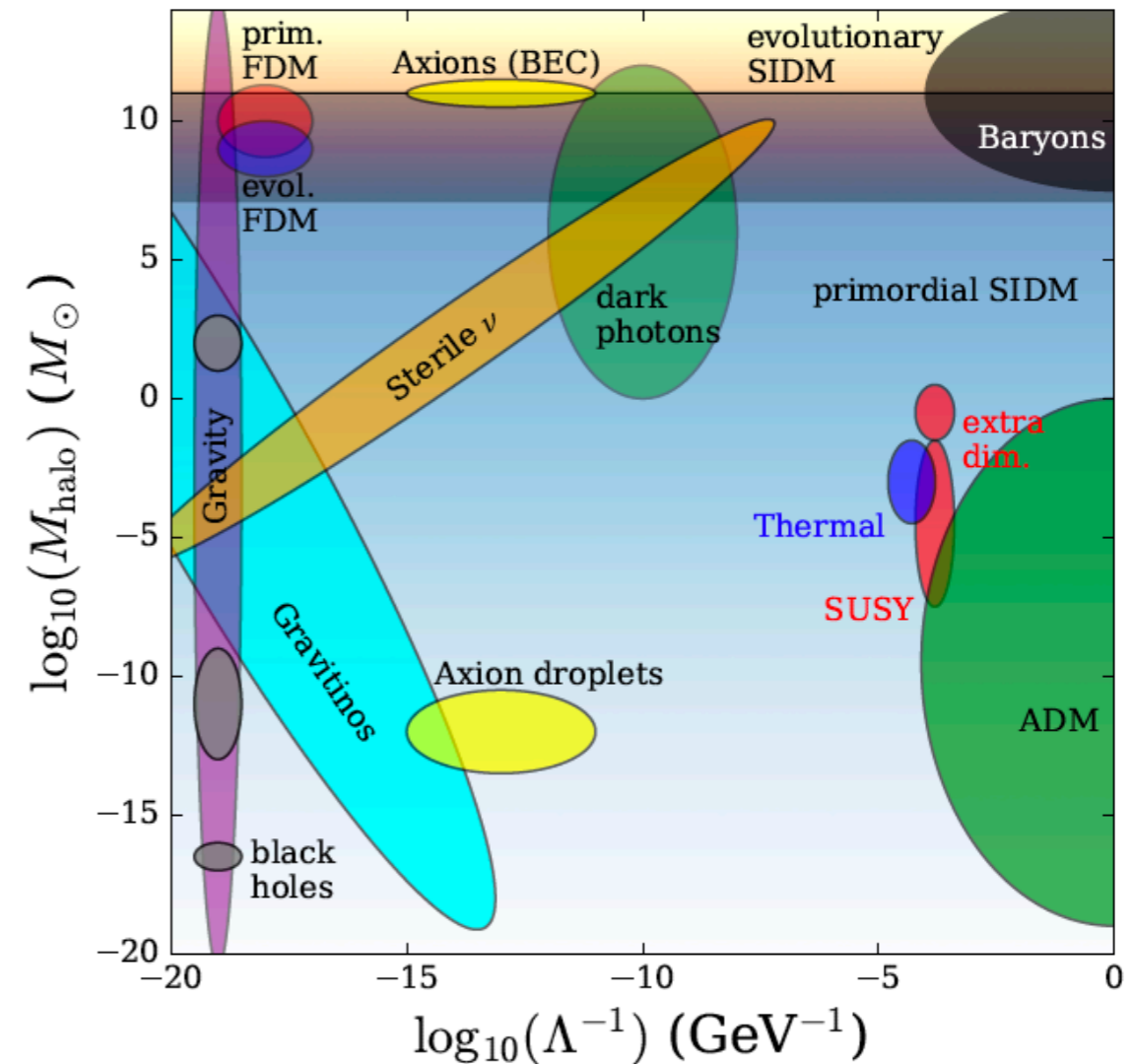
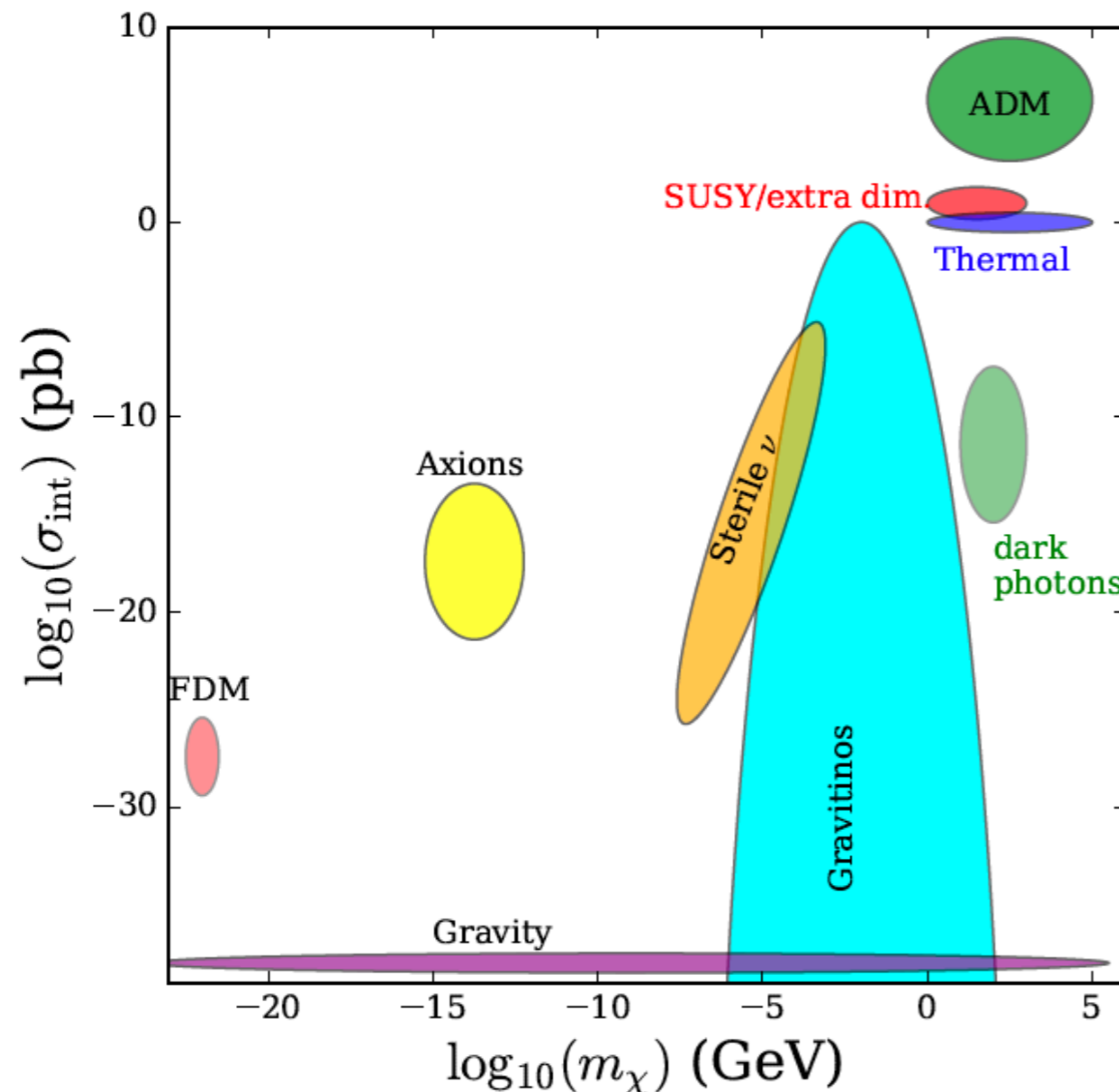
-2-



- Galaxy rotation curves, gravity lensing, Bullet cluster, CMB, hint at invisible mass, Dark Matter.

Status of DM models

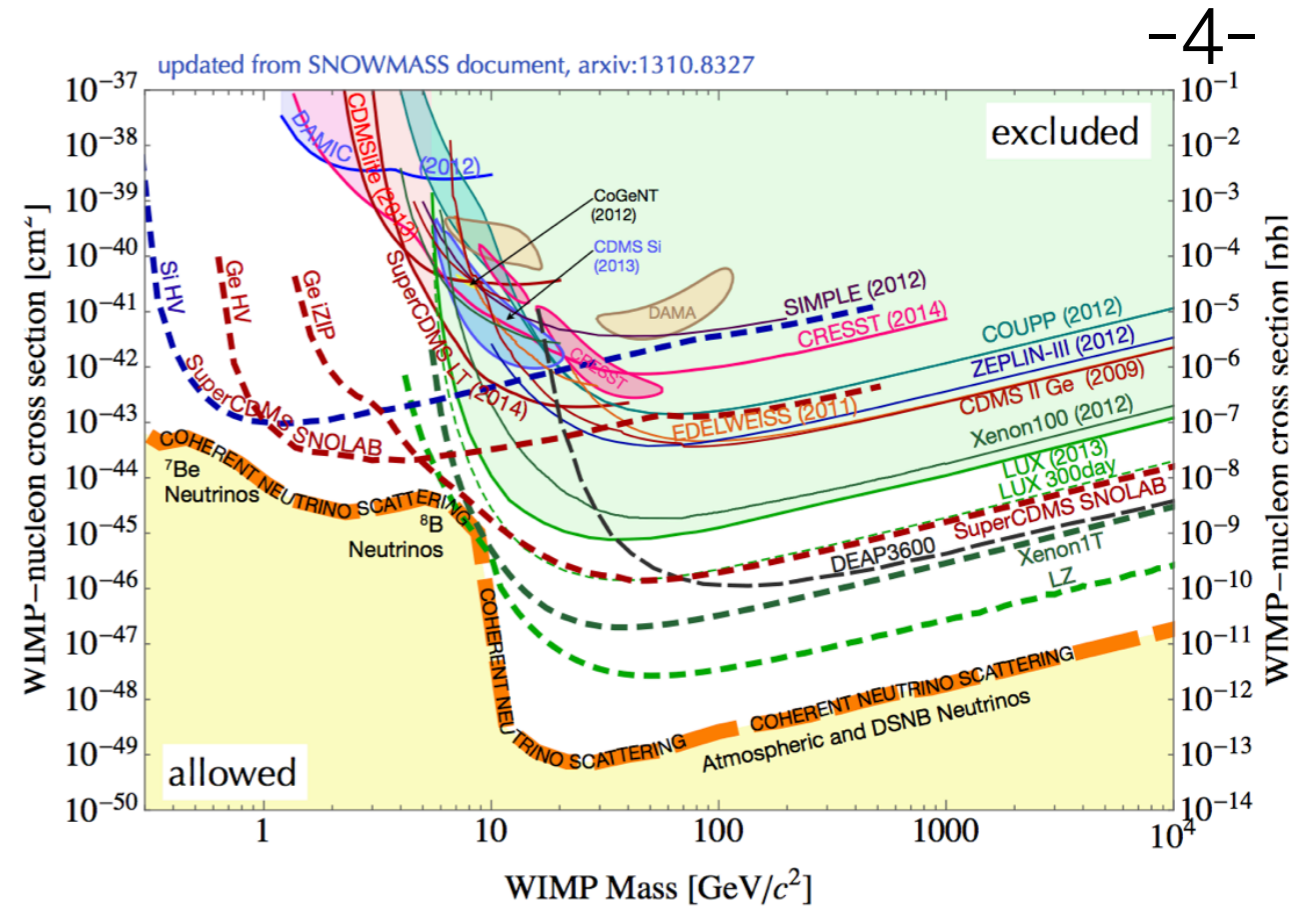
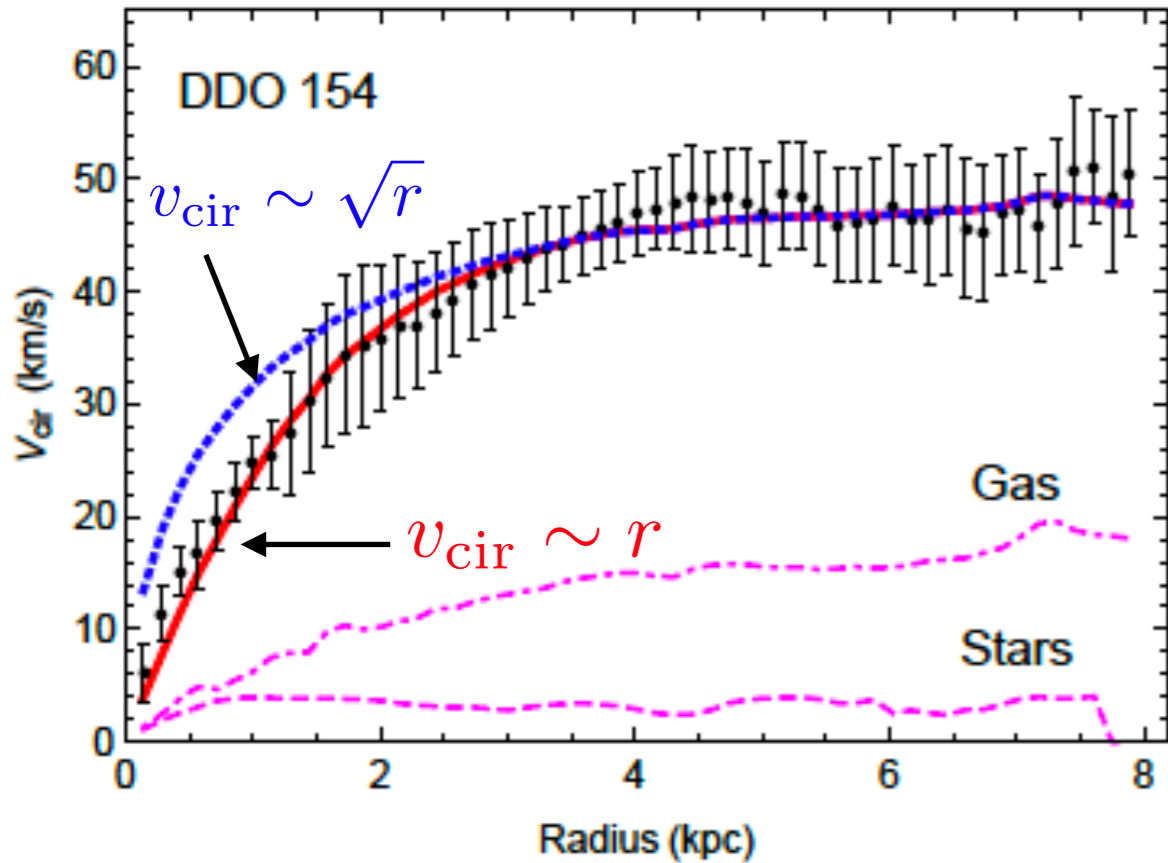
-3-



[M. Buckley, A. Peter, 1712.06615]

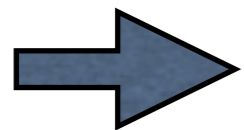
Astrophysics widens our view on dark matter:
WIMP, Axion, SIDM, etc, at colliders,
astrophysical observations, etc.

WIMP / CDM Crisis



[Spergel, Steinhardt, 2000; S.Tulin, H. Yu, 2017] DM-nucleon scattering

- **Core-cusp problem:** galaxy rotation curves in conflict with WIMP simulations at $< \text{kpc}$ scale.



Self-Interacting Dark Matter!

$$\frac{\sigma_{\text{self}}}{m_{\text{DM}}} \sim 1 \text{ cm}^2/\text{g}$$

Best candidate: light dark matter with sub-GeV mass.

Challenging for direct detection!

Light DM detection

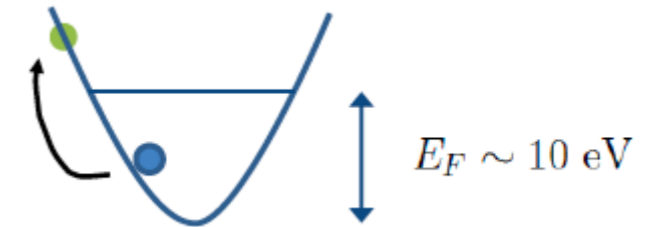
-5-

- DM-electron scattering is sensitive to light dark matter.

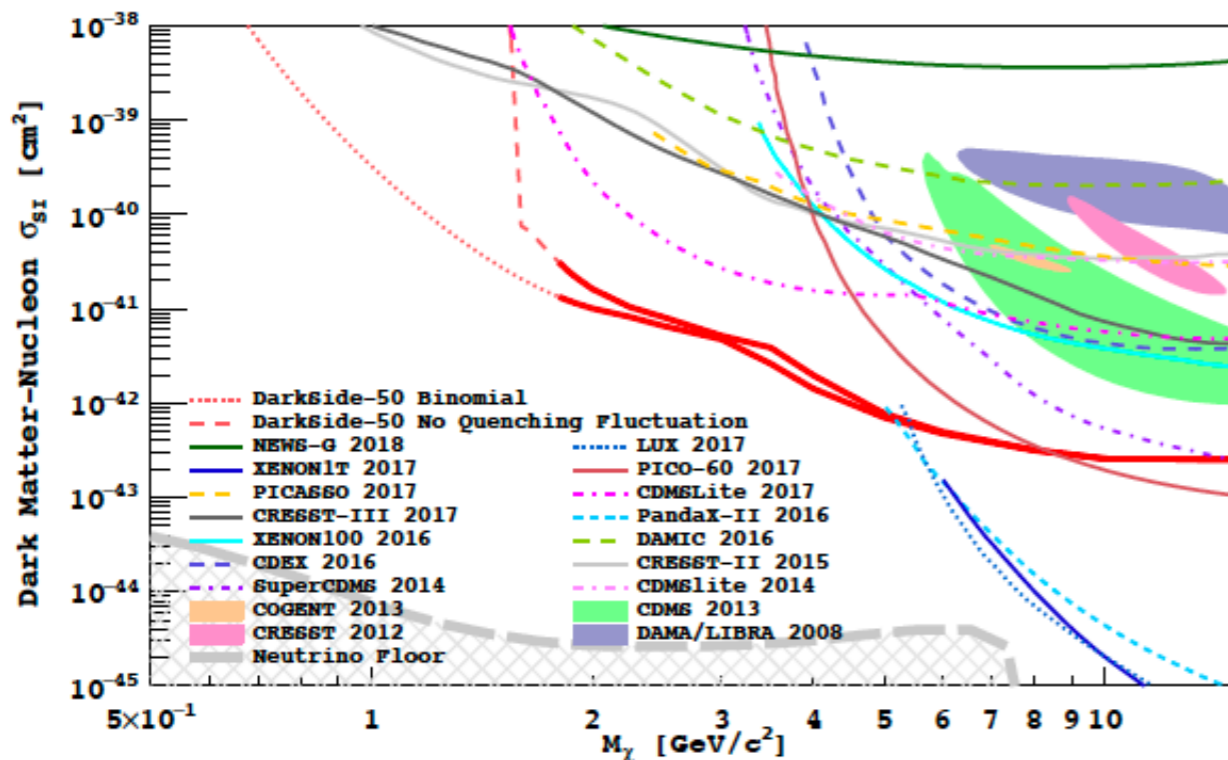
$$E_R \sim \frac{\mu^2 v_{\text{rel}}^2}{m_e} \sim m_e v_{\text{rel}}^2 \sim 0.3 \text{ eV} - 20 \text{ eV}$$

[Hochberg et al (2015)]

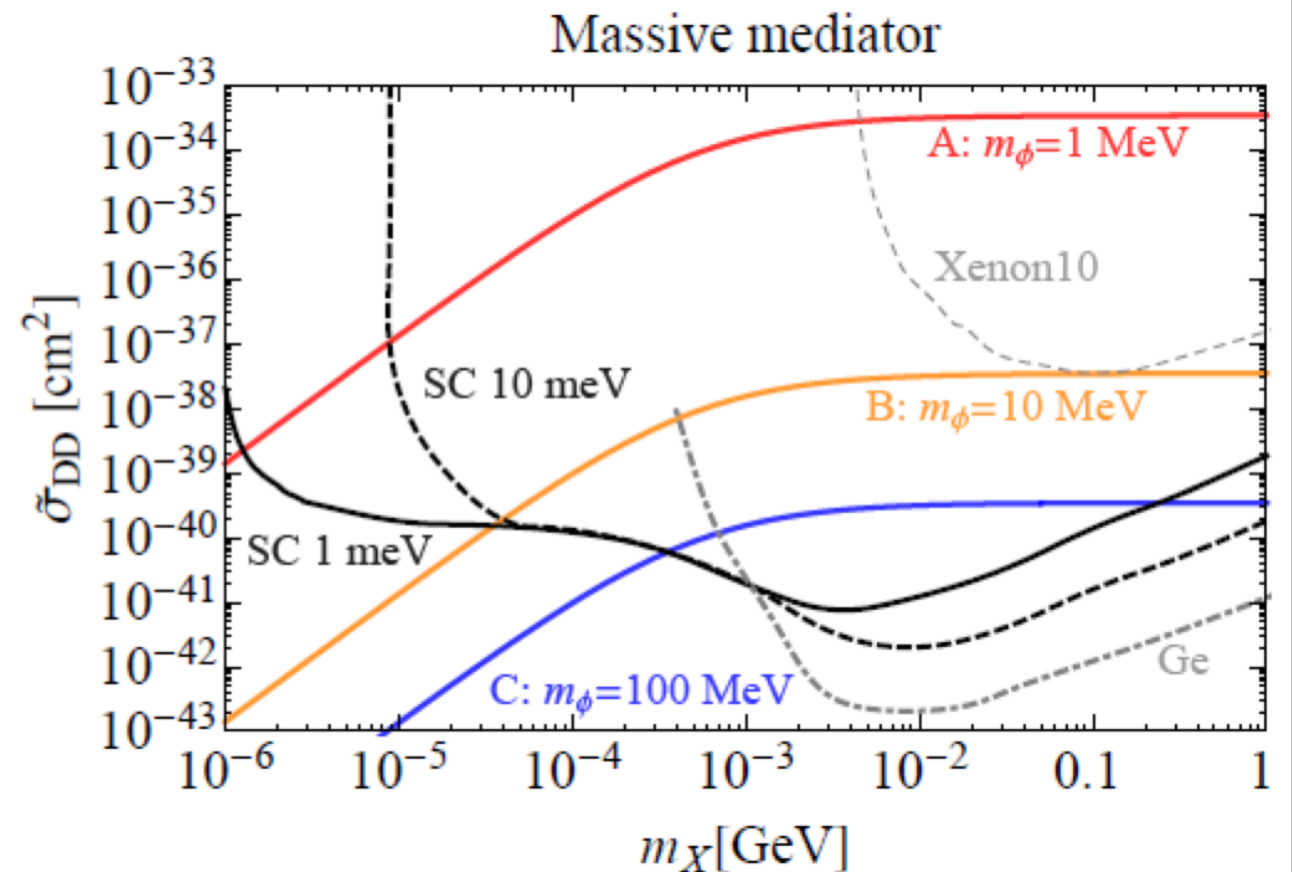
Cooper-pair breaking $m_{\text{DM}} v^2 \gtrsim \Delta \sim \text{meV}$



e.g. Al: $E_F = 11.7 \text{ eV}$, $v_{\text{rel}} \sim v_F \sim 10^{-2}$



DM-nucleon scattering

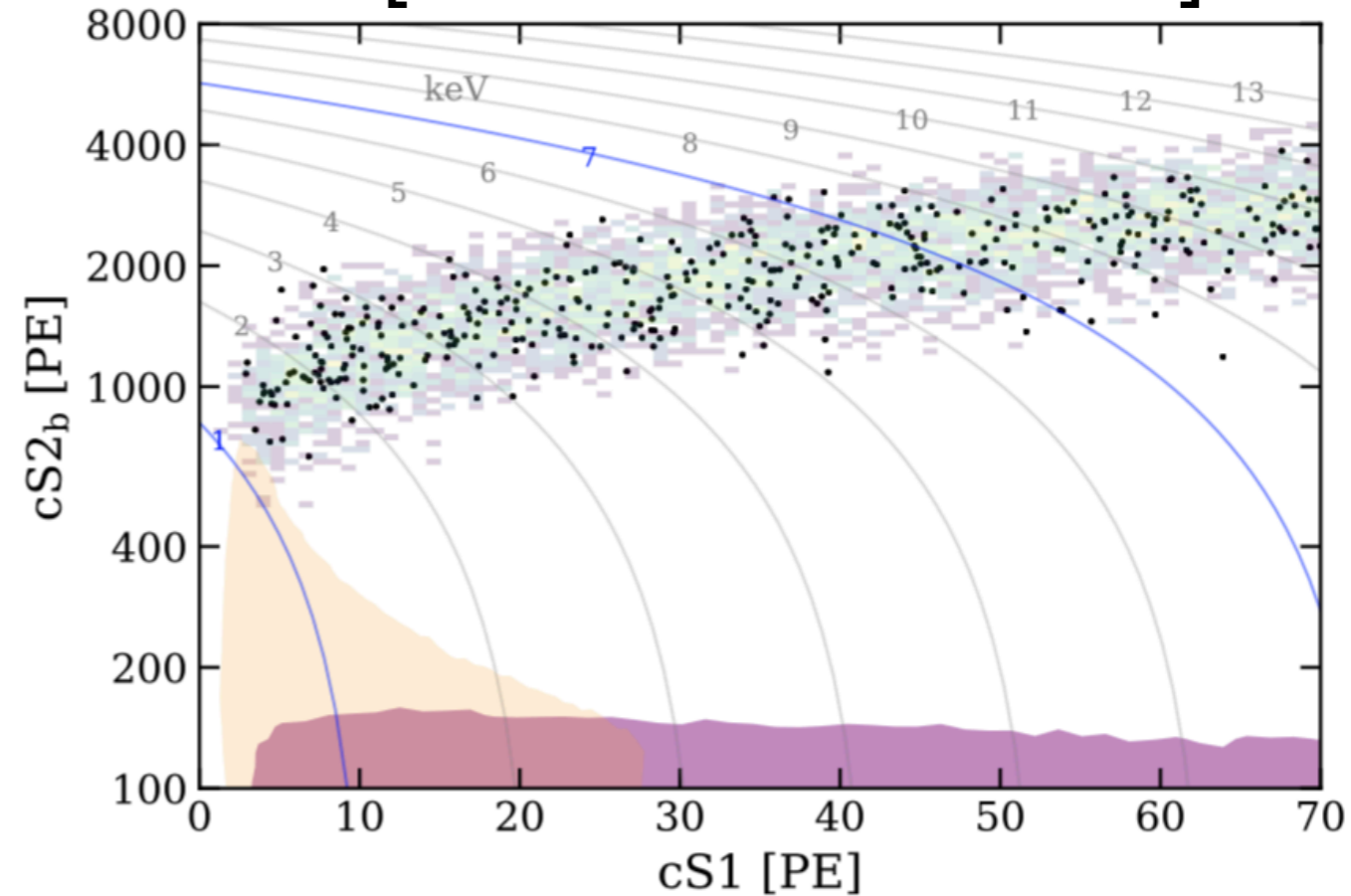
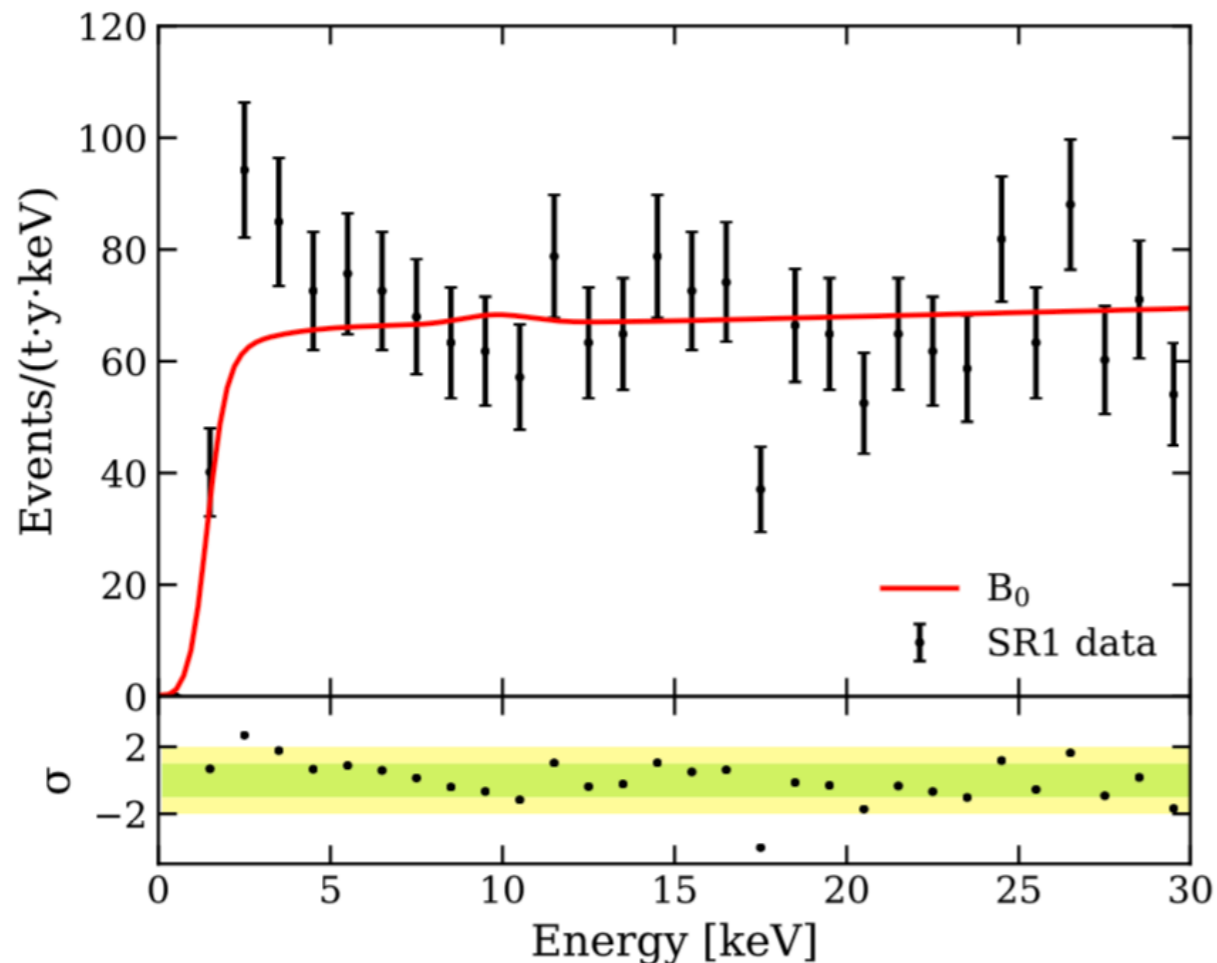


DM-electron scattering

XENONIT electron recoil

- Excess in electron recoil spectrum.

[XENONIT, 2006.0972 I]



$E_R = 1-7\text{keV}$: 285 events observed,
 232 ± 15 expected

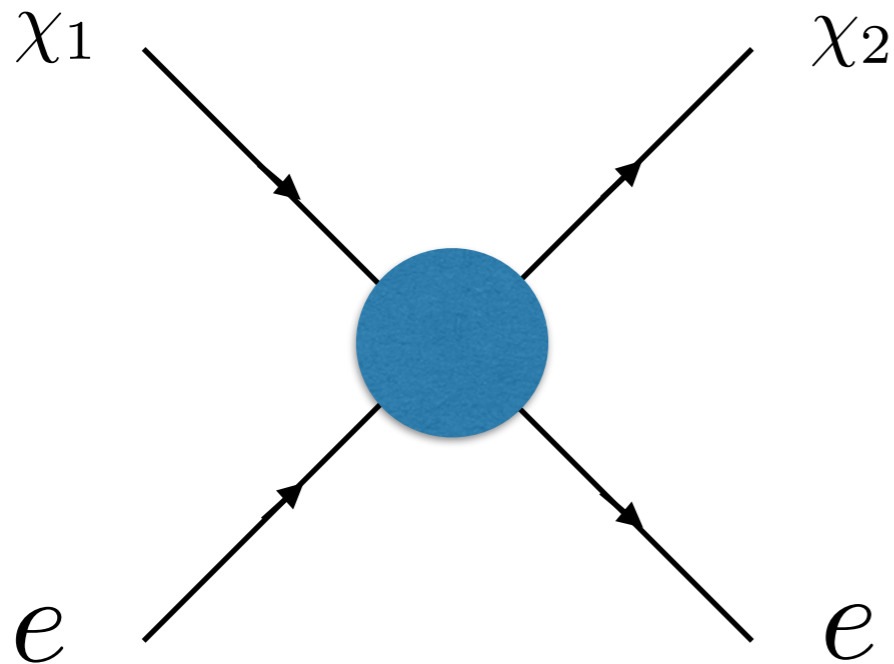


3.3σ deviation:
 most significant at
 $E_R = 2-3\text{keV}$

cf. Other backgrounds: Unknown Tritium, Ar37

Exothermic dark matter

-7-



[K. Harigaya et al; HML; J. Bramante et al; Essig et al; S. Choi, HML, B. Zhu]

$$\Delta m = m_{\chi_1} - m_{\chi_2} \gg m_e v^2$$

➔ $E_R \sim \Delta m \sim 2.5 \text{ keV}$

“Exothermic dark matter”

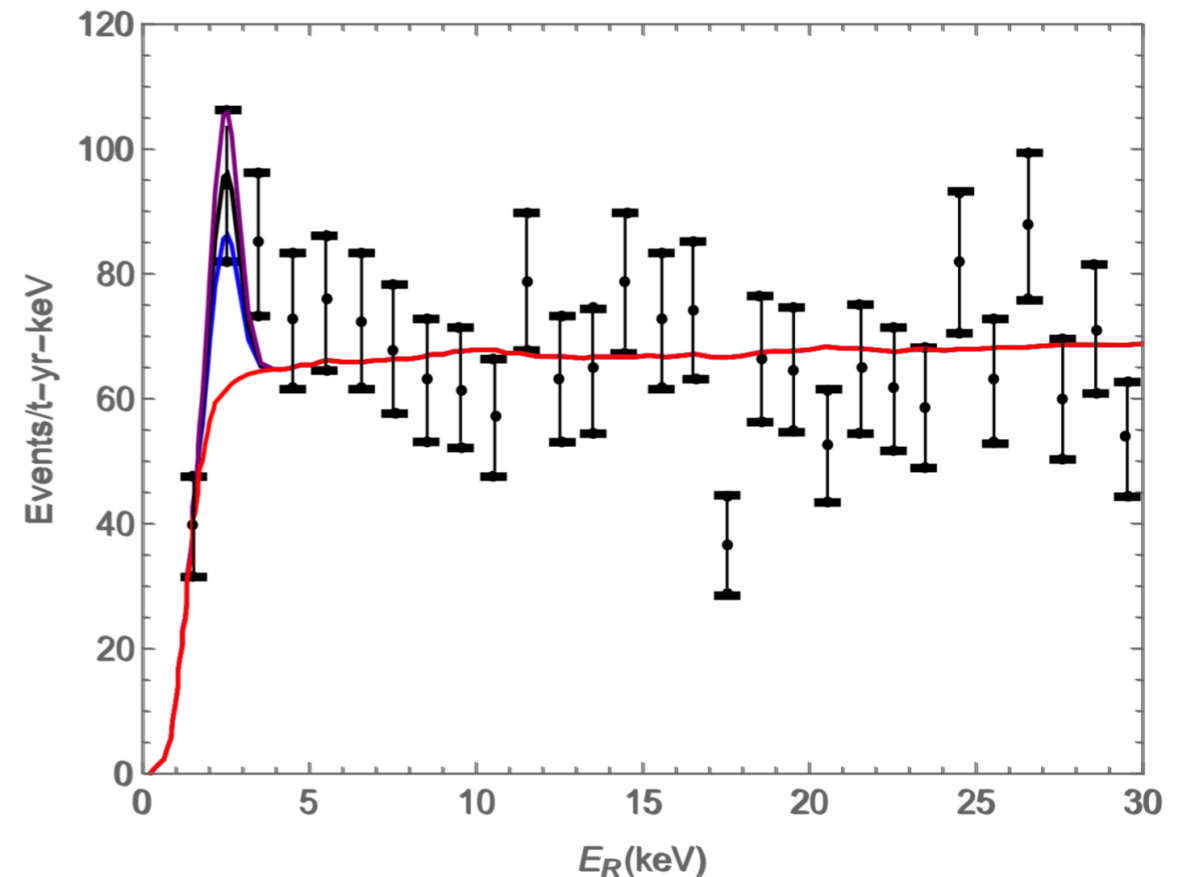
Monochromatic e-recoil energy

$$E_R \simeq \Delta m \left(1 - \frac{2}{\sqrt{\kappa}} \cos \theta \right)$$

$$\kappa = \frac{2\Delta m}{m_e v^2} \gg 1$$

Cross section

$$\bar{\sigma}_e / m_{\chi_1} \simeq 10^{-43} \text{ cm}^2 / \text{GeV}$$



Model for exothermic DM

-8-

- Two DM states and electron with Z' mediator:

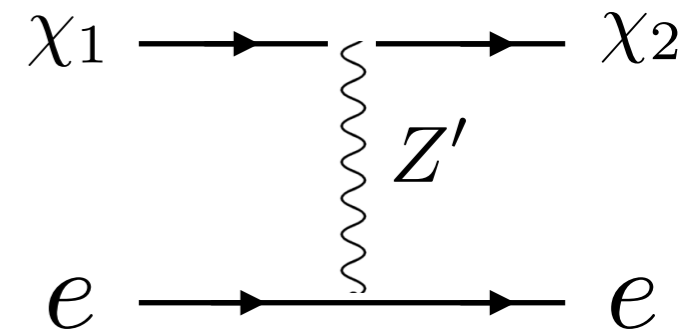
$$\mathcal{L}_{\text{eff}} = \left(g_{Z'} Z'_\mu \bar{\chi}_2 \gamma^\mu (v_\chi + a_\chi \gamma^5) \chi_1 + \text{h.c.} \right) + g_{Z'} Z'_\mu \bar{e} (v_e + a_e \gamma^5) e + g_{Z'} Z'_\mu \bar{\nu} \gamma^\mu (v_\nu + a_\nu \gamma^5) \nu$$

[HML, 2020]

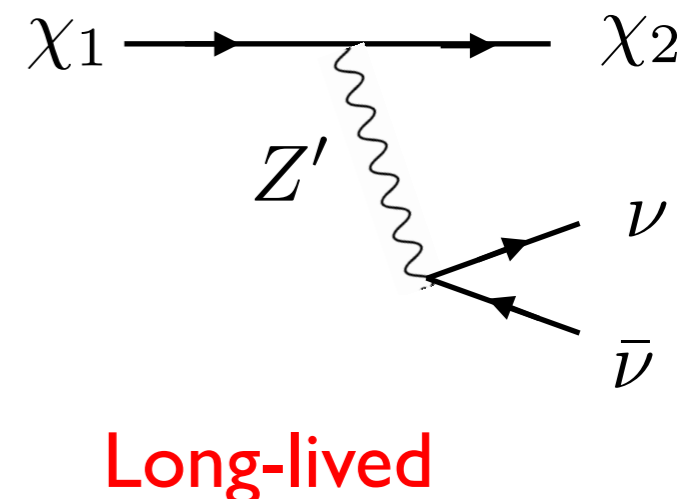
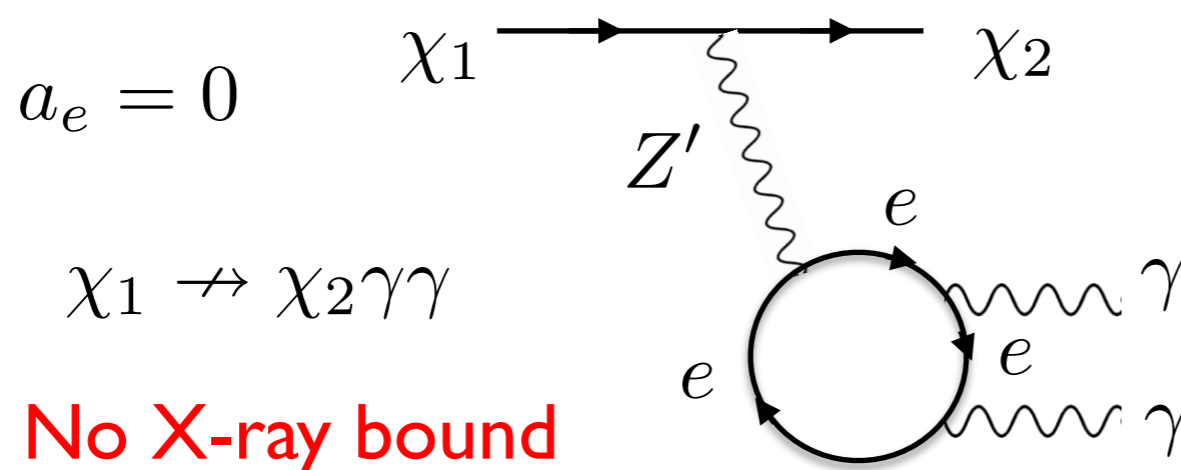
- DM-electron inelastic cross section:

$$\bar{\sigma}_e \simeq \frac{v_\chi^2 v_e^2 g_{Z'}^4 \mu_1^2}{\pi m_{Z'}^4}$$

$$\simeq \left(\frac{v_\chi g_{Z'}}{0.6} \right)^2 \left(\frac{v_e g_{Z'}}{10^{-4} e} \right)^2 \left(\frac{600 \text{ MeV}}{m_{Z'}} \right)^4 \left(\frac{\mu_1}{m_e} \right)^2 \times 10^{-43} \text{ cm}^2$$



- Long-lived heavy DM state:

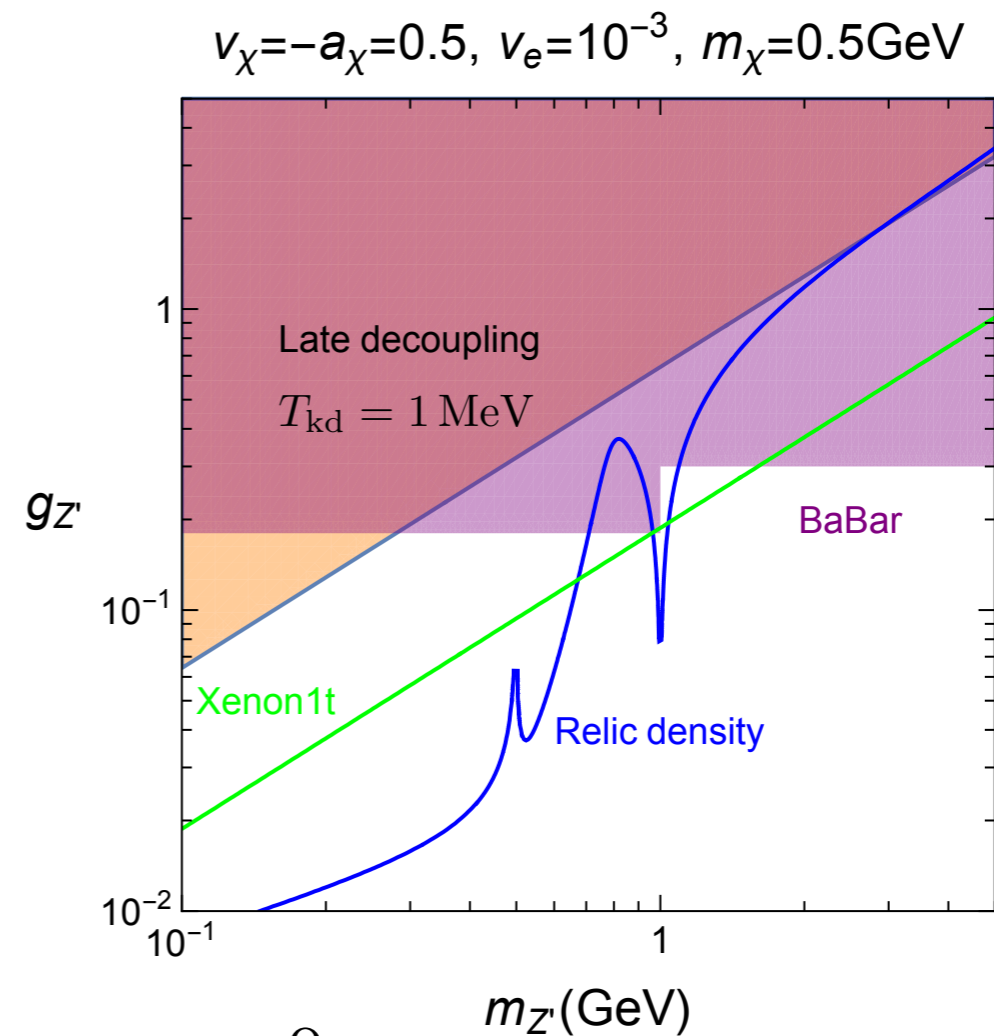
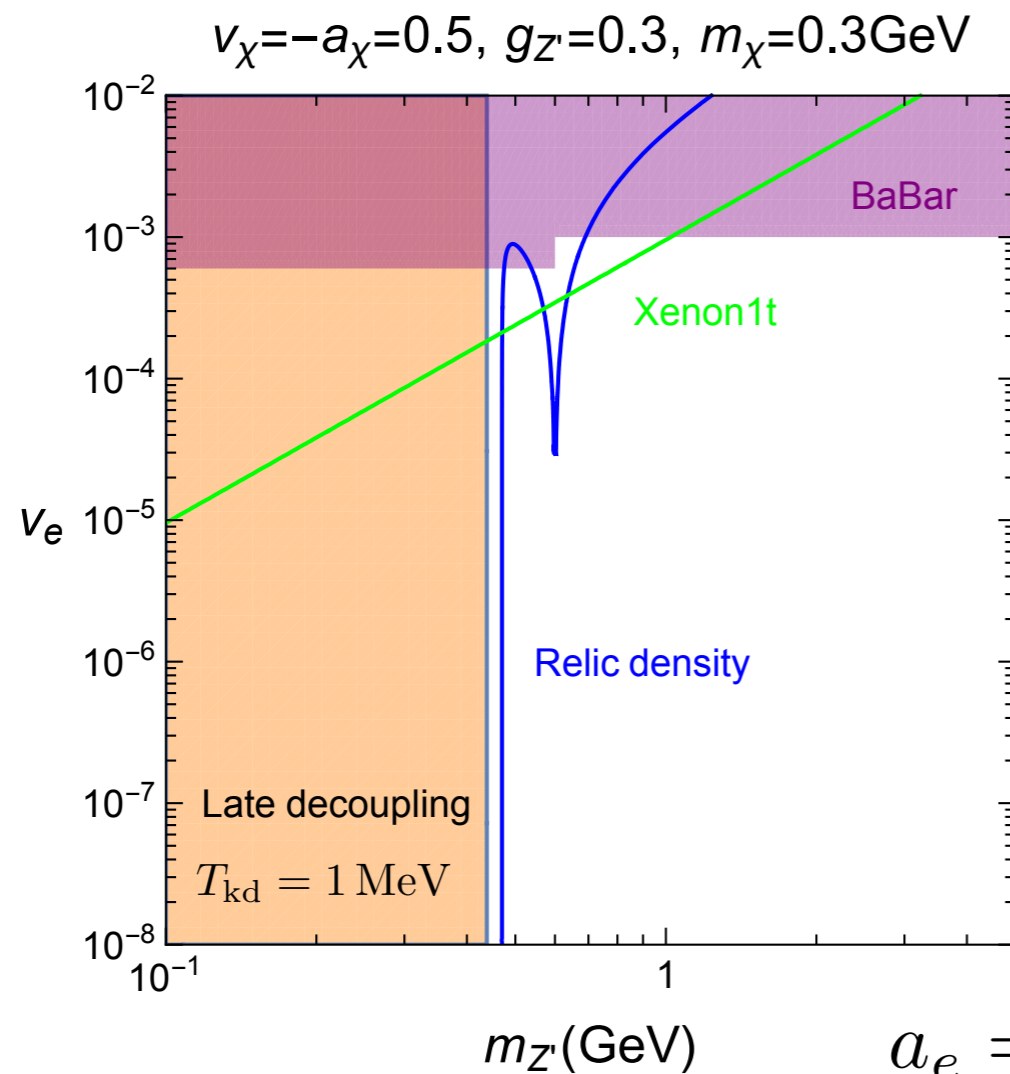


XENONIT + DM relic

-9-

- Electron couplings are constrained by visible/invisible searches at BaBar, beam dump, meson decays, Belle-2.

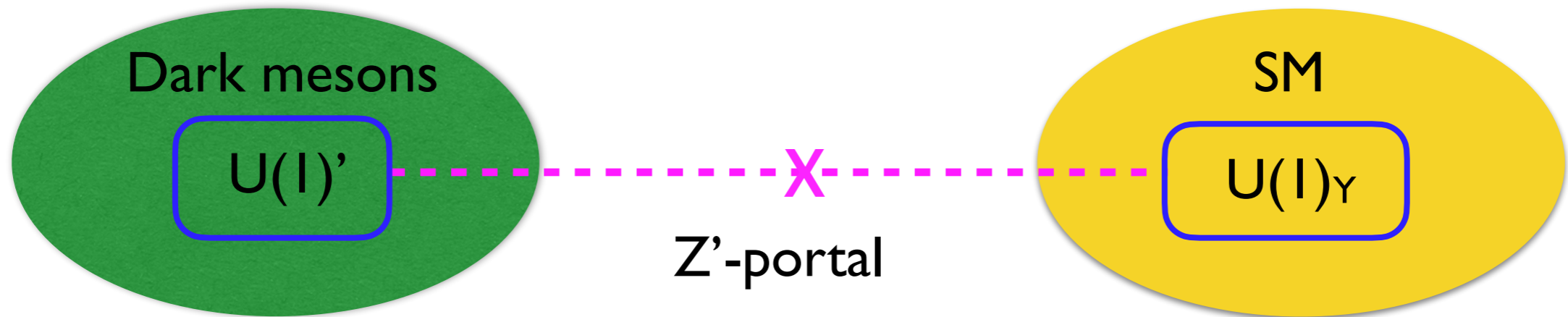
$$m_{Z'} \lesssim 10 \text{ GeV} \quad \longrightarrow \quad |v_e| g_{Z'} \lesssim (10^{-4} - 10^{-3}) e$$



$$a_e = v_\nu = a_\nu = 0$$

Dark mesons & Z'-portal

-10-



- Dark mesons from hidden QCD = dark matter

“Dark flavor violation” split dark meson masses.

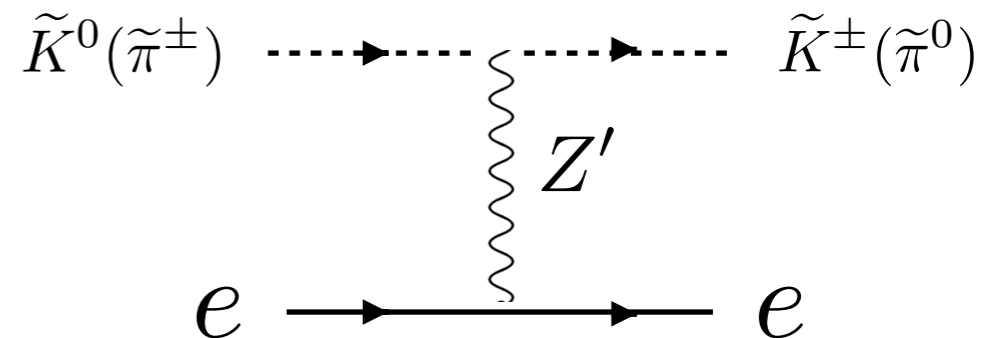
$$\mathcal{L}_{\text{mix}} = -y_{12} \phi \bar{u}' d' - y_{13} \phi \bar{u}' s' - \text{h.c.}$$

[HML, M. Seo, 2015;
S.Choi, HML, B. Zhu, 2012.03713]

➔ $m_{\tilde{K}^0} - m_{\tilde{K}^\pm} \simeq \Delta m, \quad m_{\tilde{\pi}^\pm} - m_{\tilde{\pi}^0} \simeq \frac{1}{\sqrt{3}} \Delta m.$

- Non-universal Z' portal:

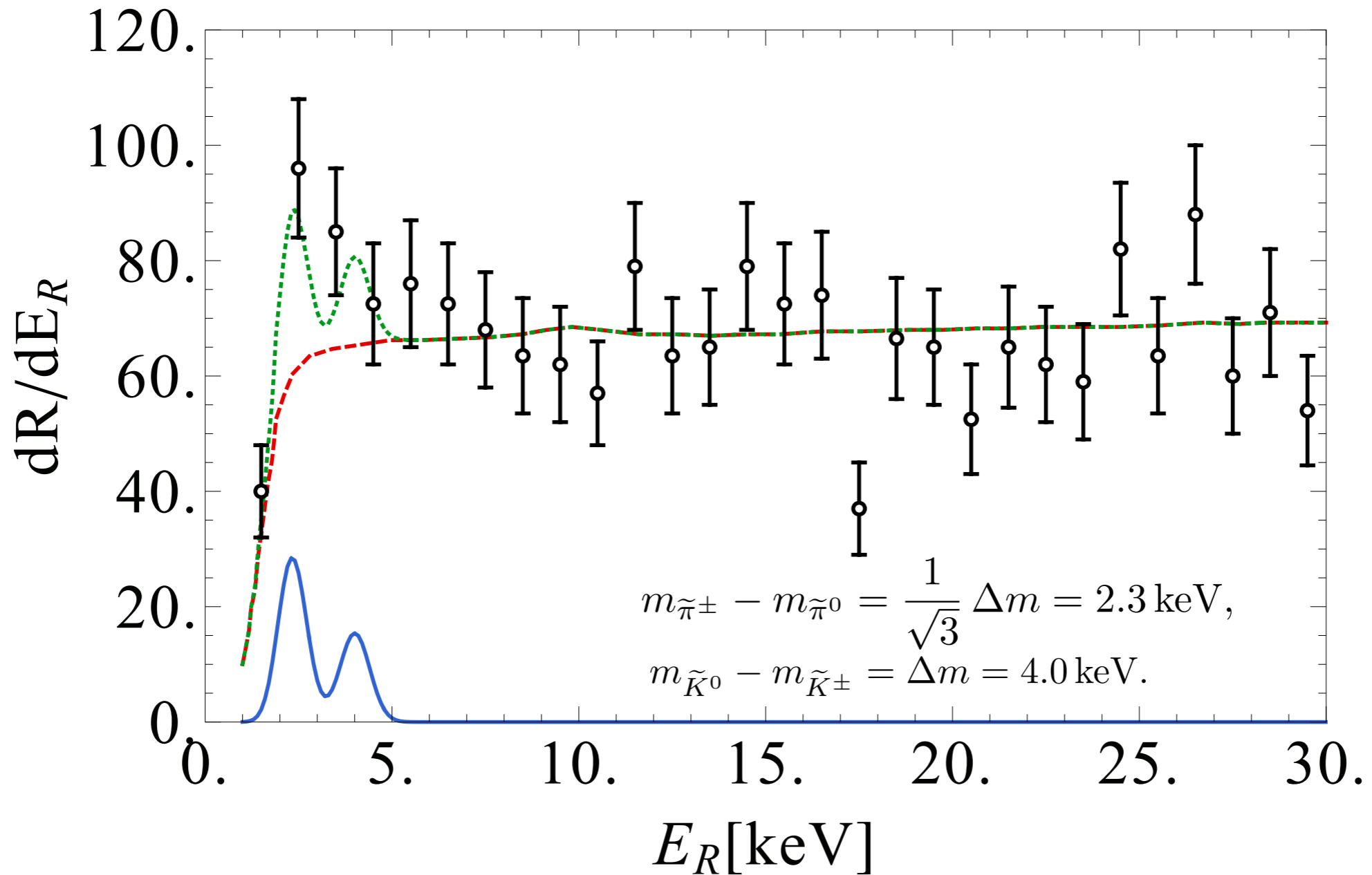
Dark meson-changing Z'
=> exothermic dark matter



Electron E_R from dark mesons

-11-

[S.Choi, HML, B. Zhu, 2012.03713]



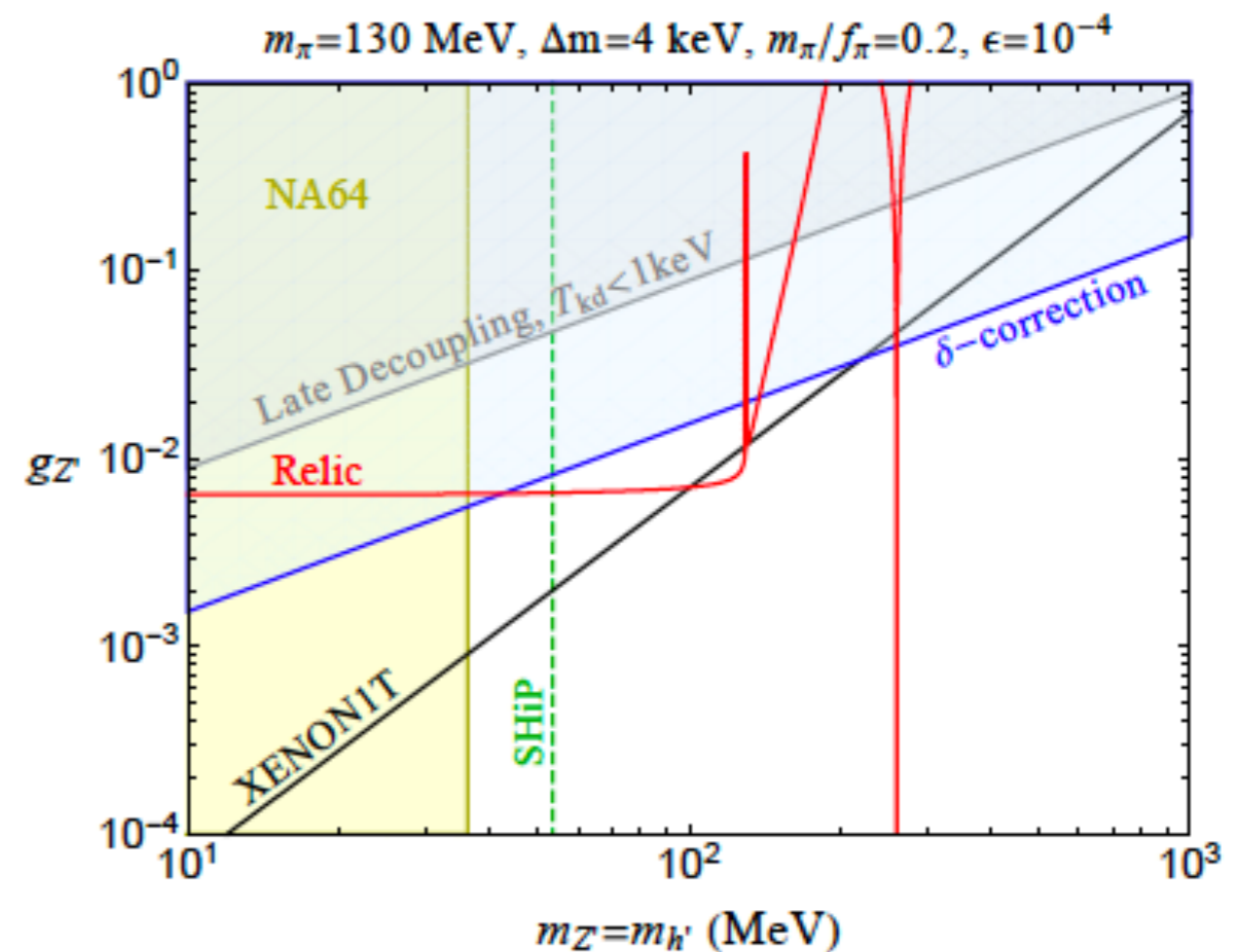
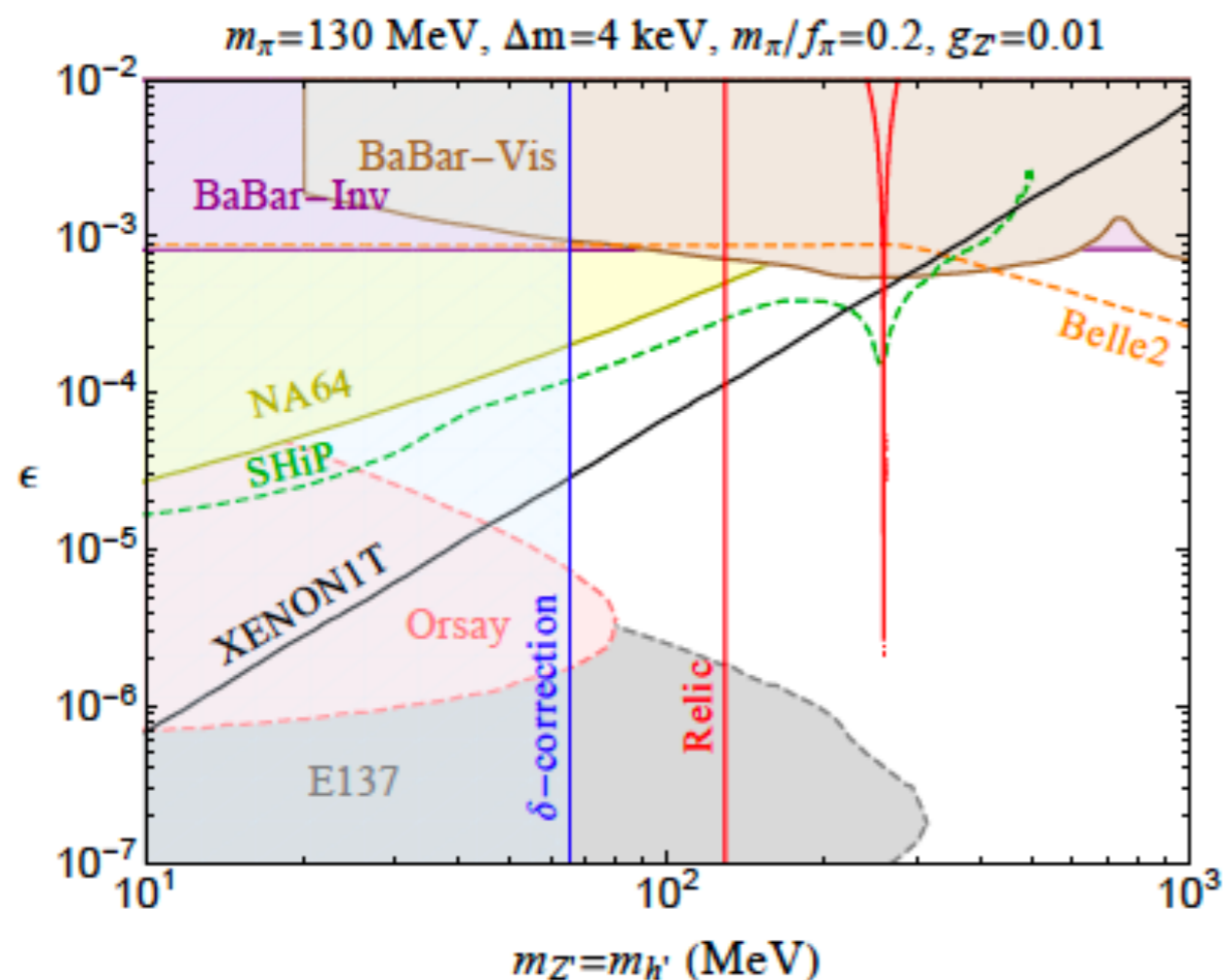
Double-peak case fits better than one-peak case.

Dark mesons & XENONIT

-12-

- Almost degenerate dark Higgs/ Z' masses can be searched in intensity experiments such as Belle-2.

[S.Choi, HML, B. Zhu, 2020]



Exothermic dark matter with larger mass splitting can lead to displaced vertices at Belle-2.

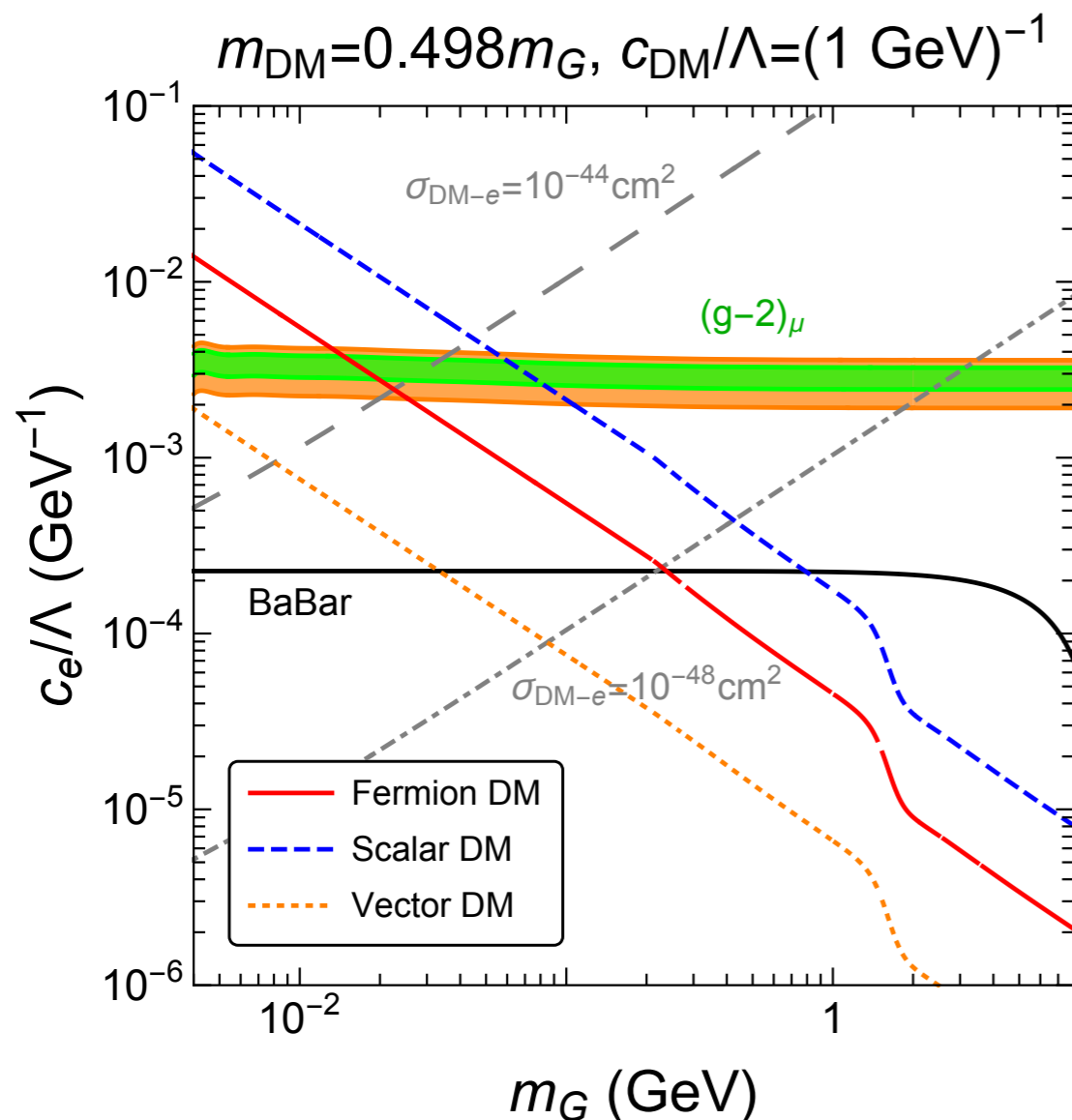
cf. M. Duerr et al, 2012.08595;
D.W. Kang et al, 2101.02503

Other portals to light DM

-13-

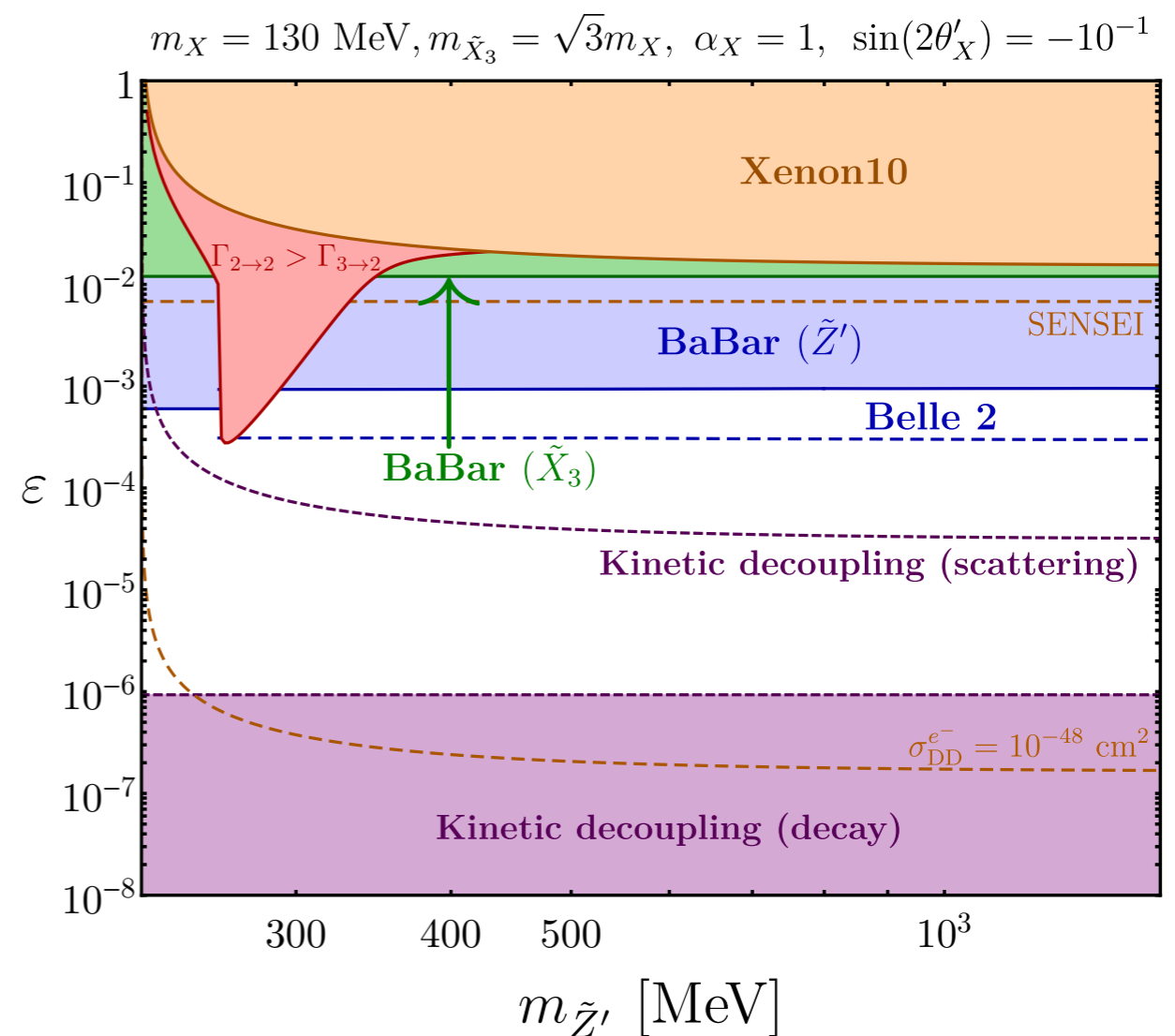
- Other portals such as spin-2, axion, ...; DM spins

Spin-2 mediator



[Y. Kang, HML, 2020]

Non-abelian DM



[S. Choi, HML, Y. Mambrini, M. Pierre, 2019]

B-meson anomalies and new physics

Flavors and new physics

-14-

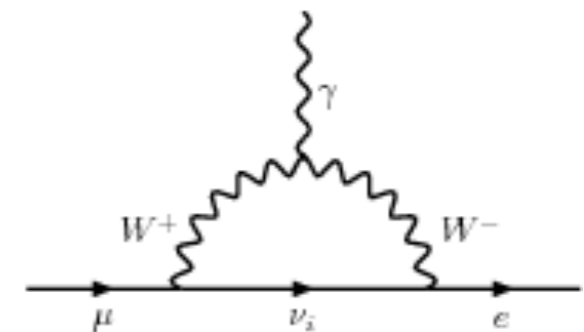
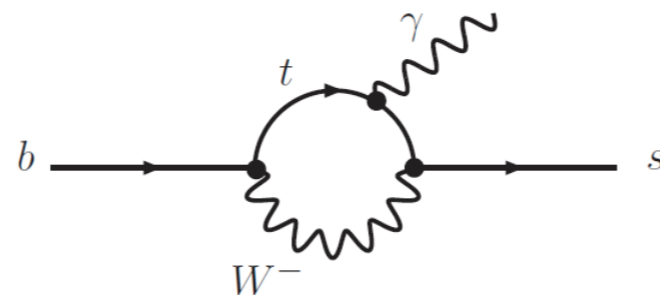
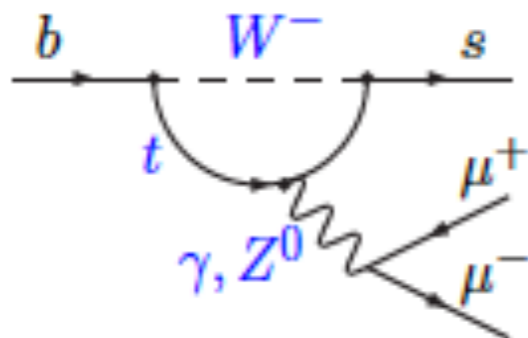
- “Charged currents” induce flavor violating processes at tree level, while FCNCs are induced at loop level.

$$\frac{-g}{\sqrt{2}}(\bar{u}_L, \bar{c}_L, \bar{t}_L)\gamma^\mu W_\mu^+ V_{\text{CKM}} \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} + \text{h.c.}, \quad V_{\text{CKM}} \equiv V_L^u V_L^{d\dagger} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}.$$

- Lepton universality is well tested in the SM.

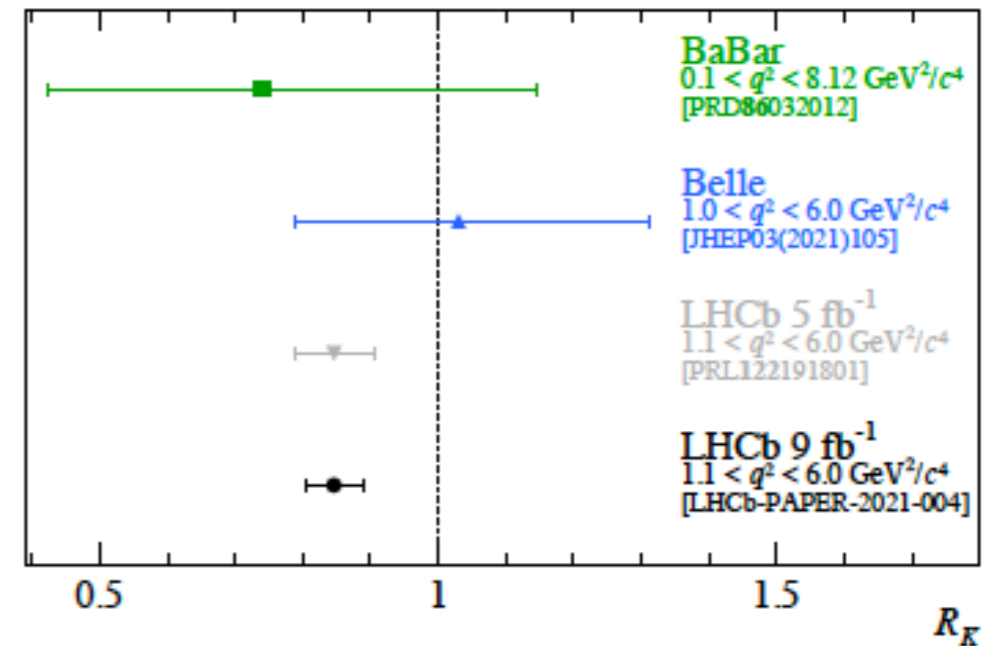
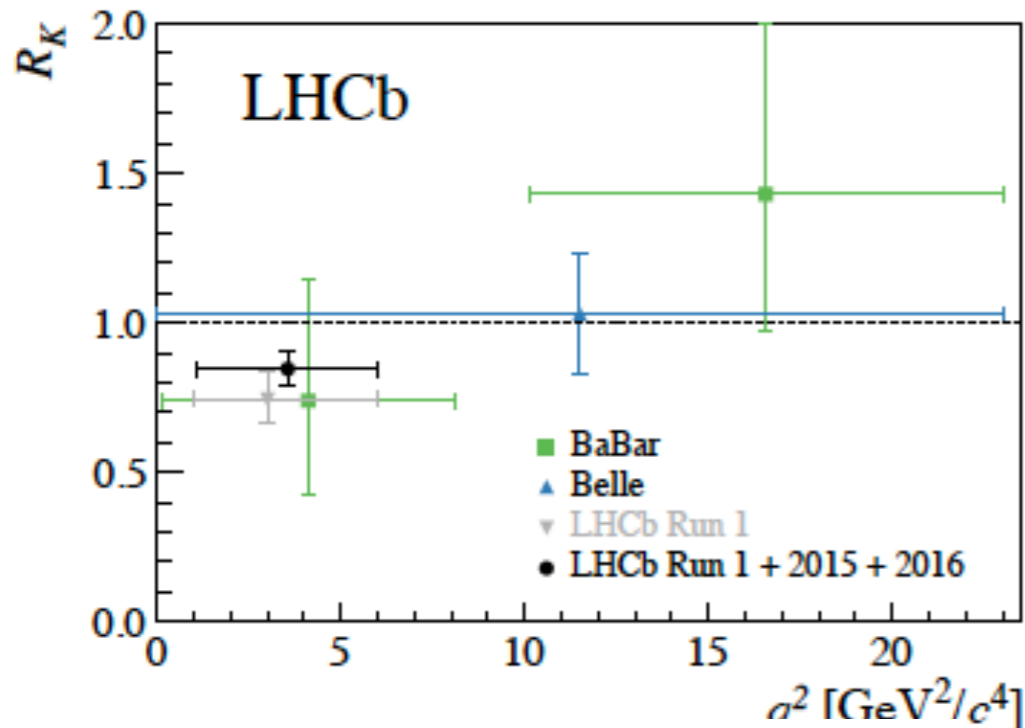
$$\frac{\Gamma_{Z \rightarrow \mu^+ \mu^-}}{\Gamma_{Z \rightarrow e^+ e^-}} = 1.0009 \pm 0.0028, \quad \frac{\mathcal{B}(W^- \rightarrow e^- \bar{\nu}_e)}{\mathcal{B}(W^- \rightarrow \mu^- \bar{\nu}_\mu)} = 1.004 \pm 0.008. \quad \frac{\Gamma_{K^- \rightarrow e^- \bar{\nu}_e}}{\Gamma_{K^- \rightarrow \mu^- \bar{\nu}_\mu}} = (2.488 \pm 0.009) \times 10^{-5}$$

- “FCNC processes” and lepton universality are sensitive probes of new physics.



B-anomalies at LHCb

-15-



$$R_K = \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\Gamma[B^+ \rightarrow K^+ \mu^+ \mu^-]}{dq^2} dq^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\Gamma[B^+ \rightarrow K^+ e^+ e^-]}{dq^2} dq^2}$$

$$R_K^{[1.1,6.0]} = 1.00 \pm 0.01 \quad (\text{SM})$$

Hadronic uncertainties cancelled \Rightarrow Clean test of LFU

LHCb: 2011~2016 data

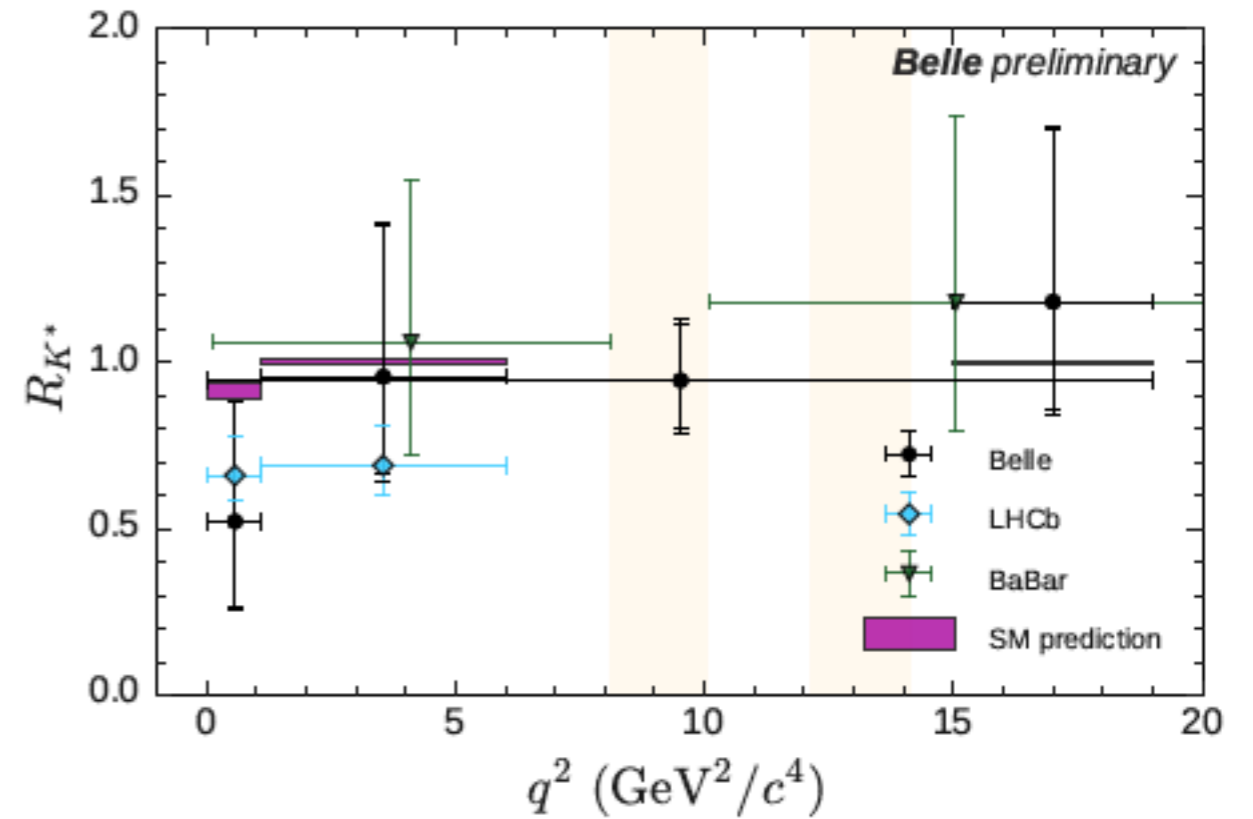
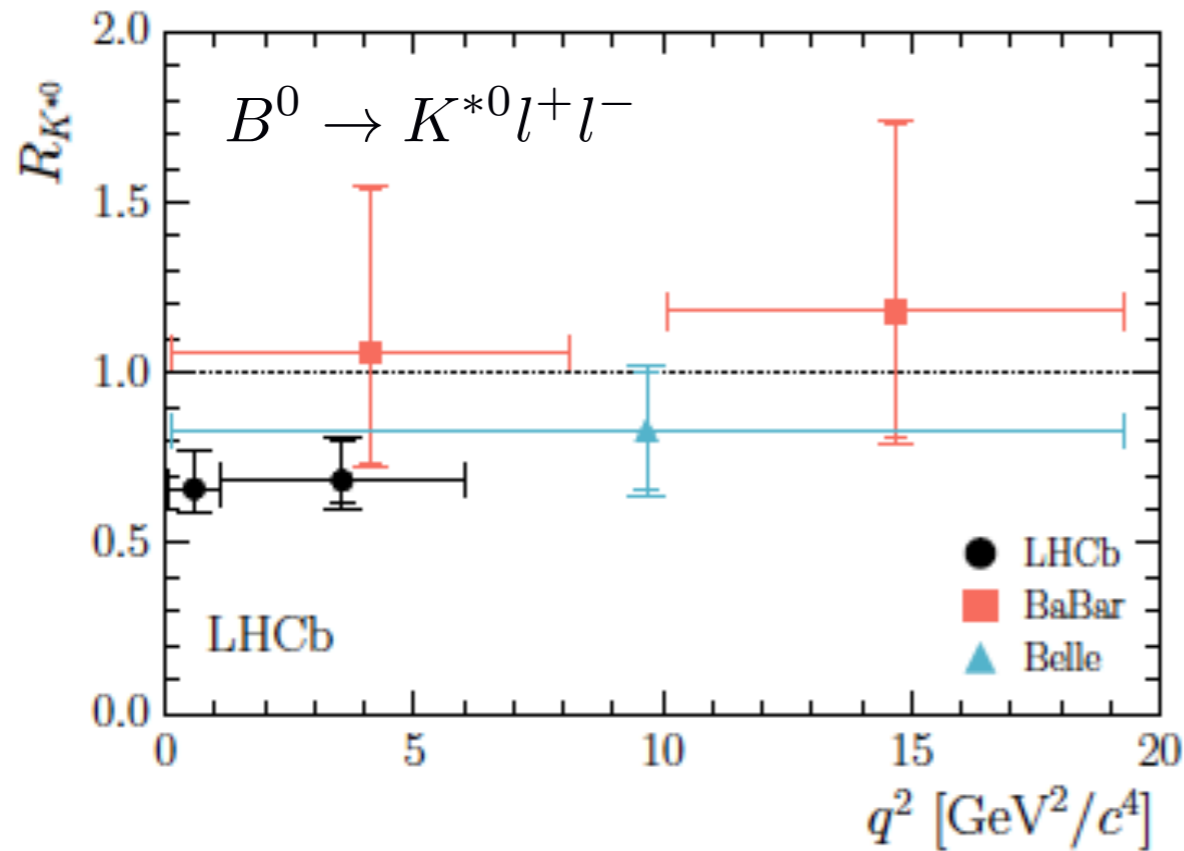
$$R_K = 0.846^{+0.060}_{-0.054} (\text{stat.})^{+0.016}_{-0.014} (\text{syst.}) \sim 2.5\sigma$$

2017~2018 data \Rightarrow

$$R_K = 0.846^{+0.042}_{-0.039} (\text{stat})^{+0.013}_{-0.012} (\text{syst}) \sim 3.1\sigma$$

B-anomalies at LHCb

-16-

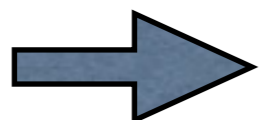


LHCb Preliminary	low- q^2	central- q^2
$\mathcal{R}_{K^{*0}}$	$0.660 \pm_{-0.070}^{+0.110} \pm 0.024$	$0.685 \pm_{-0.069}^{+0.113} \pm 0.047$
95% CL	[0.517–0.891]	[0.530–0.935]
99.7% CL	[0.454–1.042]	[0.462–1.100]

$$R_{K^*}^{[1.1,6.0]} = 1.00 \pm 0.01 \quad (\text{SM})$$

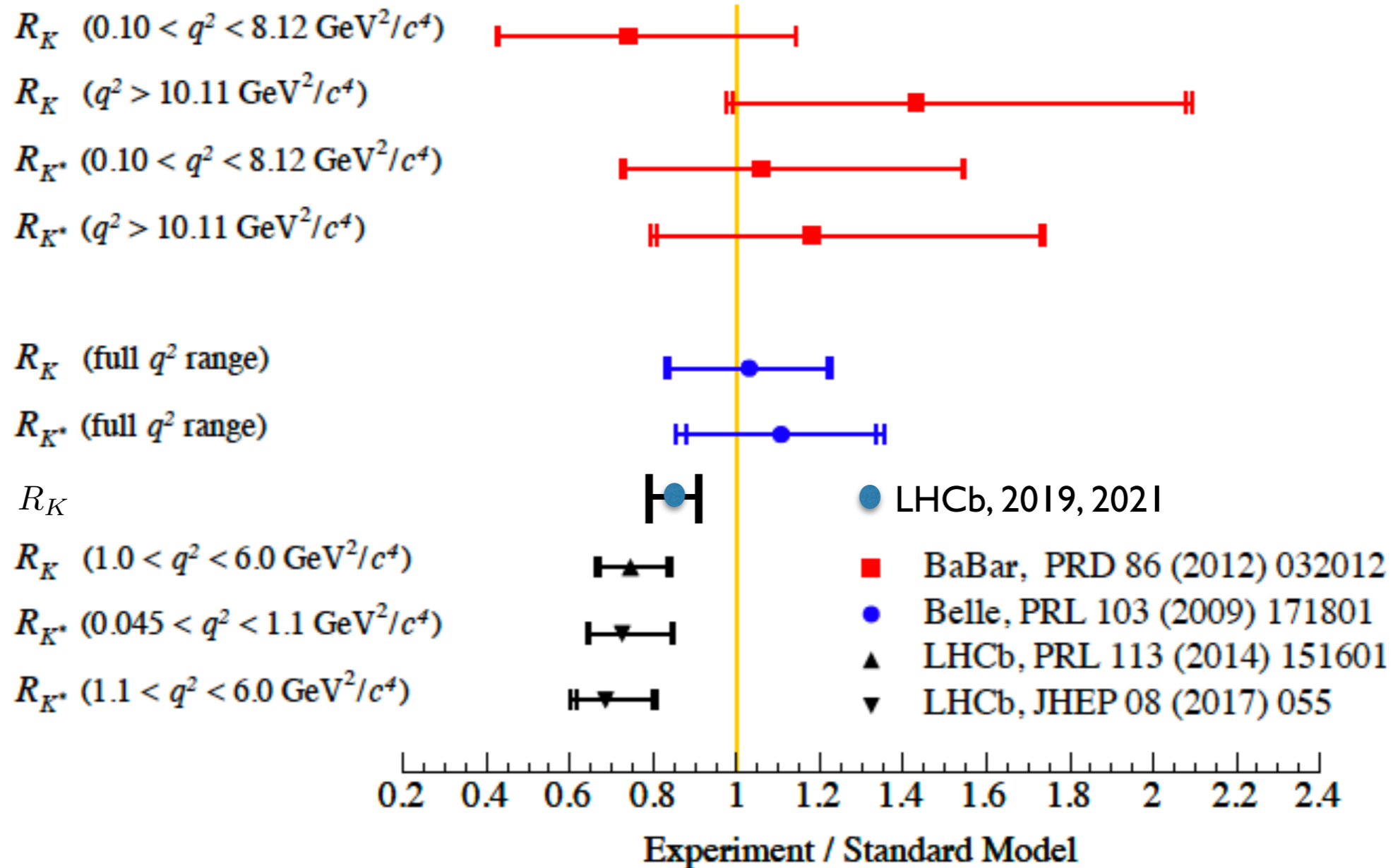
$$R_{K^*}^{[0.045,1.1]} = 0.906 \pm 0.028 \quad (\text{SM})$$

- R_{K^*} : 2.2-2.4 σ deviation and 2.4-2.5 σ deviation.



Hints for lepton flavor non-universality?

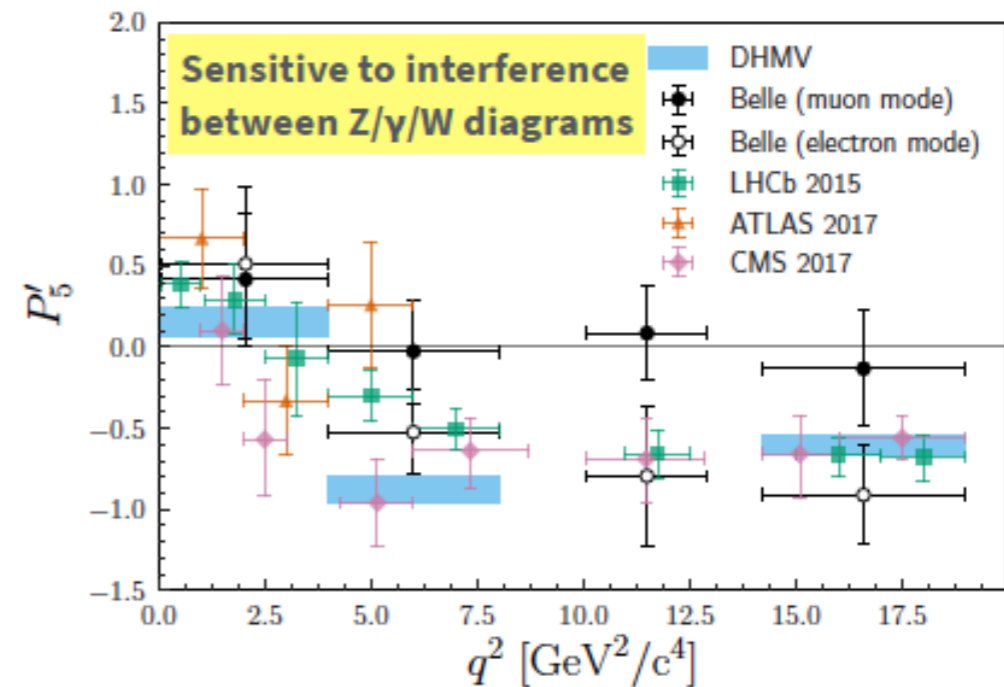
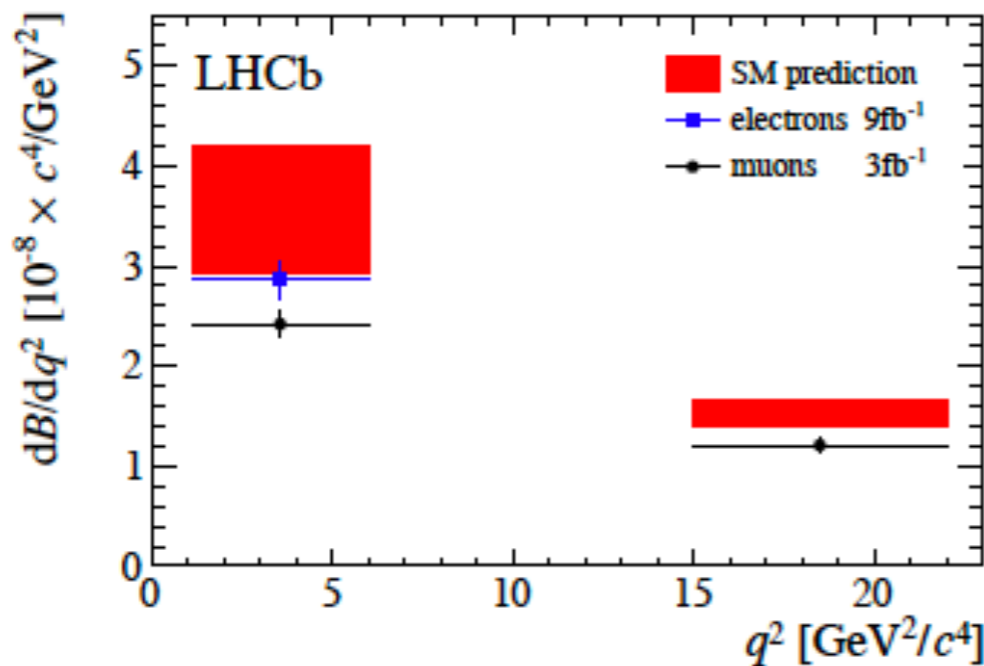
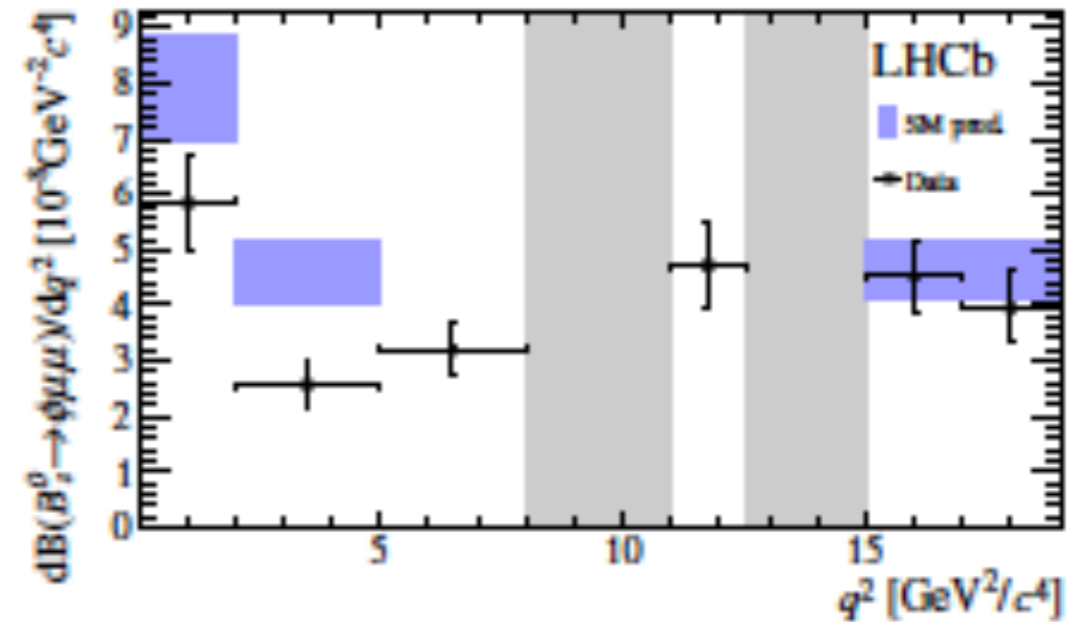
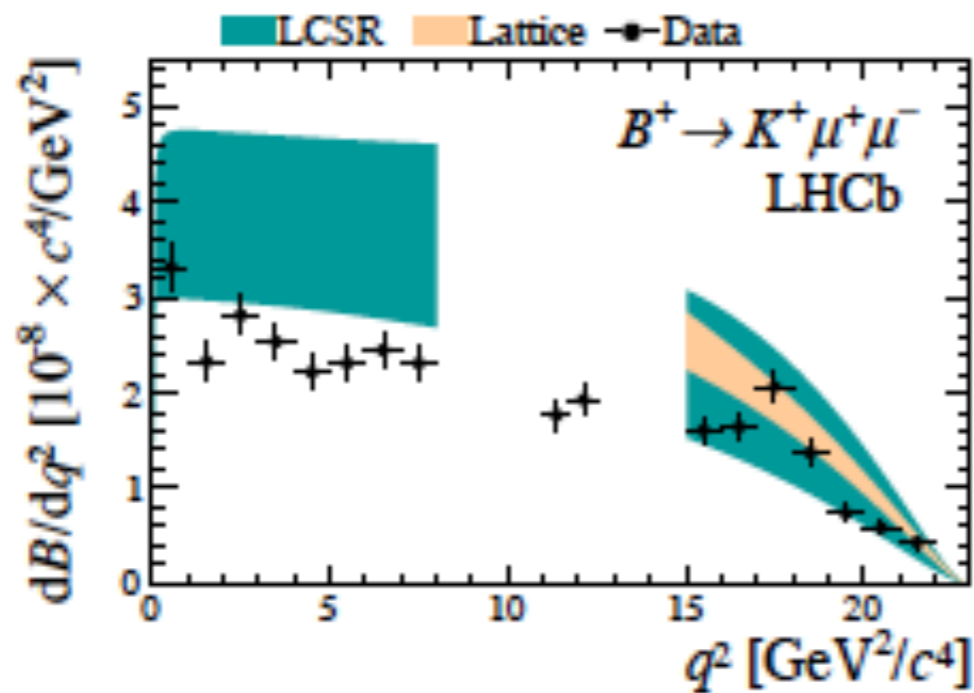
Summary of B-anomalies -17-



[S. Bifani et al, 1809.06229 + updates]

Muon less SM than electron

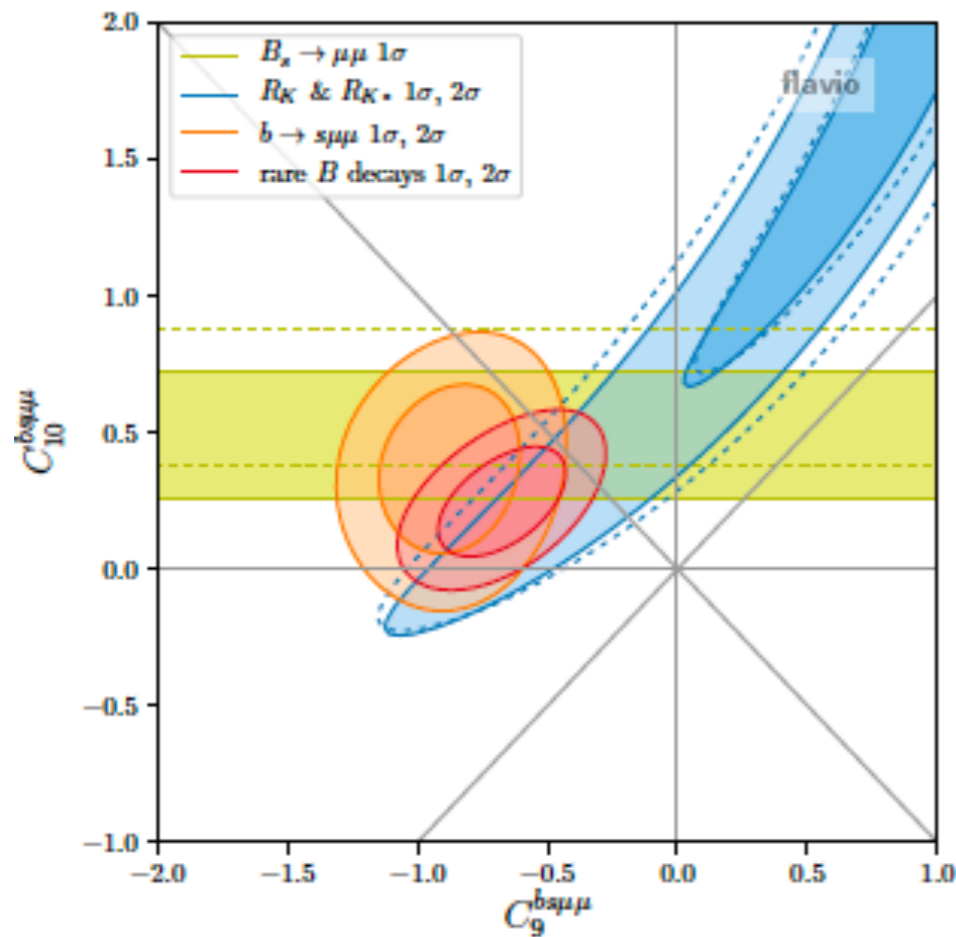
-18-



- Differential branching fractions & angular distribution are consistently lower than the SM values in muon channels.

Global fits

[Altmannshofer, Stangl, 2021]

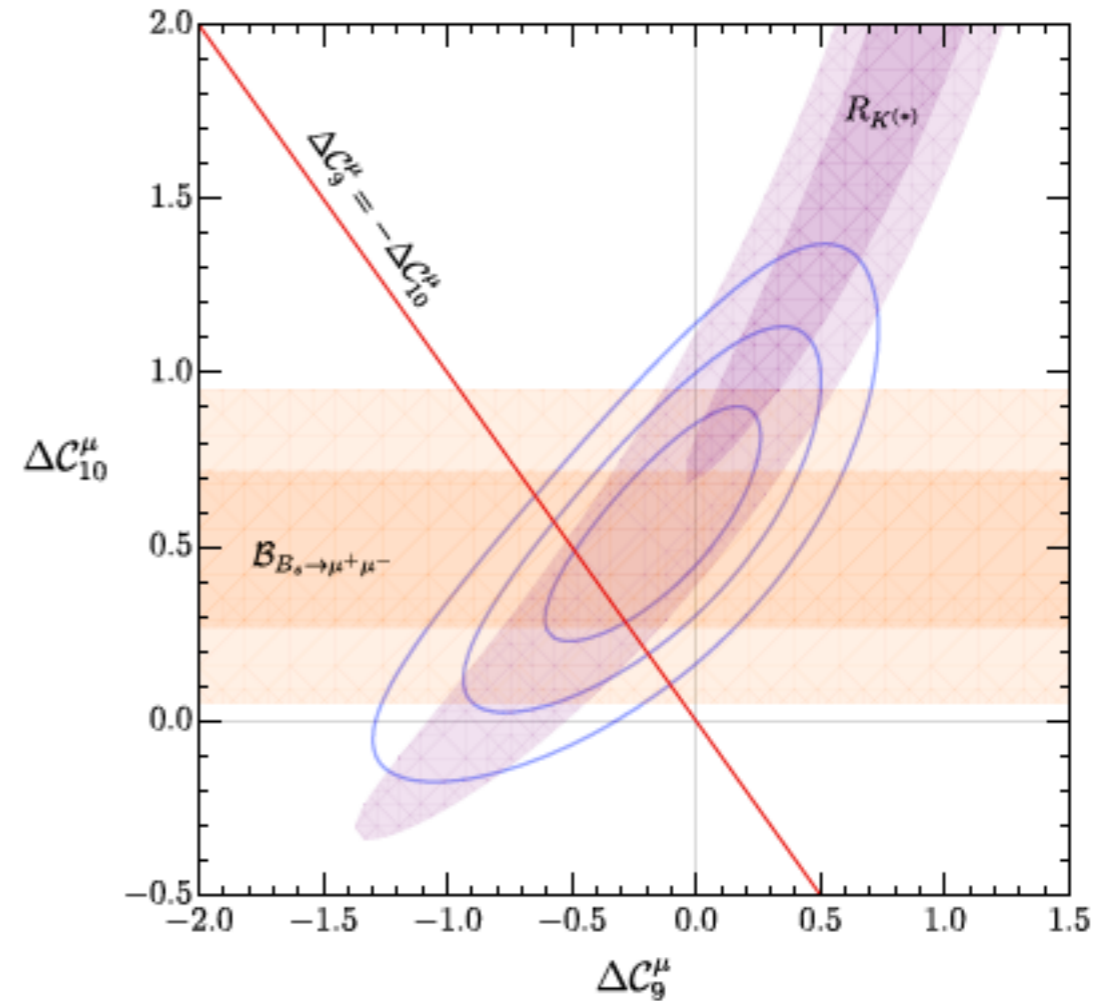


Best fit: $\sim 6.1\sigma$ from SM

$$C_9^{bs\mu\mu} \simeq -0.82$$

$$C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu} \simeq -0.43.$$

[Cornella et al, 2021]



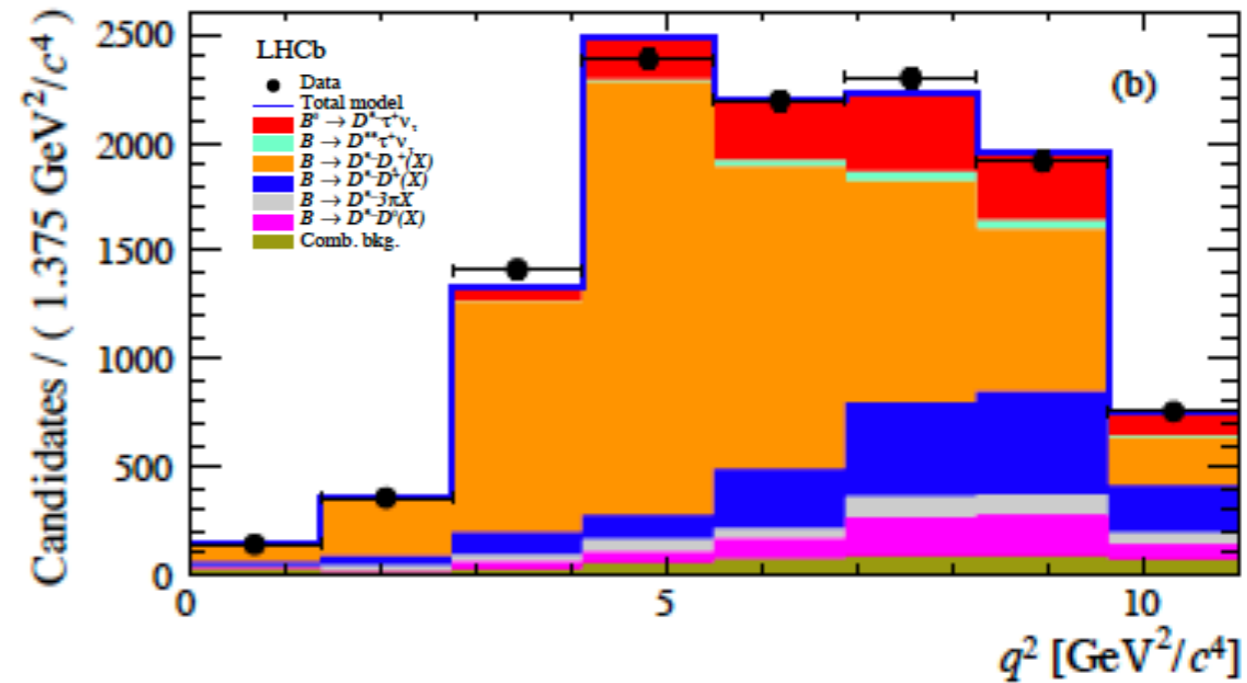
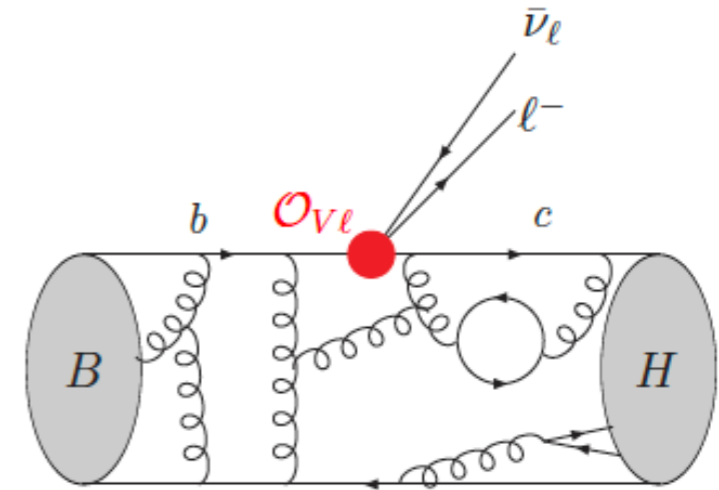
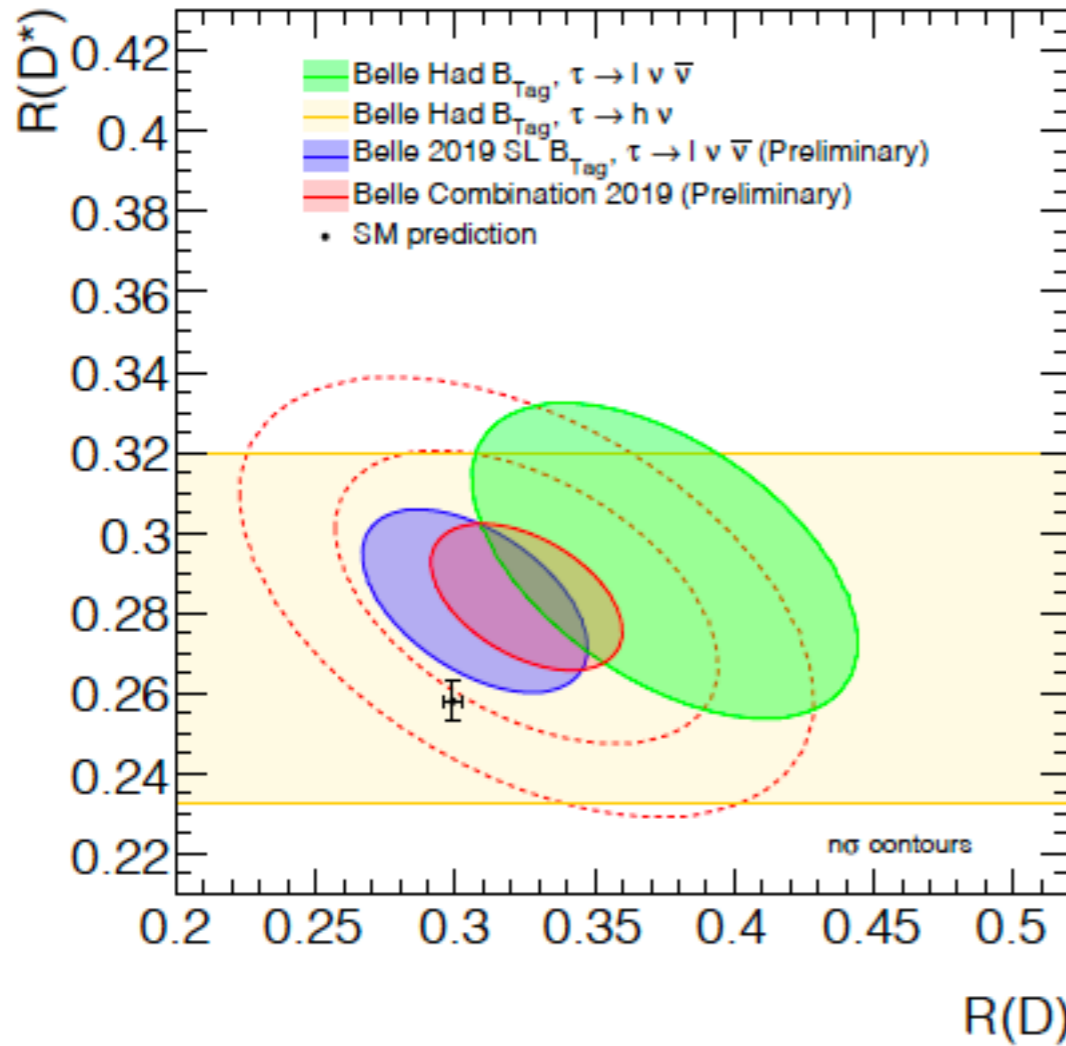
(Consistent with $B_s \rightarrow \mu^+ \mu^-$)

Z' models

Leptoquark models

$B \rightarrow D^{(*)} \tau \nu$

$$R_{D^*} = \mathcal{B}(B \rightarrow D^* \tau \nu) / \mathcal{B}(B \rightarrow D^* l \nu)$$



[Belle-II, 1808.10567] $R_D = \mathcal{B}(B \rightarrow D \tau \nu) / \mathcal{B}(B \rightarrow D l \nu)$

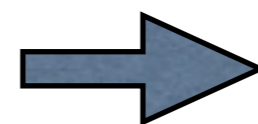
$$R_D^{\text{SM}} = 0.299 \pm 0.003,$$

$$R_{D^*}^{\text{SM}} = 0.257 \pm 0.003.$$

$$R_D^{\text{exp}} = 0.403 \pm 0.040 \pm 0.024,$$

$$R_{D^*}^{\text{exp}} = 0.310 \pm 0.015 \pm 0.008.$$

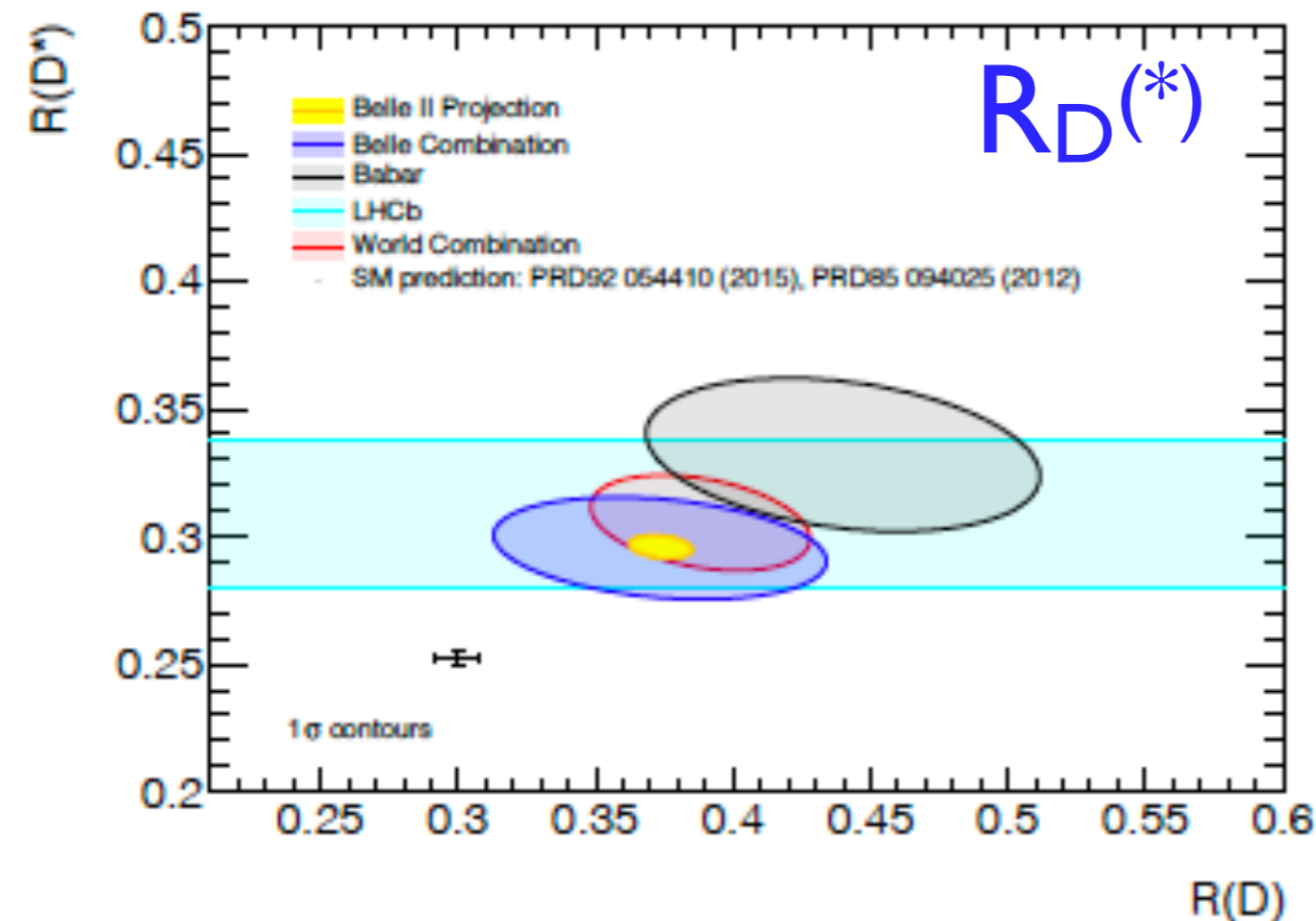
● 3.8σ anomalies in $B \rightarrow D^{(*)} \tau \nu$.



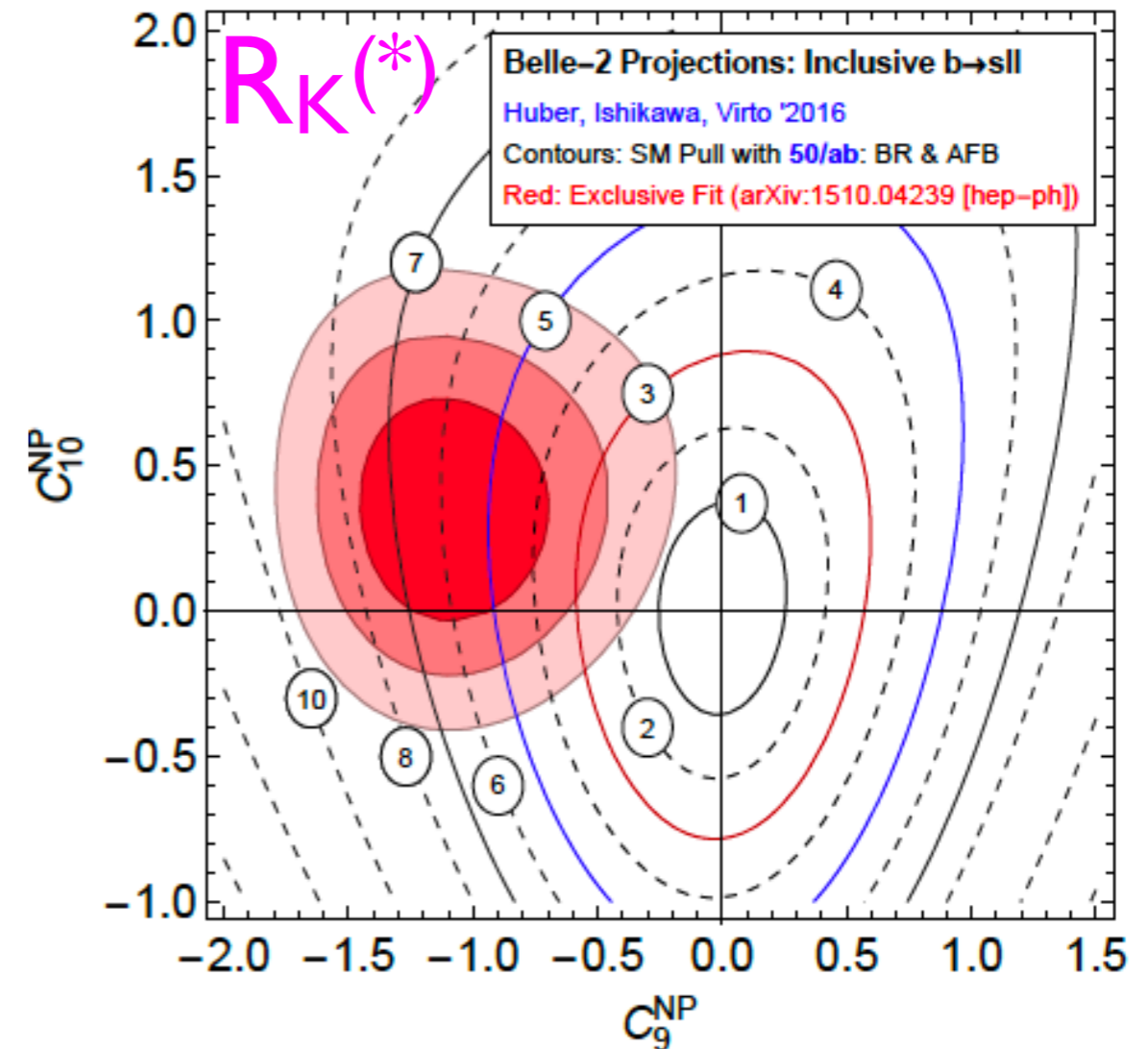
3.1σ after Belle (Moriond 2019).

Belle II for B-anomalies

-21-



[Belle-II, 1808.10567]



- Starting in 2019, Belle II can test LFUV in B-meson decays to few % accuracy with data of 5 ab^{-1} .

EFT for B-decays

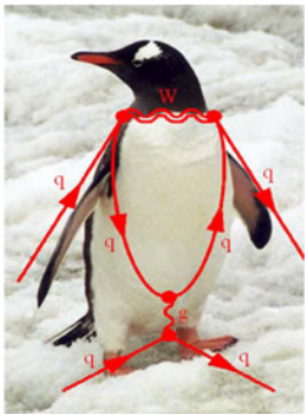
-22-

Effective Hamiltonian for $b \rightarrow s \mu \mu$:

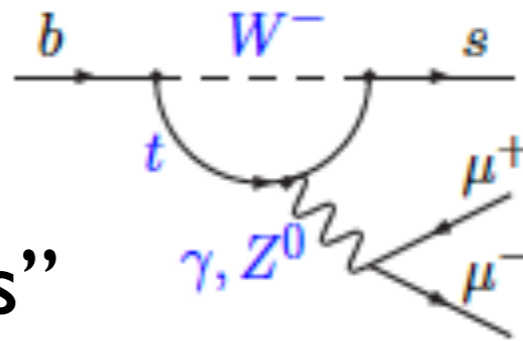
$$\mathcal{H}_{\text{eff}, \bar{b} \rightarrow \bar{s} \mu^+ \mu^-} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \frac{\alpha_{em}}{4\pi} (C_9^\mu \mathcal{O}_9^\mu + C_{10}^\mu \mathcal{O}_{10}^\mu + C_9^{\prime\mu} \mathcal{O}_9^{\prime\mu} + C_{10}^{\prime\mu} \mathcal{O}_{10}^{\prime\mu}) + \text{h.c.}$$

$$\mathcal{O}_9^\mu \equiv (\bar{s} \gamma^\mu P_L b) (\bar{\mu} \gamma_\mu \mu), \quad \mathcal{O}_{10}^\mu \equiv (\bar{s} \gamma^\mu P_L b) (\bar{\mu} \gamma_\mu \gamma^5 \mu), \quad C_9^{\mu, \text{SM}}(m_b) = -C_{10}^{\mu, \text{SM}}(m_b) = 4.27$$

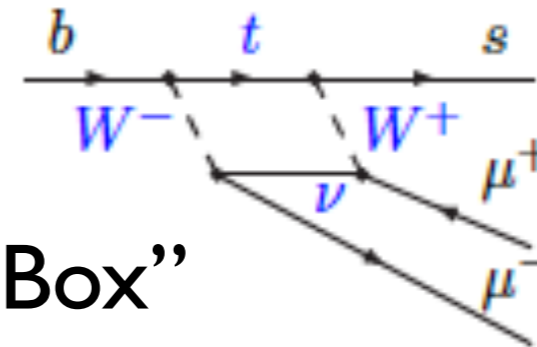
$$\mathcal{O}_9^{\prime\mu} \equiv (\bar{s} \gamma^\mu P_R b) (\bar{\mu} \gamma_\mu \mu), \quad \mathcal{O}_{10}^{\prime\mu} \equiv (\bar{s} \gamma^\mu P_R b) (\bar{\mu} \gamma_\mu \gamma^5 \mu) \quad C_9^{\prime\mu, \text{SM}}(m_b) \approx -C_{10}^{\prime\mu, \text{SM}}(m_b) \approx 0.$$



“Penguins”



“Box”

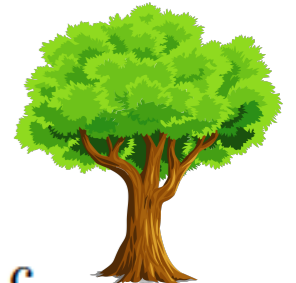


$$R_K[1, 6] \simeq 1 + 0.24 (C_{LL}^{\text{NP}\mu} + C_{RL}^\mu), \quad R_{K^*}[1, 6] \simeq 1 + 0.24 (C_{LL}^{\text{NP}\mu} - C_{RL}^\mu) + 0.07 C_{RL}^\mu,$$

$$C_{LL}^{\text{NP}\ell} = C_9^{\text{NP}\ell} - C_{10}^{\text{NP}\ell}, \quad C_{RL}^\ell = C_9^{\ell} - C_{10}^{\ell}$$

Effective Hamiltonian for $b \rightarrow c \tau \nu$:

“Tree”



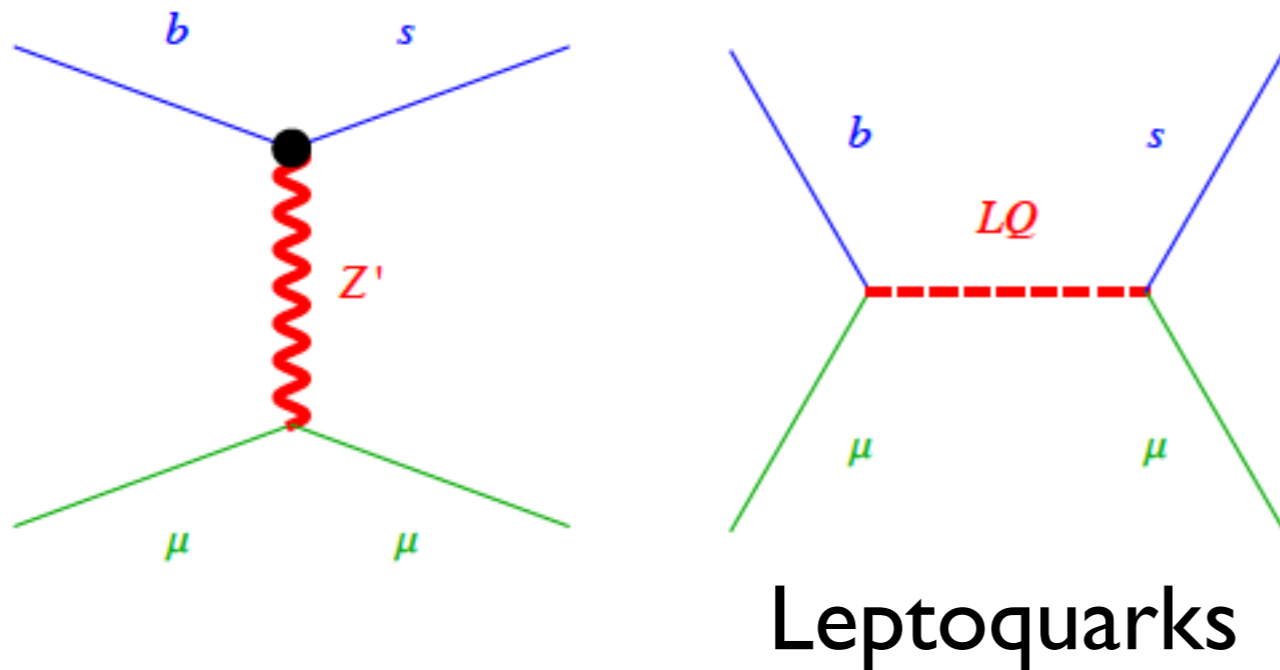
$$\mathcal{H}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{cb} \left[C_V (\bar{c} \gamma^\mu P_L b) (\bar{\tau} \gamma_\mu P_L \nu_\tau) + C_S (\bar{c} P_L b) (\bar{\tau} P_L \nu_\tau) + C_T (\bar{c} \sigma^{\mu\nu} P_L b) (\bar{\tau} \sigma_{\mu\nu} P_L \nu_\tau) \right] + \text{h.c.}$$

$$C_V = 1 \text{ and } C_S = C_T = 0 \text{ in the SM}$$

New physics for B-anomalies

-23-

New physics for $R_{K^{(*)}}$ anomalies:

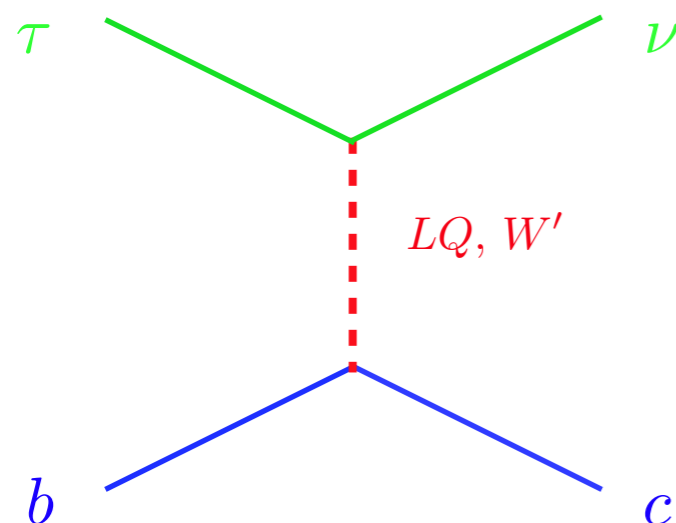


Z' , leptoquarks, loops, etc.

$$\mathcal{L}_{\text{eff}} = \frac{1}{\Lambda_{\text{NP}}^2} (\bar{s}\gamma^\mu P_L b)(\bar{\mu}\gamma_\mu \mu),$$

➔ $\Lambda_{\text{NP}} \simeq 30 \text{ TeV}.$

New physics for $R_{D^{(*)}}$ anomalies:



Leptoquarks, W' , charged Higgs, etc.

$$\mathcal{L}_{\text{eff}} = \frac{1}{\Lambda_{\text{NP}}^2} (\bar{c}\gamma^\mu P_L b)(\bar{\tau}\gamma_\mu P_L \nu_\tau),$$

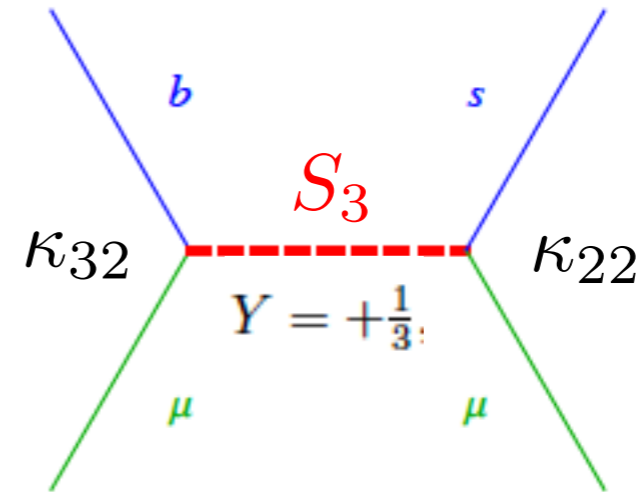
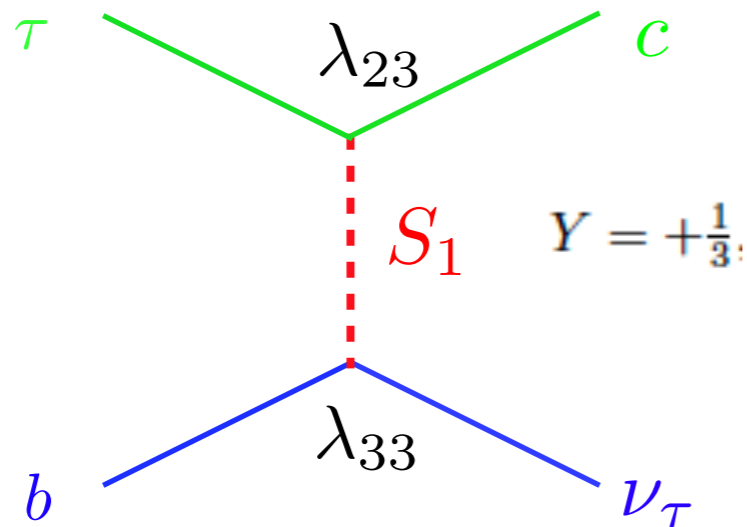
➔ $\Lambda_{\text{NP}} \simeq 3.5 \text{ TeV}.$

Scalar leptoquarks

-24-

$R_{D^{(*)}}$: Singlet leptoquark

$R_{K^{(*)}}$: Triplet leptoquark



$$\mathcal{L}_{S_1} = -\lambda_{ij} \overline{(Q^C)_{Ri}^a} (i\sigma^2)_{ab} S_1 L_{Lj}^b - \lambda'_{ij} \overline{(u^C)_{Li}} S_1 e_{jR} + \text{h.c.}$$

$$\mathcal{L}_{S_3} = -\kappa_{ij} Q_{Li}^a \Phi_{ab} L_{Lj}^b + \text{h.c.}$$

$B - \bar{B}$ mixing : loop-suppressed, unlike Z' case.

$B_s \rightarrow \mu^+ \mu^-$: constrains the triplet leptoquark.

$B \rightarrow K^{(*)} \nu \bar{\nu}$: tree-level corrections due to singlet leptoquark.

$$B(B \rightarrow K \nu \bar{\nu}) \Big|_{\text{SM}} = (3.98 \pm 0.43 \pm 0.19) \times 10^{-6}, \quad B(B \rightarrow K^* \nu \bar{\nu}) \Big|_{\text{SM}} = (9.19 \pm 0.86 \pm 0.50) \times 10^{-6}$$

$$B(B \rightarrow K \nu \bar{\nu}) < 1.6 \times 10^{-5}, \quad [\text{Belle}]$$

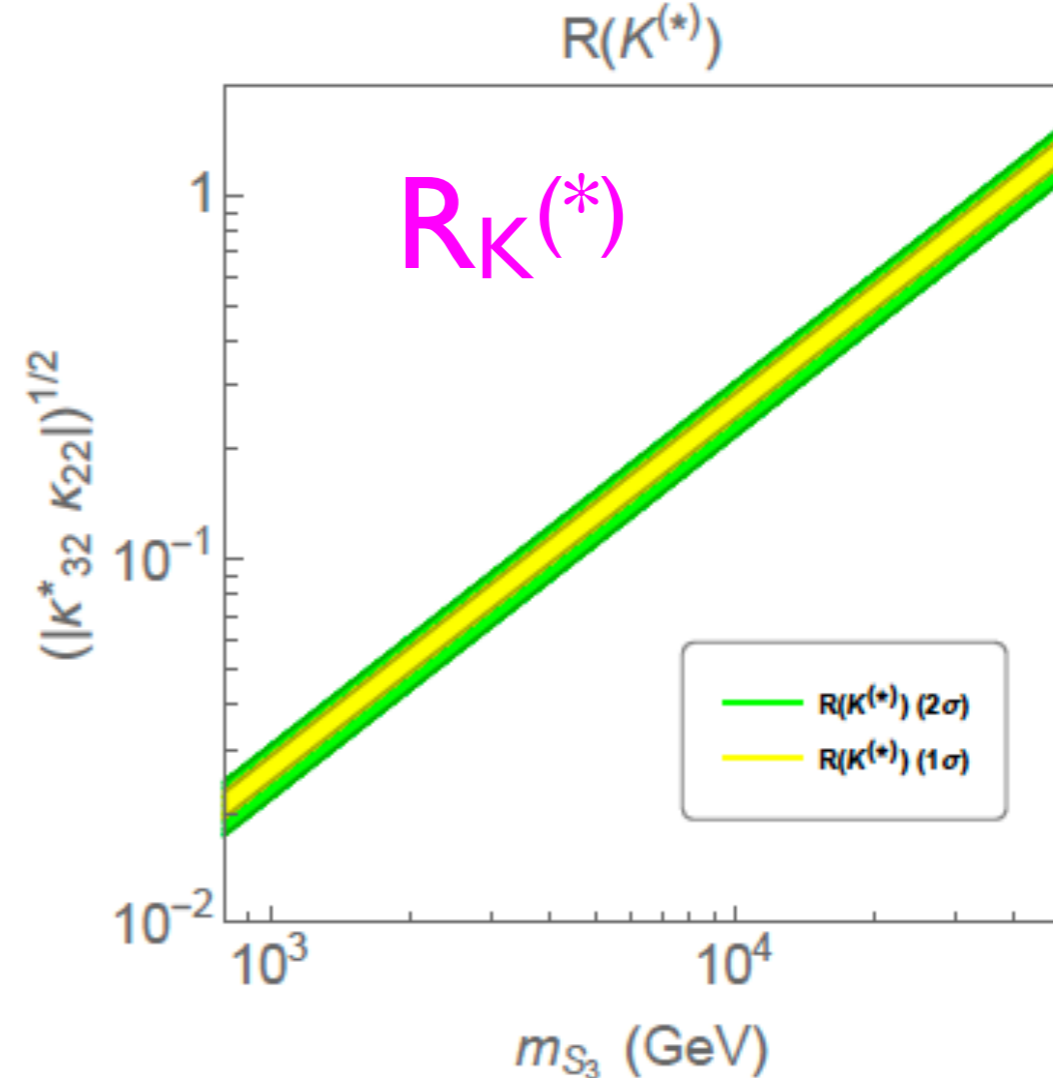
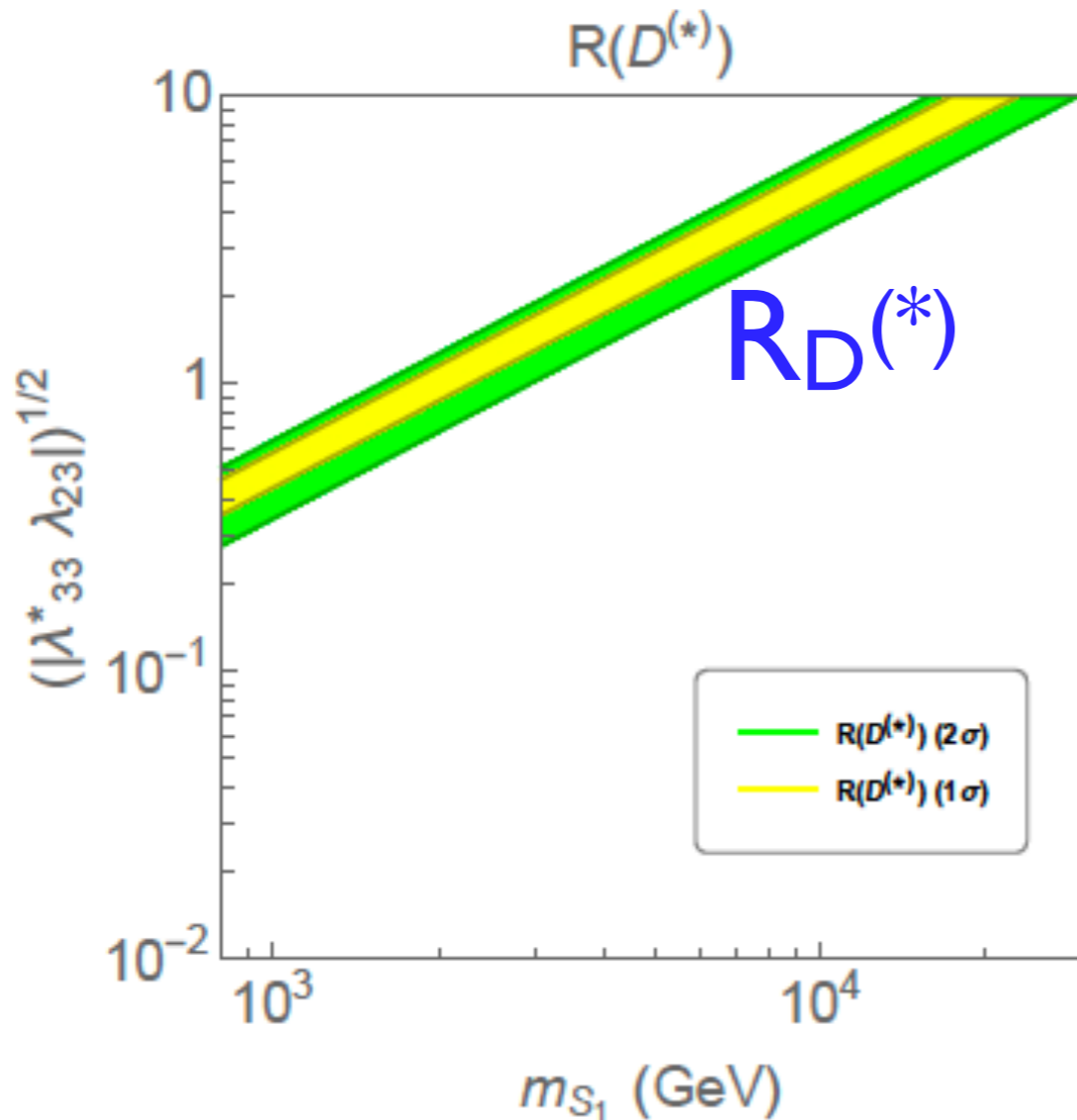
$$B(B \rightarrow K^* \nu \bar{\nu}) < 2.7 \times 10^{-5}$$

Belle-2 at 10% level => strong constraints on leptoquark models.

Scalar leptoquarks

-25-

[Choi, Kang, HML, Ro, 2018]



Minimal flavor:

$$\lambda = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & \lambda_{23} \\ 0 & \lambda_{32} & \lambda_{33} \end{pmatrix}, \quad \kappa = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \kappa_{22} & \kappa_{23} \\ 0 & \kappa_{32} & \kappa_{33} \end{pmatrix}$$

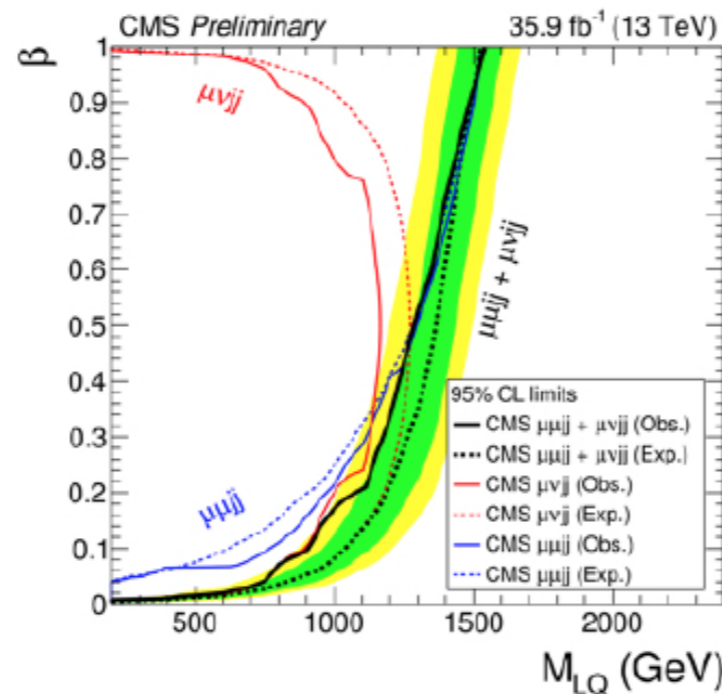
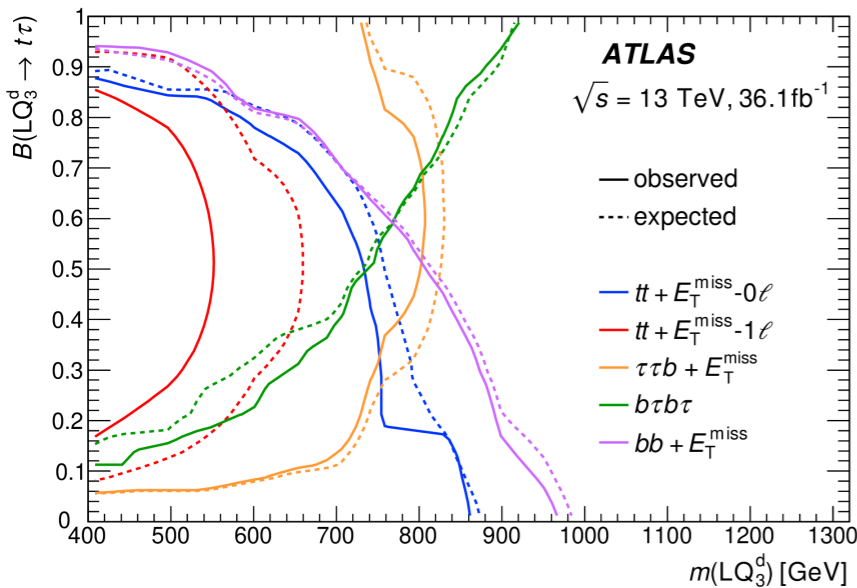
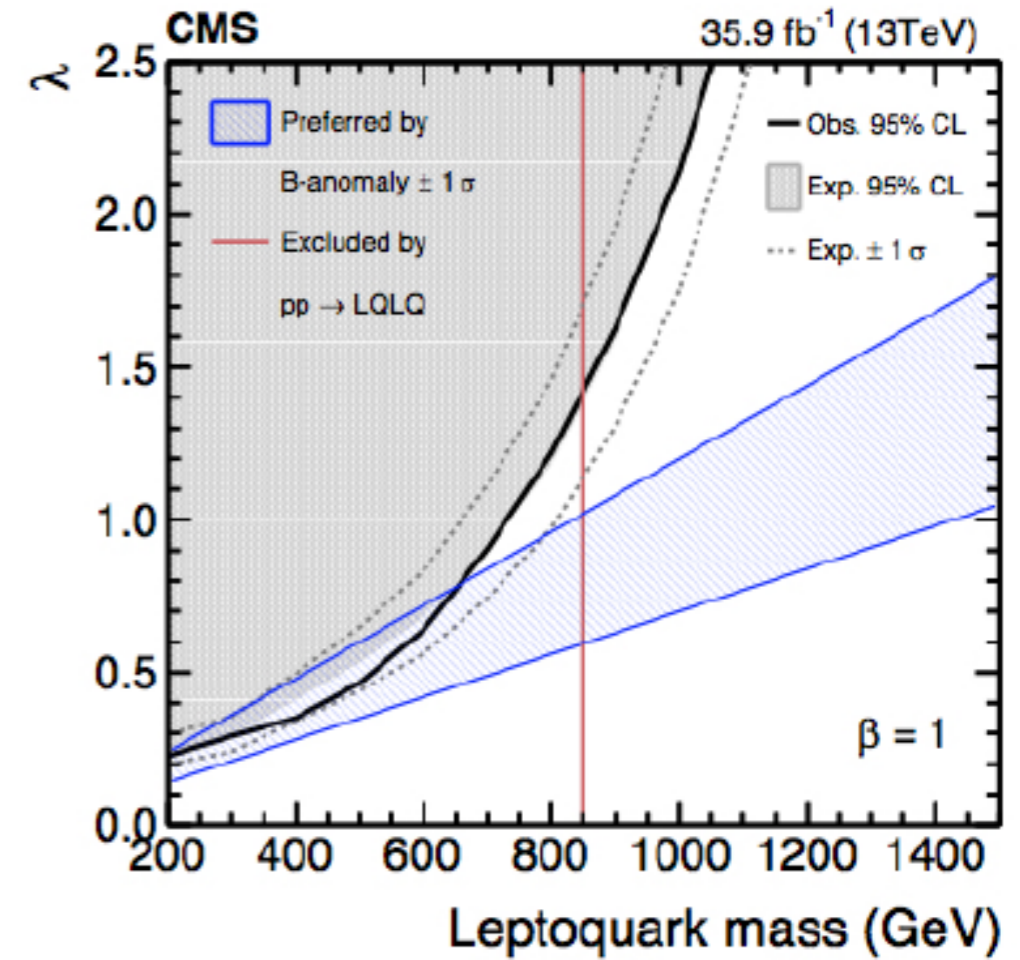
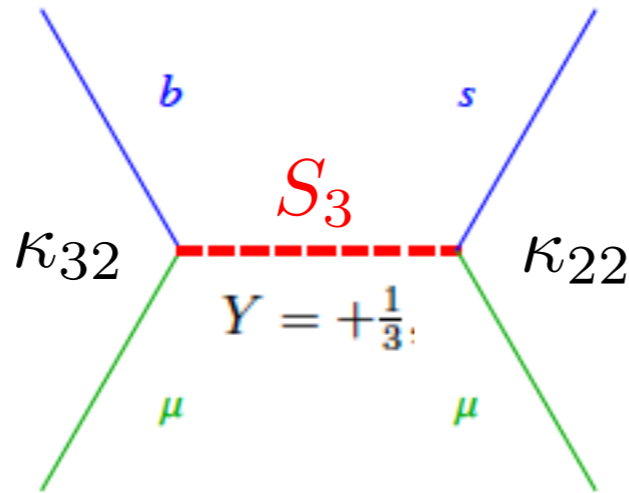
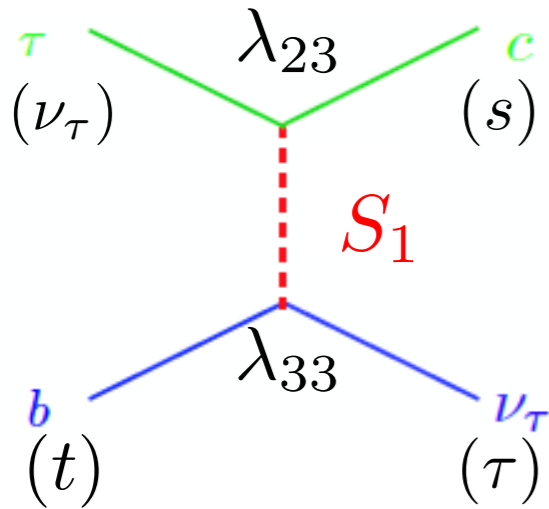
leptons \rightarrow quarks

for $B \rightarrow K^{(*)} \nu \bar{\nu}$

$$\frac{|\kappa_{33}^* \kappa_{23}|}{|\lambda_{33}^* \lambda_{23}|} \approx \frac{|\kappa_{32}^* \kappa_{23}|}{|\lambda_{32}^* \lambda_{23}|} \approx \frac{m_{S_3}^2}{m_{S_1}^2}$$

Hunting leptoquarks

-26-



[Choi, Kang, HML, Ro, 2018]

LQs	BRs	$m_{LQ, \min}$	BRs	$m_{LQ, \min}$
S_1	$B(\bar{t}\bar{\tau}/b\nu_{\tau}) = \frac{1}{2}\beta$	1.22 TeV ($b\nu_{\tau}$) [32]	$B(\bar{c}\bar{\tau}/s\nu_{\tau}) = \frac{1}{2}(1 - \beta)$	950 GeV ($\nu_{\tau}j$) [33]
$S_3(\phi_1)$	$B(\bar{b}\bar{\mu}) = \gamma$	1.4 TeV [34]	$B(\bar{s}\bar{\mu}) = 1 - \gamma$	1.08 TeV ($\bar{\mu}j$) [35]
$S_3(\phi_2)$	$B(\bar{t}\bar{\mu}/b\bar{\nu}_{\mu}) = \frac{1}{2}\gamma$	1.45 TeV ($\bar{t}\bar{\mu}$) [36]	$B(\bar{c}\bar{\mu}/s\bar{\nu}_{\mu}) = \frac{1}{2}(1 - \gamma)$	850 GeV ($\bar{\mu}\bar{\nu}_{\mu}jj$) [37]
$S_3(\phi_3)$	$B(\bar{t}\bar{\nu}_{\mu}) = \gamma$	1.12 TeV [38]	$B(\bar{c}\bar{\nu}_{\mu}) = 1 - \gamma$	950 GeV ($\bar{\nu}_{\mu}j$) [33]

“Decay BRs”

$$\beta \equiv \lambda_{33}^2 / (\lambda_{33}^2 + \lambda_{23}^2)$$

$$\gamma \equiv \kappa_{32}^2 / (\kappa_{32}^2 + \kappa_{22}^2)$$

Lepton g-2, LFV, EDM

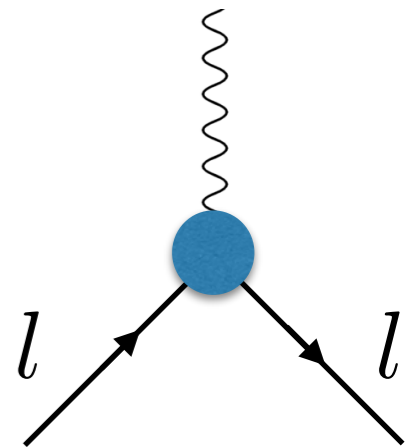
-27-

- Lepton g-2 and lepton flavor violation are important precision tests of the SM.

Muon g-2: $a_\mu(E821) = 116592089(63) \times 10^{-11}$

$$a_\mu(\text{FNAL}) = 116\,592\,040(54) \times 10^{-11}$$

$$a_\mu(\text{Exp}) = 116\,592\,061(41) \times 10^{-11}$$



$$a_\mu(\text{Exp}) - a_\mu(\text{SM}) = (251 \pm 59) \times 10^{-11}$$

4.2 σ from SM

Electron g-2: $\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} = -89(36) \times 10^{-14}$ [Cs] -2.5 σ

$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} = 47(30) \times 10^{-14}$$
 [Rb] 1.6 σ

Bounds on LFV: $\text{BR}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$ [MEG]

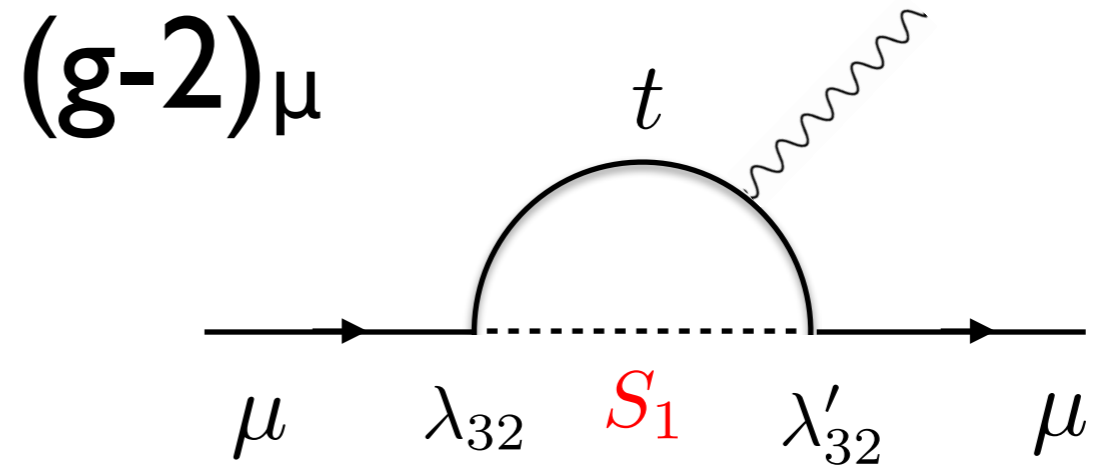
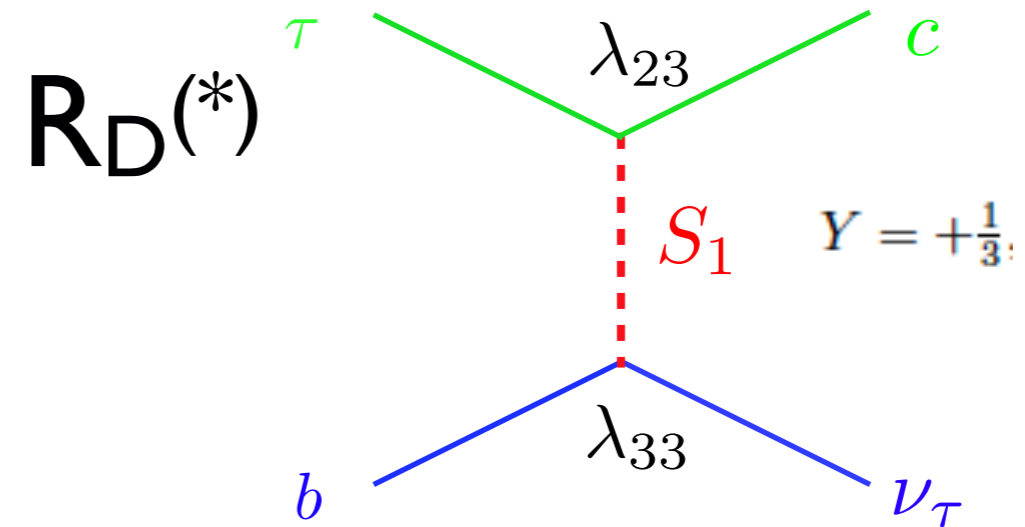
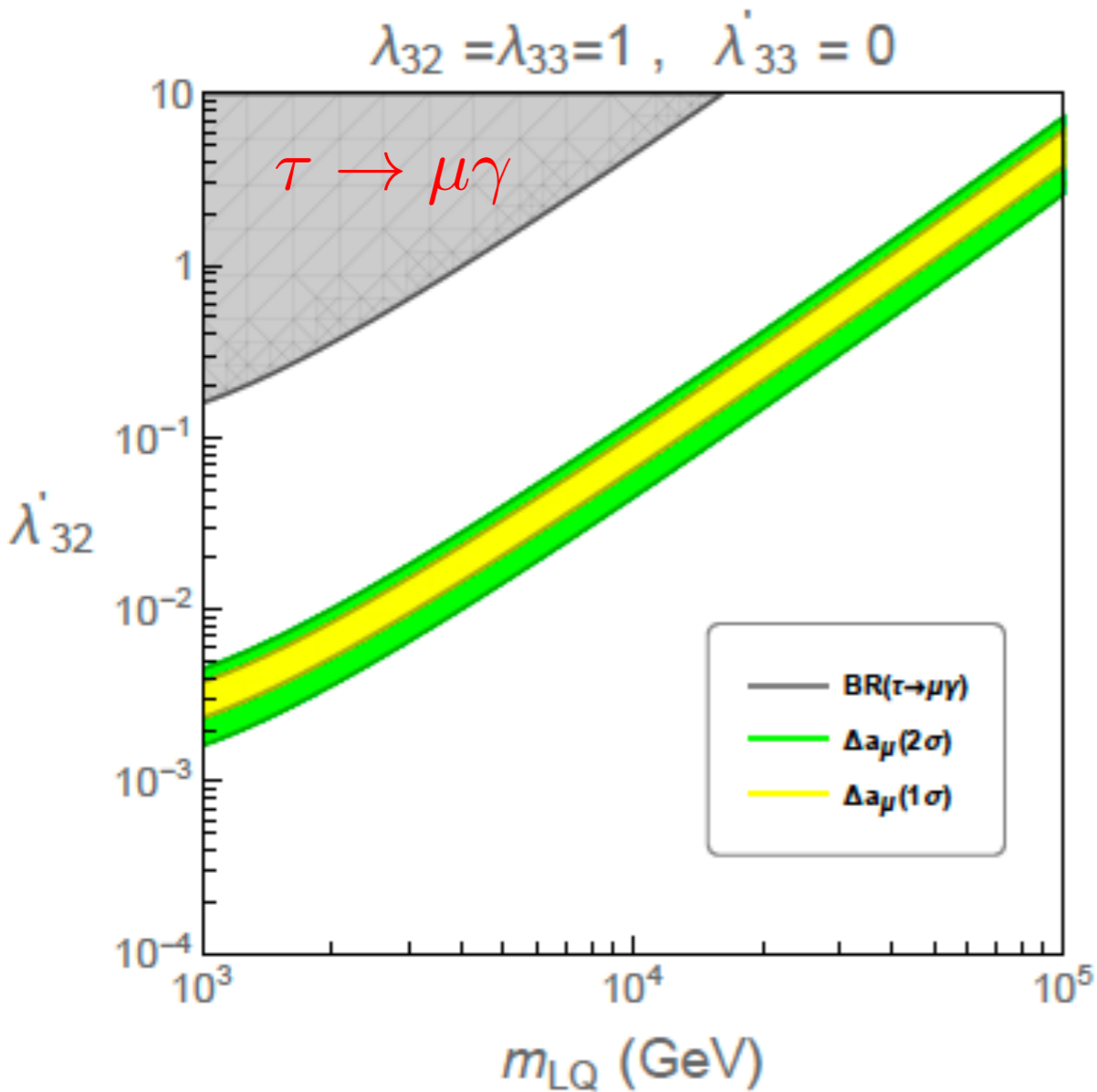
$$\text{BR}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$$

$$\text{BR}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8}$$

EDM: $d_e < 1.1 \times 10^{-29}$ e cm [ACMEII] $d_\mu < 1.5 \times 10^{-19}$ e cm

Lepton $g-2$ from top loops

-28-



Minimal flavor: Top + Singlet leptoquark loops

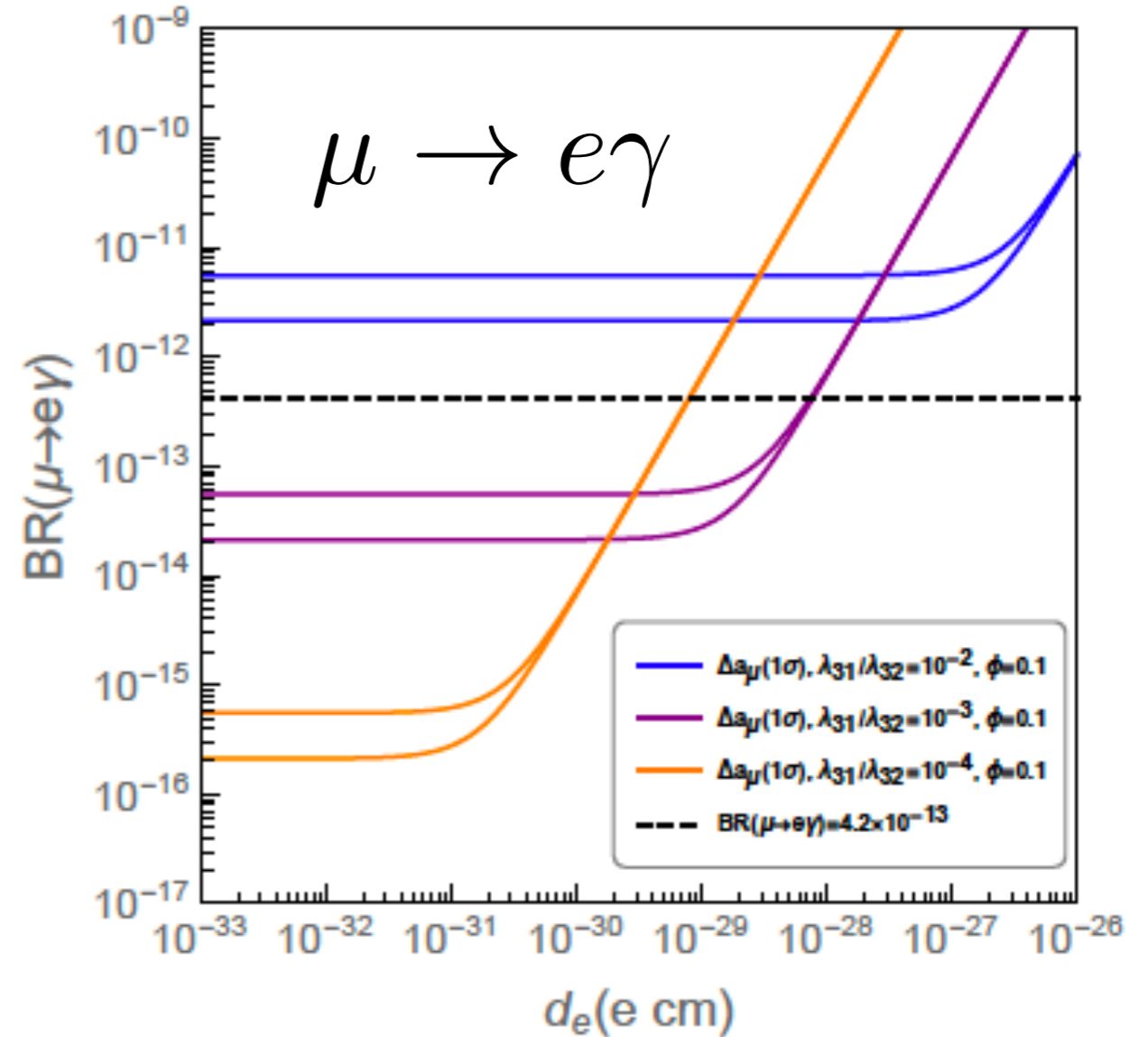
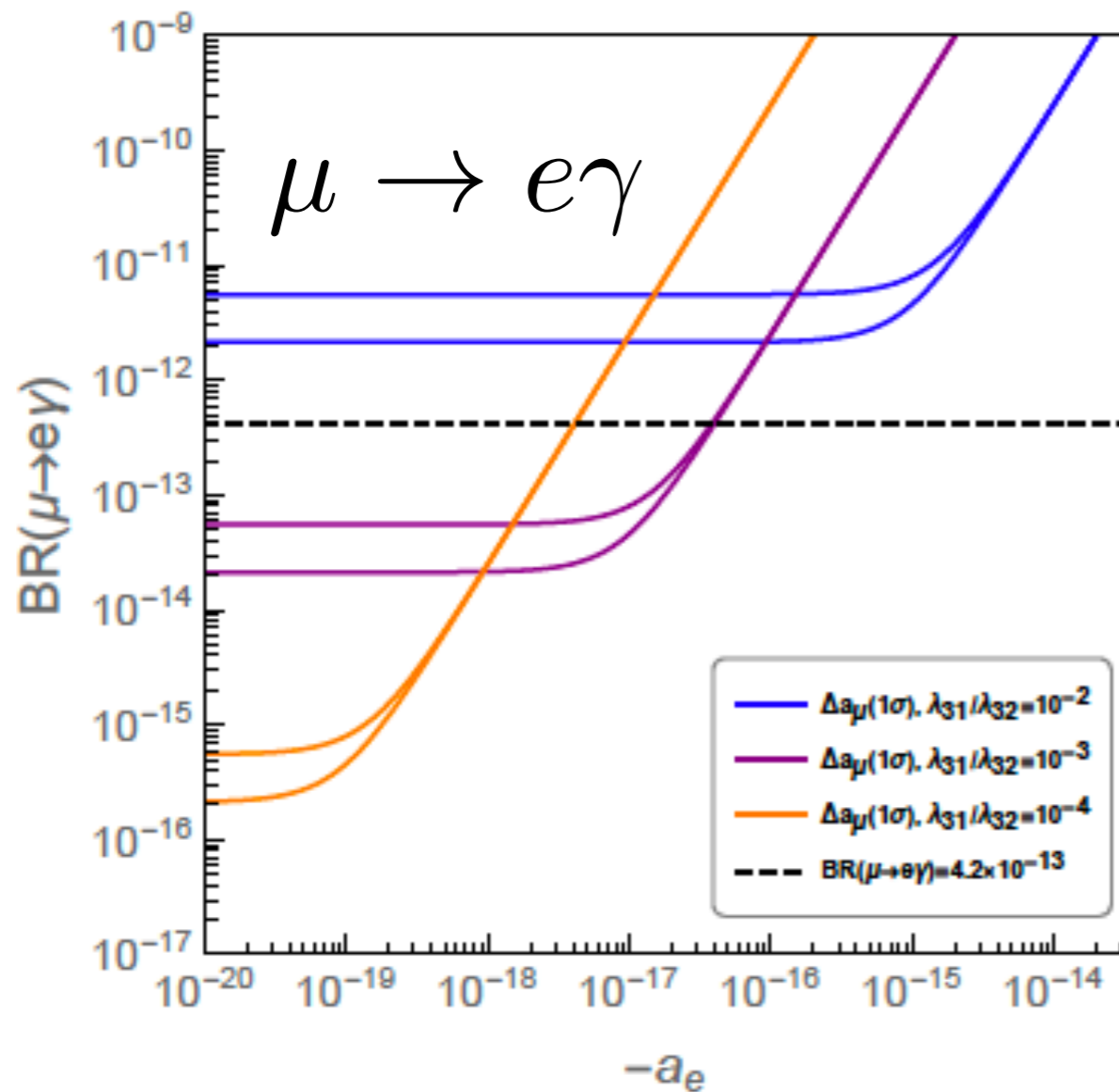
[Choi, Kang, HML, Ro, 2018]

$\rightarrow a_\mu, a_e$

Leptonic signatures

-29-

[HML, 2021]



Strong constraint from $\mu \rightarrow e\gamma$

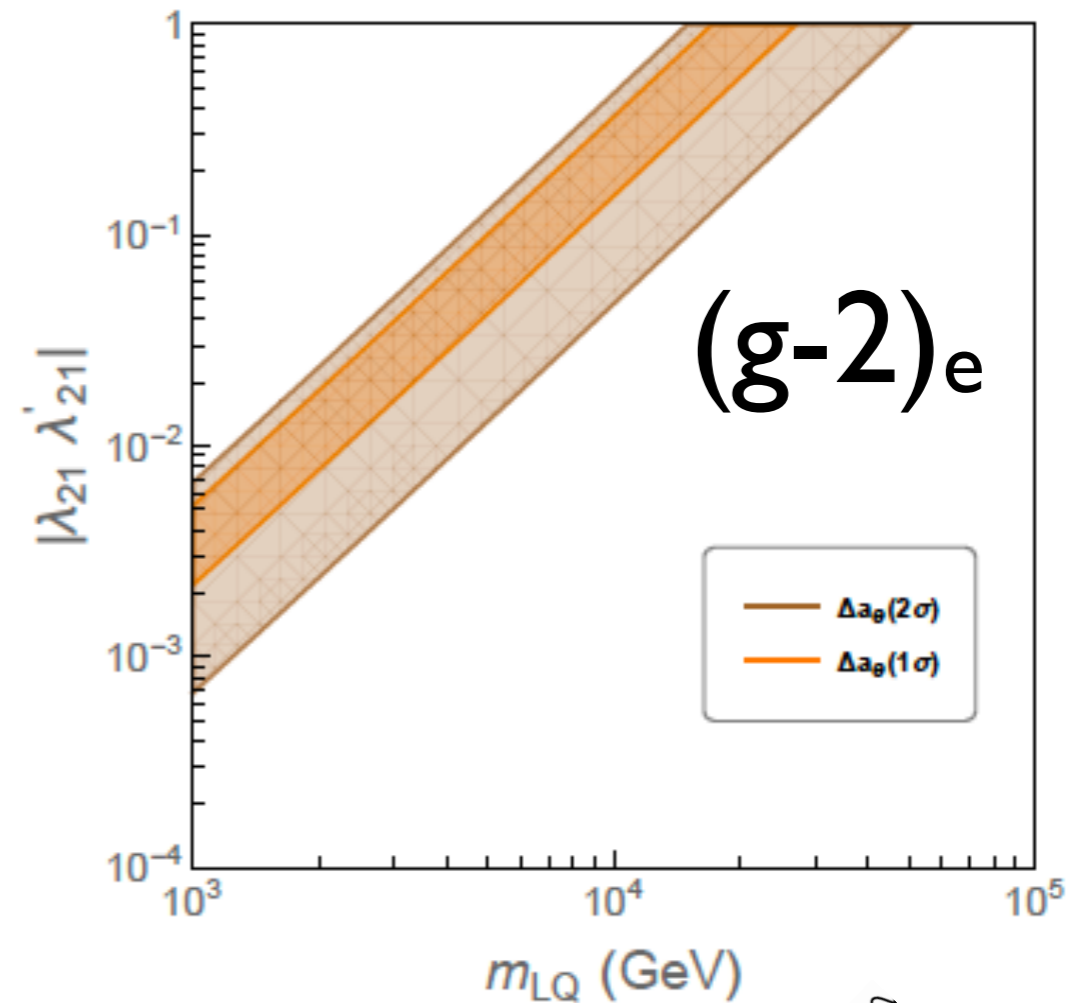
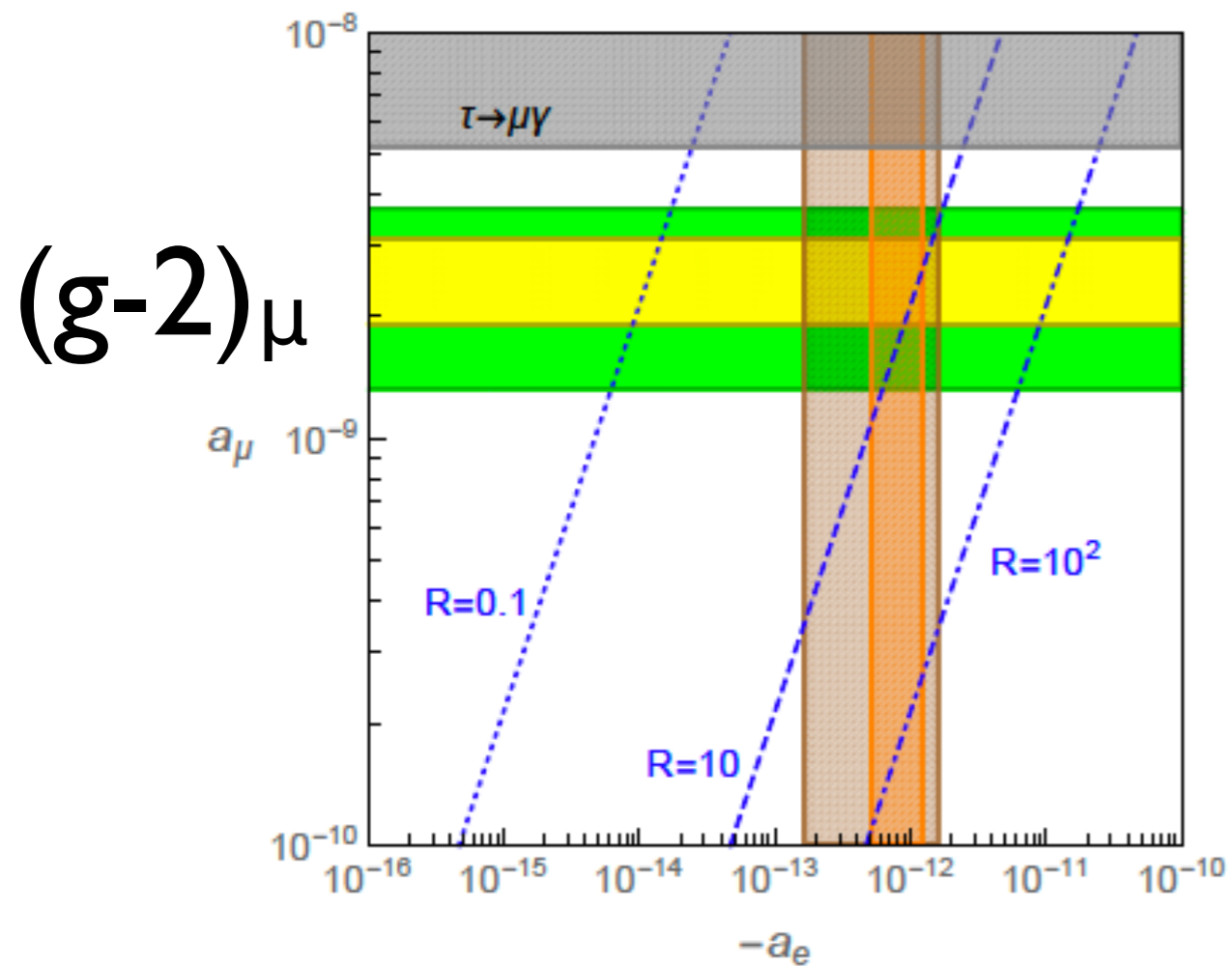


Small electron g-2

But, electron EDM is detectable for a sizable CP phase.

Muon $g-2$ from charm loops

-30-

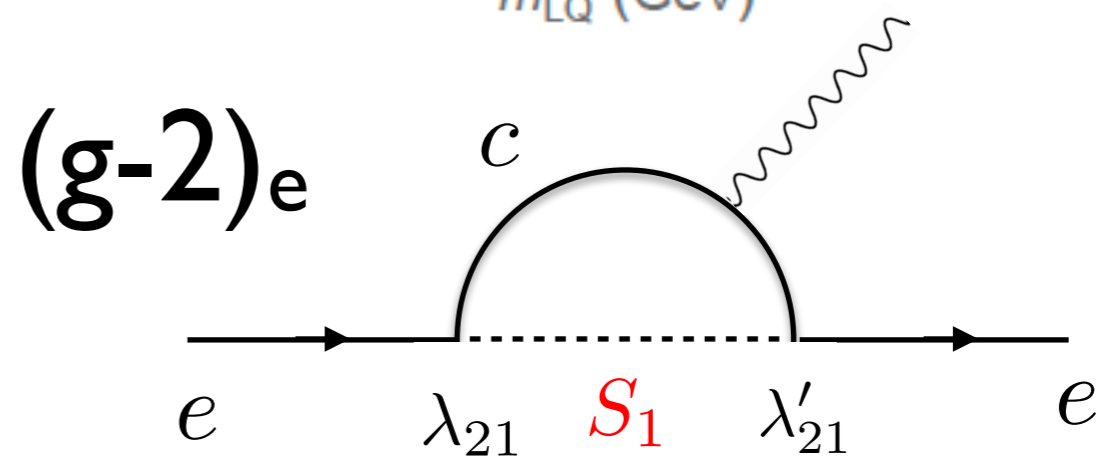


Electron $g-2$ specific flavor:

[HML, 2021]

Top loops $\rightarrow a_\mu$

Charm loops $\rightarrow a_e$



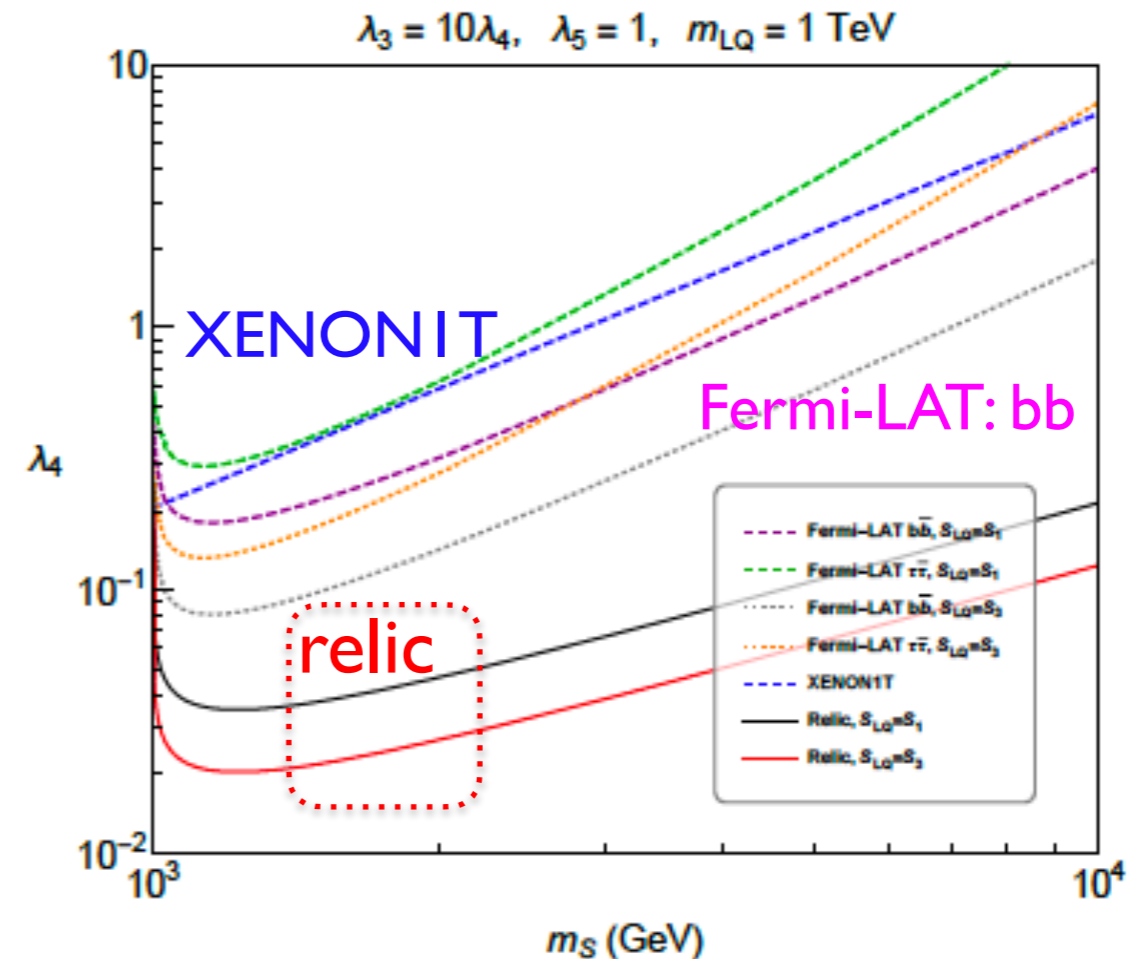
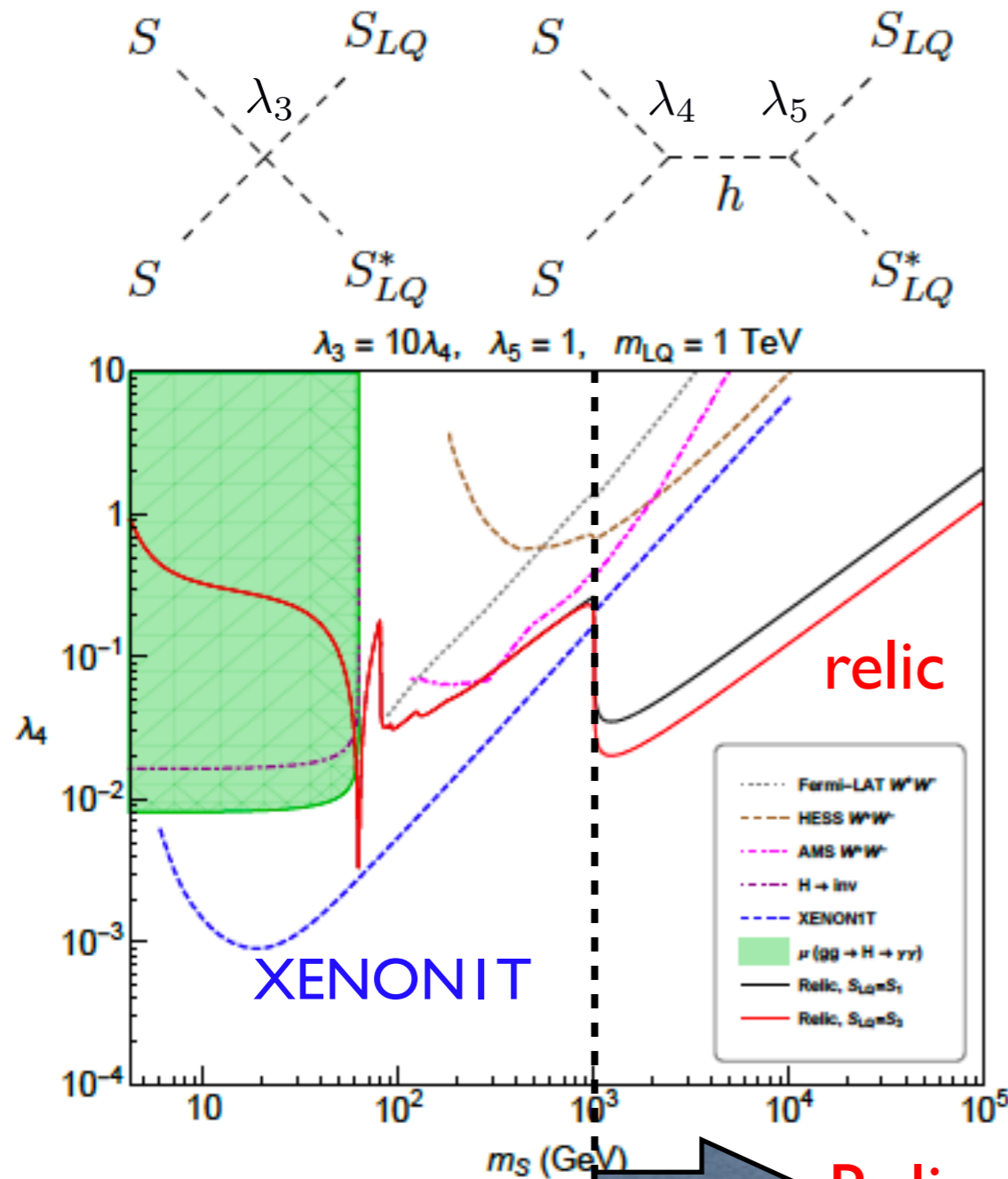
$$\frac{a_e^{S_1}}{a_\mu^{S_1}} = \frac{m_e m_c}{m_\mu m_t} \cdot R, \quad R = \frac{\text{Re}(\lambda_{21} \lambda'_{21}^*)}{\text{Re}(\lambda_{32} \lambda'_{32}^*)}$$

LQ-portal dark matter

-31-

[Choi, Kang, HML, Ro, 2018]

Annihilation into a LQ pair make Higgs-portal dark matter consistent.



➔ Relic density is ok; DM indirect signals!

$$R_{D^{(*)}}: \lambda_{33} \gg \lambda_{23}$$

$$B(\bar{t}t \bar{\tau}\tau) : B(\bar{b}b \bar{\nu}_\tau \nu_\tau) : B(\bar{t}b \bar{\tau}\nu_\tau + \text{h.c.}) = \frac{1}{2} : \frac{1}{2} : 1$$

$$R_{K^{(*)}}: \kappa_{32} \gg \kappa_{22}$$

$$B(\bar{b}b \bar{\mu}\mu) : B(\bar{t}t \bar{\mu}\mu) : B(\bar{b}b \bar{\nu}_\mu \nu_\mu) : B(\bar{t}b \bar{\mu}\nu_\mu + \text{h.c.}) : B(\bar{t}t \bar{\nu}_\mu \nu_\mu) \\ = 1 : \frac{1}{4} : \frac{1}{4} : \frac{1}{2} : 1.$$

Conclusions

- **Light dark matter and mediators** can be probed at Belle-II and LHCb, in addition to direct and indirect detections.
- **Flavor puzzles in B-meson decays** may call for new forces or extra colored particles, thus opening a window for complementary between energy and intensity frontiers.
- **Searches for light dark sector and B-meson decays at Belle-II and LHCb** would lead to a crucial guideline for flavor physics in next decades.
- **Existing anomalies in muon $g-2$** might be related to B-meson and XENONIT anomalies, and testable at Belle-II.